

PROCEEDINGS OF SPIE

***Advances in X-Ray/EUV Optics  
and Components III***

**Ali M. Khounsary**  
**Christian Morawe**  
**Shunji Goto**  
*Editors*

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- 2 Mirrors + Metrology  
**Ali M. Khounsary**, Argonne National Laboratory (United States)
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Focus on X-Ray Focusing Workshop

**Ali M. Khounsary**, Argonne National Laboratory (United States)

**Christian Morawe**, European Synchrotron Radiation Facility (France)

**Shunji Goto**, Japan Synchrotron Radiation Research Institute (Japan)

# **Focus on X-Ray Focusing Workshop**

August 13, 2008

"Focus on X-Ray Focusing" was the title of a one-day workshop during Optics + Photonics 2008 held on August 13, 2008 in conjunction with the Advances in X-Ray/EUV Optics and Components III conference. The aim of the Workshop was to provide the audience with a comprehensive introduction and up-to-date information on various X-ray focusing techniques covering theory, development, implementation, progress and applications. The Workshop consisted of ten presentations by some of the renowned practitioners in the field, each describing one of the focusing techniques and its challenges, limitations, and prospects.

Workshop Chairs:

**Ali Khounsary**, Argonne National Laboratory

**Christian Morawe**, European Synchrotron Radiation Facility (France)

**Shunji Goto**, Japan Synchrotron Radiation Research Institute (Japan)

**Introduction to x-ray focusing**, Franz Pfeiffer, Swiss Light Source, Paul Scherrer Institute and Ecole Polytechnique Fédérale de Lausanne (Switzerland)

**X-ray focusing with Kirkpatrick-Baez optics**, K. Yamauchi, Osaka Univ. (Japan)

**Hard x-ray focusing with curved reflective multilayers**, Christian Morawe, European Synchrotron Radiation Facility (France)

**Refractive x-ray lenses for hard x-ray microscopy**, Christian G. Schroer, Technische Univ. Dresden (Germany)

**Kinoform x-ray lens arrays**, Werner H. Jark, Sincrotrone Trieste (Italy)

**Monocapillary optics**, Ladislav Pina, Czech Technical Univ. (Czech Republic)  
(presentation not available)

**X-ray focusing with polycapillary optics**, Carolyn A. MacDonald, SUNY, Univ. at Albany

**Focusing of x-rays using crystal optics**, Eckhart Förster, Friedrich-Schiller-Univ. Jena (Germany)

**Multilayer Laue Lens for efficient nanometer focusing of hard x-rays**, G. B. Stephenson, Argonne National Lab.

**Diffractive focusing by zone plates**, Michael Feser, Xradia, Inc.

13<sup>th</sup> August 2008

# *Introduction to X-Ray Focusing*

Franz Pfeiffer

Swiss Light Source, Paul Scherrer Institut  
& École Polytechnique Fédérale de Lausanne



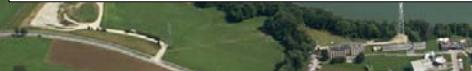
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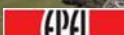
Coherent Imaging group  
at PSI & EPFL

Franz Pfeiffer      Oliver Bunk      Andreas Menzel      Xavier Donath      Pierre Thibault      Cameron Kewish      Martin Dierolf      Tobias Boehlen





 Christian David, Joan Vila, Konstantins Jefimovs, Vitaliy Guzenko, Harun Solak, Sankha Sarkar,  
Laboratory for Micro- and Nanotechnology,  
Paul Scherrer Institut, CH

Swiss Light Source

# *Outline*

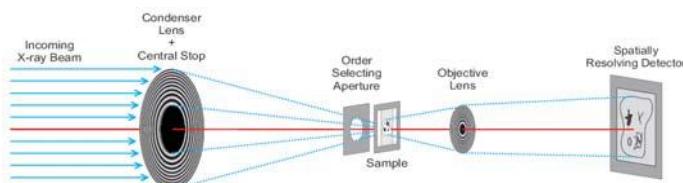
1. X-ray focusing – Why
2. Methods overview – focus on X-ray waveguides
3. Recent advances at Paul Scherrer Institut
4. ‘Super-Resolution’ coherent X-ray microscopy  
& characterization of focused wave-fields



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>

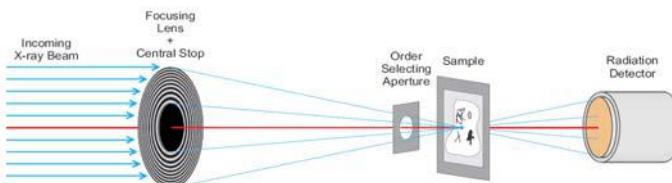


## *X-ray Focusing – Why*



+ fast  
- only x-ray transmission signal

full-field microscope



+ many detection schemes possible (elemental & chemical specificity, crystalline ordering, ...)  
- requires coherent illumination

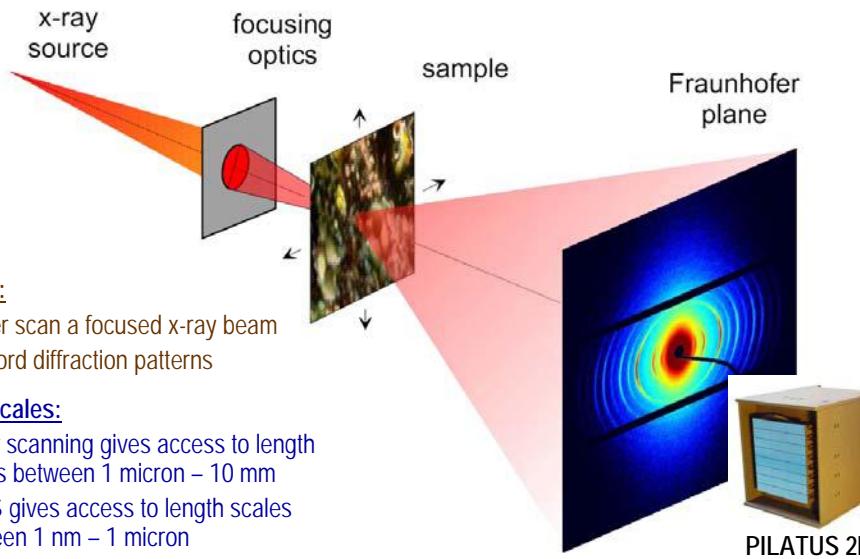
scanning microscope



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# *Small-Angle X-Ray Scattering (SAXS) & Scanning Microscopy*



## Principle:

- Raster scan a focused x-ray beam & record diffraction patterns

## Length Scales:

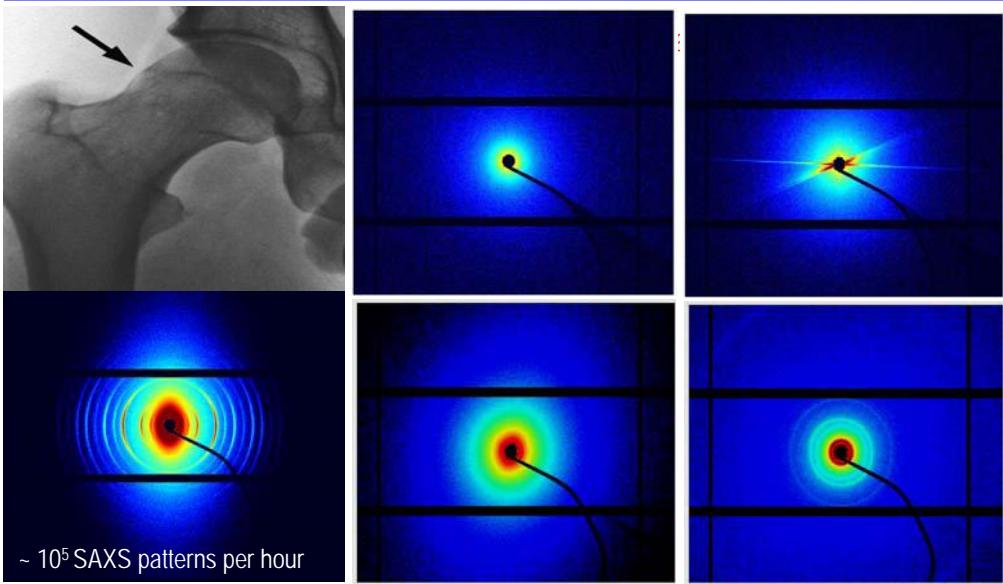
- raster scanning gives access to length scales between 1 micron – 10 mm
- SAXS gives access to length scales between 1 nm – 1 micron



Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



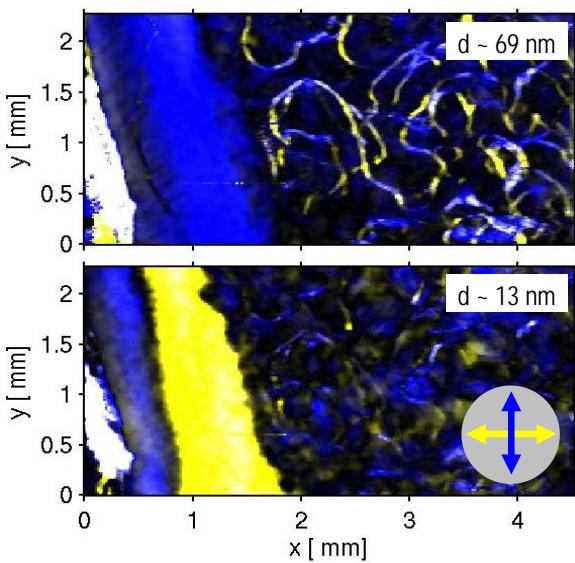
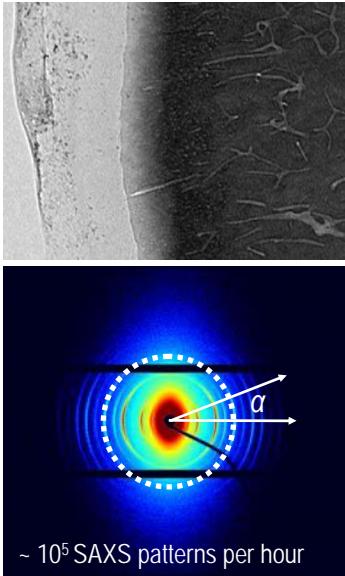
# *Small-Angle X-Ray Scattering (SAXS) & Scanning Microscopy*



Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



# *Small-Angle X-Ray Scattering (SAXS) & Scanning Microscopy*



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## *Outline*

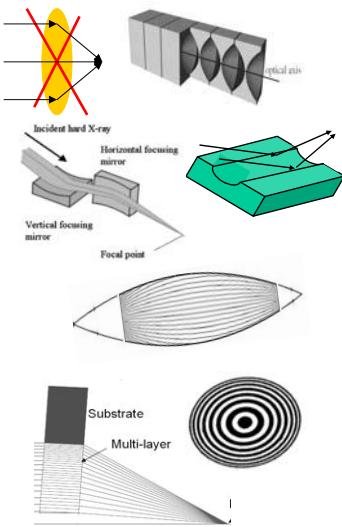
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# X-Ray Focusing - HOWTO



## Take a lens: Yes, but ...

Compound refractive lenses [C. Schroer & W. Jark]

## Reflective optics

Kirkpatrick-Baez optics [K. Yamamauchi]

Curved reflective multilayers [C. Morawe]

Bragg-reflective optics [F. Foerster]

## Capillary optics

Monocapillary optics [L. Pina]

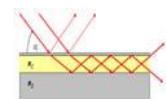
Polycapillary optics [C.A. Mc Donald]

## Diffractive optics

Fresnel Zone Plates [M. Feser]

Multilayer Laue Lenses [G.B. Stephenson]

## ...and Waveguides



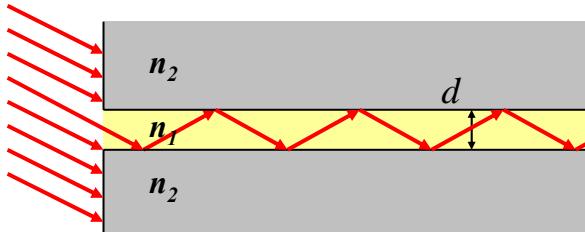
Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# X-ray waveguides

X-rays

$\lambda \sim 0.1 \text{ nm}$ ,  $d \sim 50 \text{ nm}$



Transmission  
 $\ll 1\%$



Y. P. Feng et al., Phys. Rev. Lett. 71, 537 (1993);  
S. Lagomarsino et al., Appl. Phys. Lett. 71, 2557 (1997);  
S. Di Fonzo et al., Nature 403, 638 (2000).

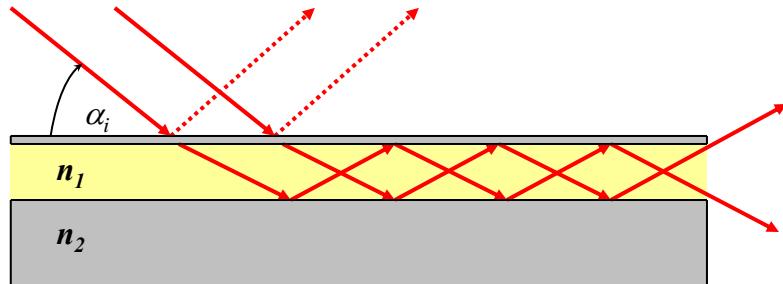


Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# Resonant beam coupling waveguides

$$\alpha_{c,n_1} < \alpha_i < \alpha_{c,n_2}$$



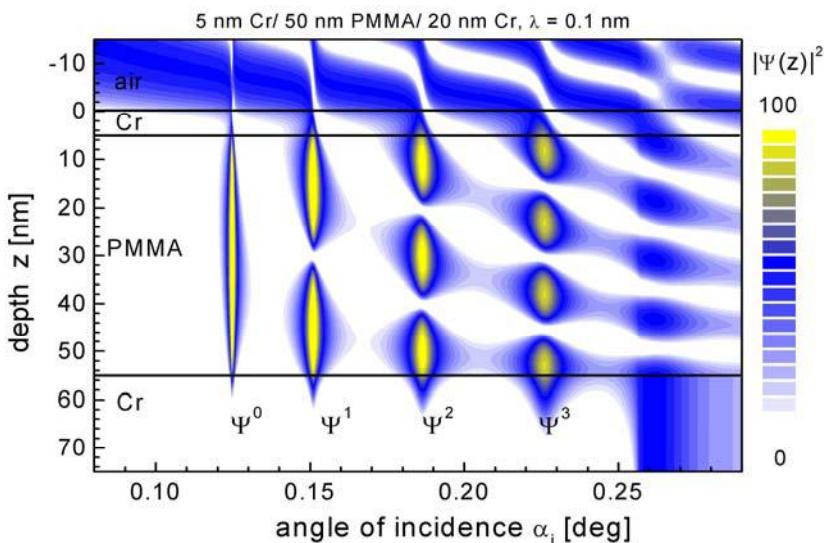
F. Pfeiffer et al., Physical Review B 62(24), 16939-16943 (2000)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## Field distribution in 1D resonant beam coupling waveguides



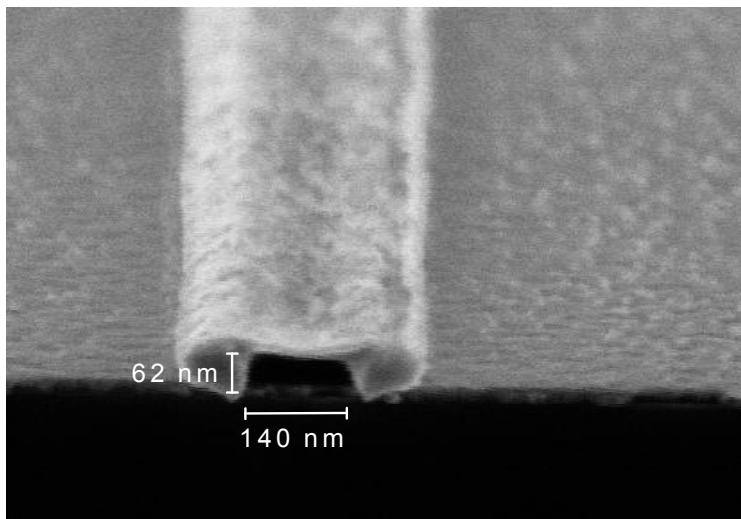
F. Pfeiffer et al., Physical Review B 62(24), 16939-16943 (2000)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## 2D Waveguides



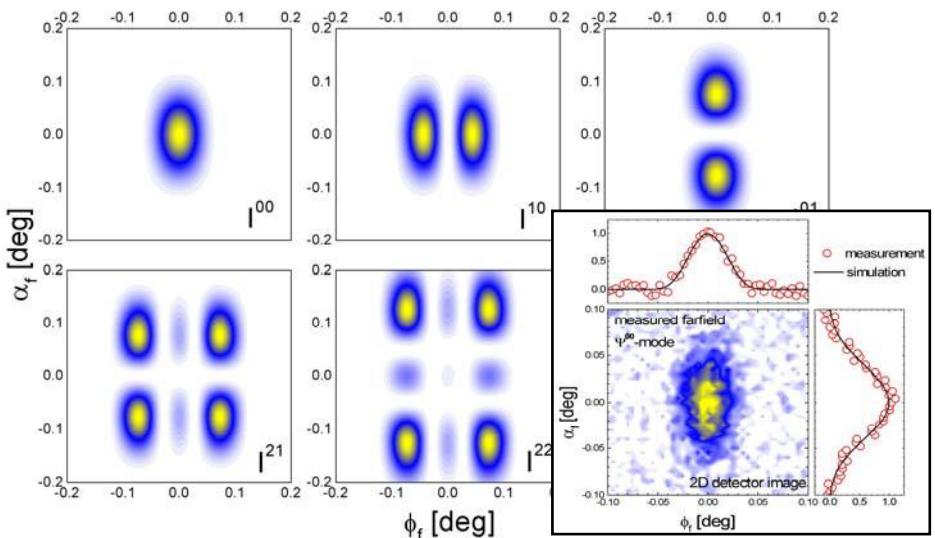
F. Pfeiffer, et al., Science 297, 205 (2002)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## Farfield pattern of modes in 2D x-ray waveguides

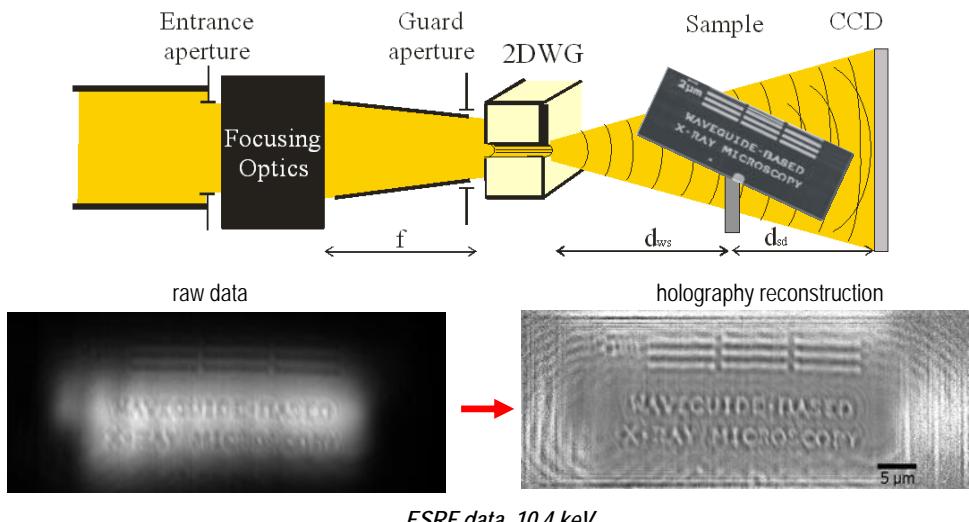


F. Pfeiffer, et al., Science 297, 205 (2002)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>





ESRF data, 10.4 keV

C. Fuhse et al., Appl. Phys. Lett. 85 (2004) & C. Fuhse et al., Phys. Rev. Lett. (2006)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## Outline

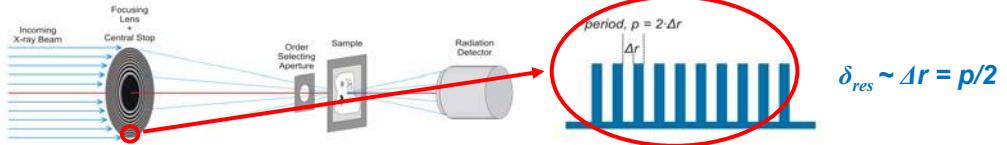
1. X-ray focusing – Why
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3. Recent advances at Paul Scherrer Institut
  - > Fresnel Zone Plate fabrication by EUV inference lithography
  - > Zone-doubling technique for ultra-high resolution FZP
4. 'Super-Resolution' coherent X-ray microscopy  
& characterization of focused wave-fields



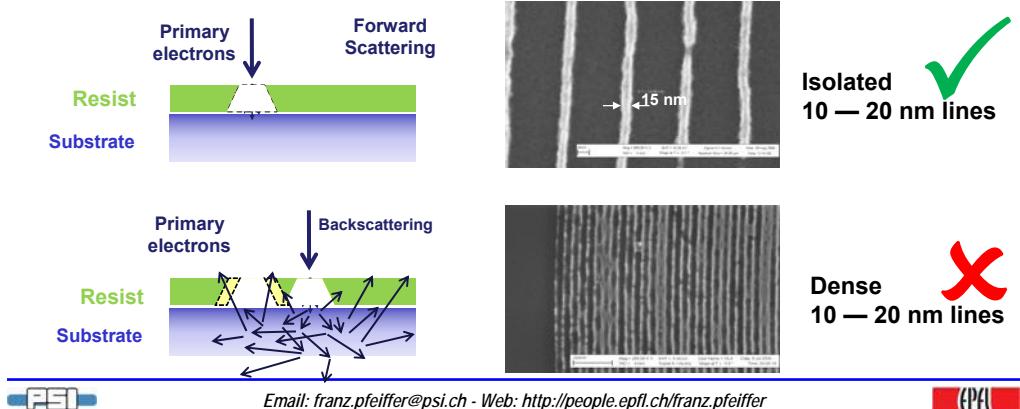
Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# Spatial resolution limit in x-ray microscopy



## e-beam lithography limits



PSI

Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>

EPFL

## Possible solutions

W. L. Chao et al. NATURE 435 (2005) 1210-1213



Figure 2 | An illustration of the overlay nanofabrication technique for micro zone plate fabrication.

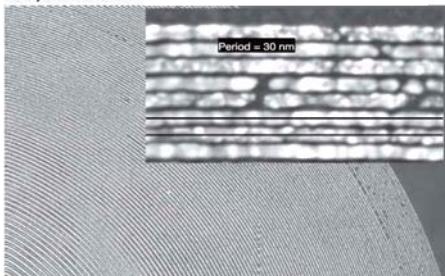
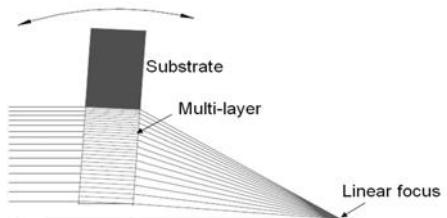


Figure 3 | Scanning electron micrograph of a zone plate with 15 nm outermost zone. Shown in the inset is a more detailed view of the outermost zones. The zonal period, as indicated by the two black lines, is measured to be 30 nm. The zone placement accuracy is measured to be 1.7 nm.

H. C. Kang et al. PRL96 (2006) 127401



### The Swiss alternatives:

- FZP fabrication by EUV inference lithography
- Zone-doubled FZP

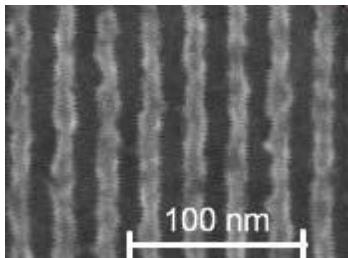
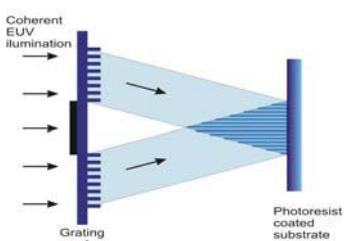
PSI

Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>

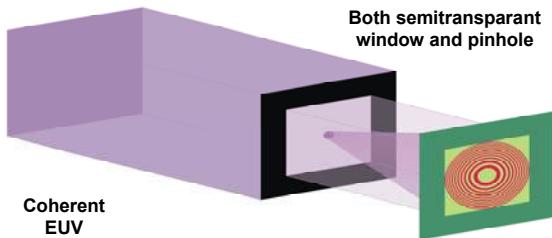
EPFL

## *FZP fabrication by EUV inference lithography (H. Solak)*

work by Sankha S. Sarkar, Yasin Ekinci, and Harun Solak @ PSI



**Solak HH, Ekinci Y, Kaser P, Park S**  
*Photon-beam lithography reaches 12.5 nm half-pitch resolution.*  
JOURNAL OF VACUUM SCIENCE & TECHNOLOGY B 25, 91 (2007)



Advantages in relation to e-beam lithography:

- Parallel writing
  - No Proximity effect
  - No Finite pixel size

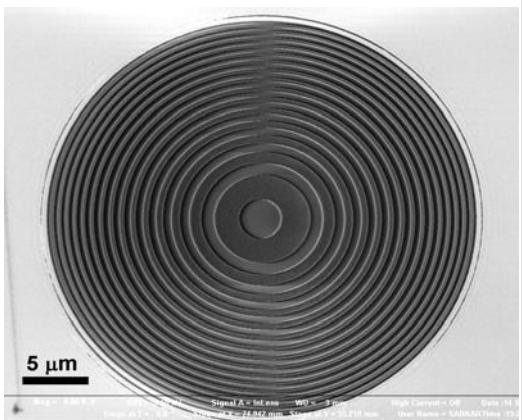
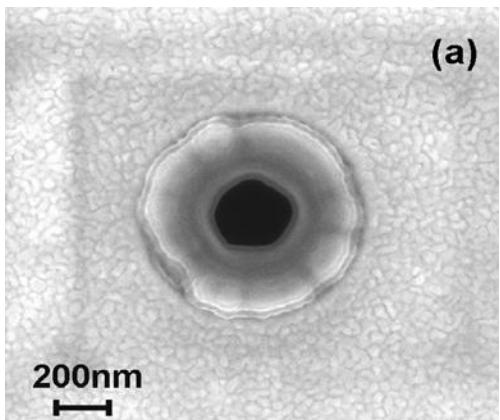


Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



## *FZP fabrication by EUV lithography*

work by Sankha S. Sarkar, Yasin Ekinci, and Harun Solak @ PSI



Pinhole Diameter ~ 300 nm

**Distance from mask ~ 600  $\mu\text{m}$**

$N = 30$ ,  $D \sim 32 \mu\text{m}$

$\Delta r_N \sim 260$  nm

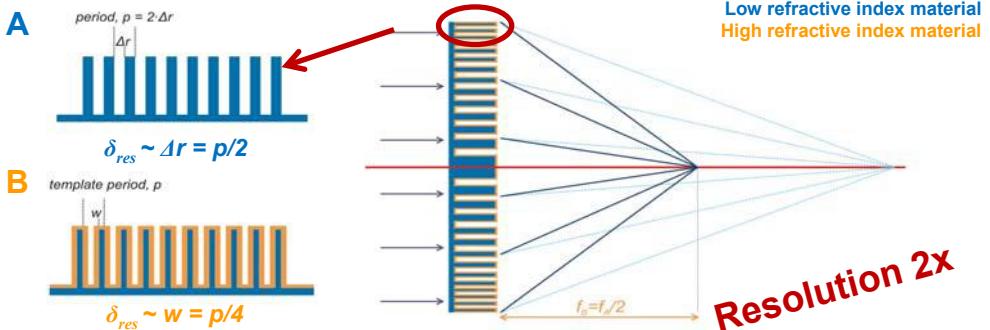


Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



# Zone-doubling for high resolution FZP (slides J. Vila)

work by J. Vila, K. Jefimovs, and C. David @ PSI



Manufacturing advantages:

- No alignment required
- One single EBL exposure

K. Jefimovs et al., Phys. Rev. Lett. 99, 264801 (2007)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>

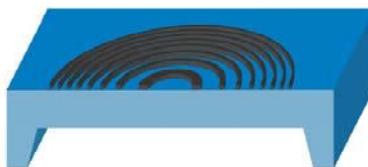


# Zone-doubling for high resolution FZP (slides J. Vila)

1) Substrate preparation and e-beam lithography (0.25 duty cycle at the outer regions)



2) Cr mask dry etching in a Cl<sub>2</sub>:CO<sub>2</sub> plasma



3) Silicon RIE in a CHF<sub>3</sub>:SF<sub>6</sub>:O<sub>2</sub> plasma



ALD Deposition @ University of Helsinki T. Pilvi & M. Ritala

4) Iridium coating by atomic layer deposition



Low refractive index material → Silicon

High refractive index material → Iridium

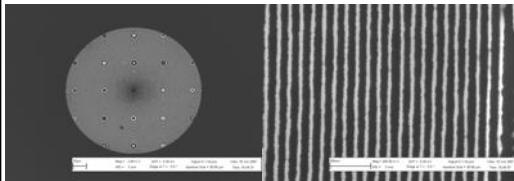


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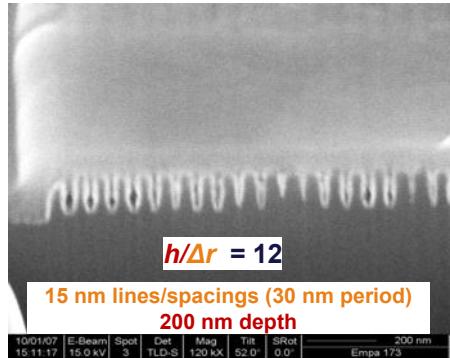
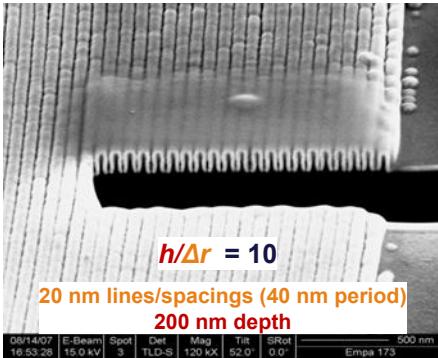
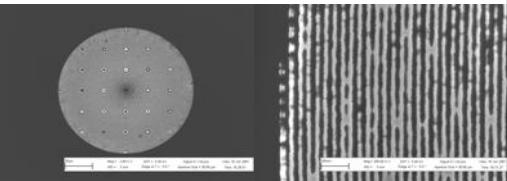


## Zone-doubling for high resolution FZP (*slides J. Vila*)

FZP with D = 100 $\mu$ m,  $\Delta r$  = 20 nm



FZP with D = 100 $\mu$ m,  $\Delta r$  = 15 nm

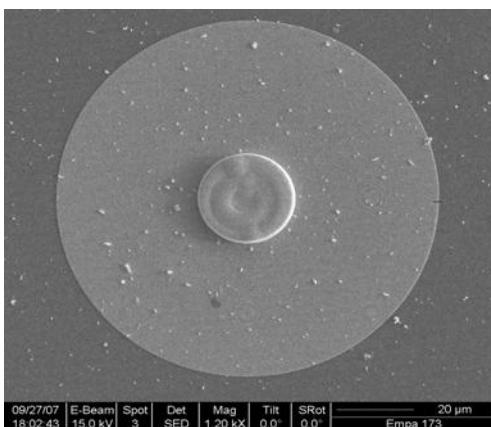


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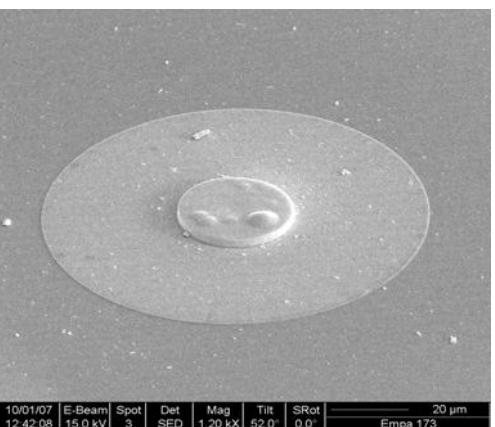


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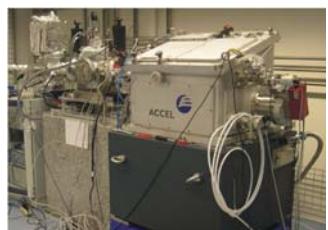
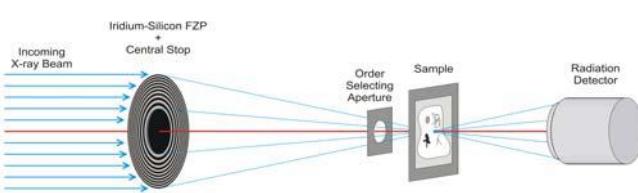
20  $\mu$ m diameter central stops made of 1.5  $\mu$ m thick layer of Pt by  
FIB induced deposition.



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# *STXM @ PolLux beamline of SLS (J. Raabe & G. Tzvetkov)*

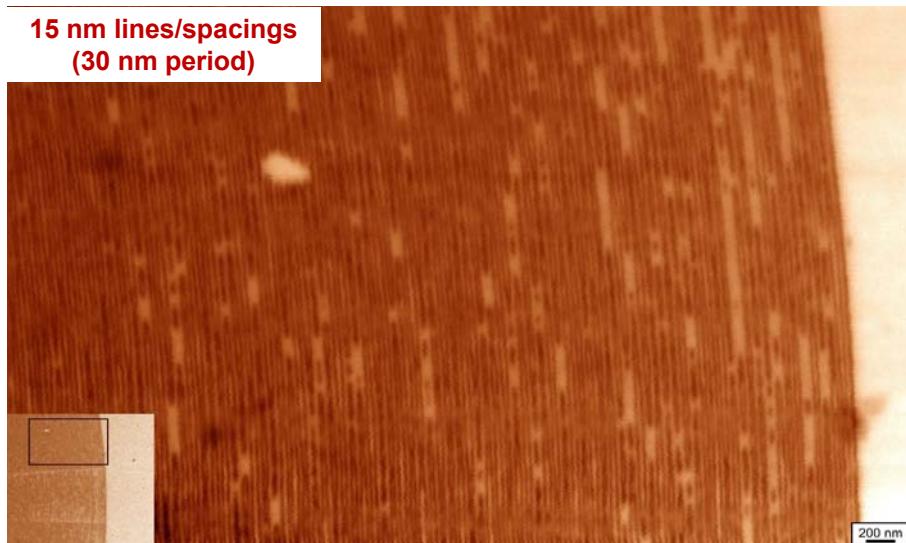


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# *STXM @ PolLux beamline of SLS (J. Raabe & G. Tzvetkov)*

**15 nm lines/spacings  
(30 nm period)**



1.0 keV  
photon  
energy



Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



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4. **'Super-Resolution' coherent X-ray microscopy & characterization of focused wave-fields**



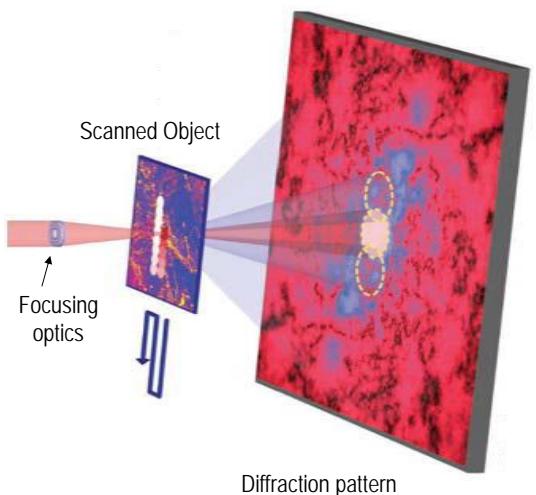
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## *'Super-Resolution' Coherent Scanning X-Ray Microscopy*

### Principles:

- In standard scanning x-ray microscopy, resolution is limited to probe size
- Collect coherent diffraction patterns while scanning the spot (Ptychography)
- Phase and amplitude of the object can be retrieved with *enhanced resolution*



P. Thibault, M. Dierolf, A. Menzel, O. Bunk, C. David, F. Pfeiffer, SCIENCE 321, 379-382 (2008)



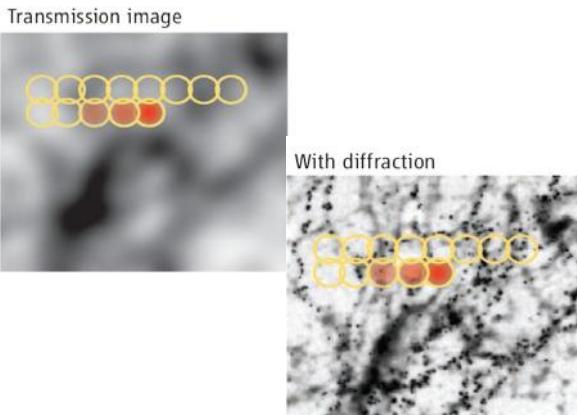
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P. Thibault, M. Dierolf, A. Menzel, O. Bunk, C. David, F. Pfeiffer, SCIENCE 321, 379-382 (2008)



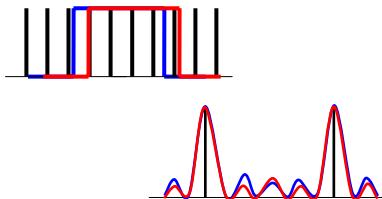
Email: [franz.pfeiffer@psi.ch](mailto:franz.pfeiffer@psi.ch) - Web: <http://people.epfl.ch/franz.pfeiffer>



## *Ptychographic phase retrieval*



- W. Hoppe,  
Acta Cryst. A 25, 508  
(1969).
  - R. Hegerl, W. Hoppe, Ber.  
Bunsen-Ges. Phys. Chemie  
74, 1148 (1970).



1148

R. Hegerl und W. Hoppe: Dynamische Theorie der Kristallstrukturanalyse vom

Berichte der  
Bunsen-Gesellschaft

## Dynamische Theorie der Kristallstrukturanalyse durch Elektronenbeugung im inhomogenen Primärstrahlwellenfeld

U. R. H. A. 333

Some time ago a new principle was proposed for the registration of the complete information (amplitudes and phases) in a diffraction diagram, which does not – as does Holography – require the interference of the scattered waves with a single reference wave. The basis of the principle lies in the interference of neighbouring scattered waves which result when the object function  $\varrho(x,y)$  is multiplied by a generalized primary wave function  $p(x,y)$  in Fourier space (diffraction diagram) this is a convolution of the Fourier transforms of these functions. The above mentioned interferences necessary for the phase determination can be obtained by suitable choice of the shape of  $p(x,y)$ . To distinguish it from holography this procedure is designated "pychography" ( $\pi\tau\tau\xi = \text{fold}$ ). The procedure is applicable to periodic and aperiodic structures. The relationships are simplest for plane lattices. In this paper the theory is extended to space lattices both with and without consideration of the dynamic theory. The resulting effects are demonstrated using a practical example.



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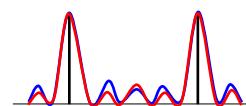
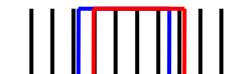


# Ptychographic phase retrieval



➤ W. Hoppe,  
Acta Cryst. A 25, 508  
(1969).

➤ R. Hegerl, W. Hoppe, Ber.  
Bunsen-Ges. Phys. Chemie  
74, 1148 (1970).



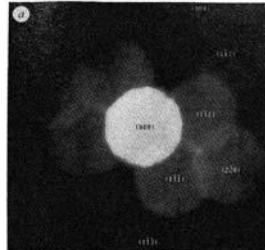
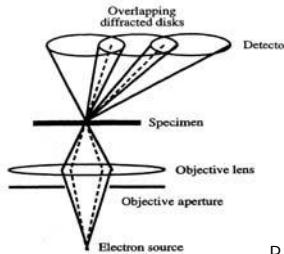
## LETTERS TO NATURE

### Resolution beyond the 'information limit' in transmission electron microscopy

P. D. Nellist, B. C. McCallum  
& J. M. Rodenburg

Cavendish Laboratory, University of Cambridge, Madingley Road,  
Cambridge CB3 0HE, UK.

The conventional resolution of transmission electron microscopes is orders of magnitude larger than the wavelength of the electrons used. Aberrations of the objective lens corrupt spatial information on length scales below a limit known as the point resolution. Methods to correct for aberrations do not fully account for the phase of the waves which make up the image (this constitutes the 'phase problem'). Beyond the point resolution, information can still be transferred by the microscope, but spatial coherence of the waves is needed to make an accurate image (this is usually on the resolution of the transferred image information). Here we show that this limit can be突破 to obtain images of soft matter.



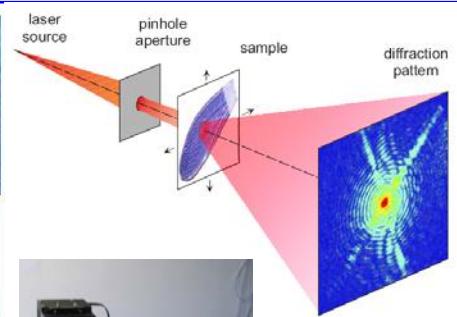
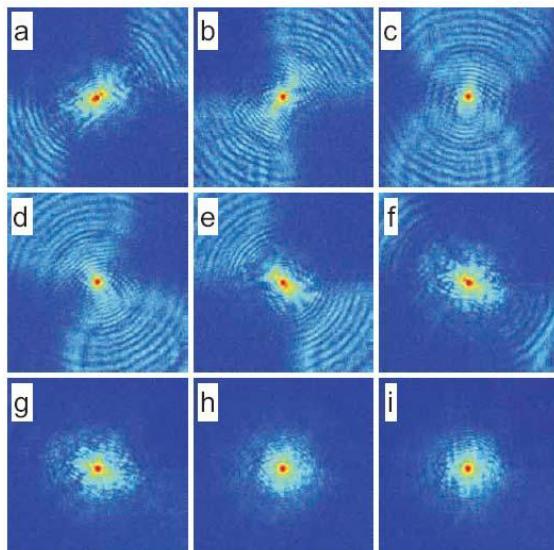
P.D. Nellist et al., Nature 374, 630 (1995)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



## A test case: far-field phase retrieval with laser light



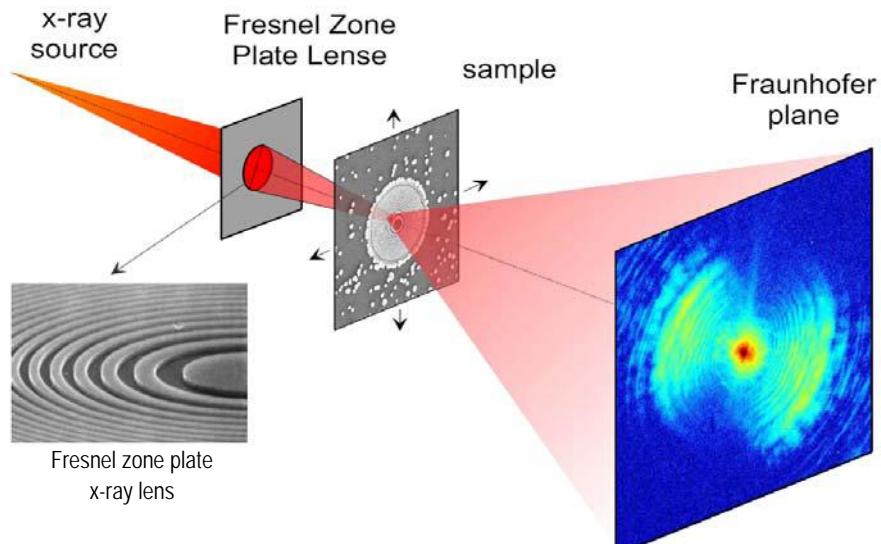
M. Dierolf et al., Europhysics News 39, 22 (2008)



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## 'Super-Resolution' Scanning X-Ray Transmission Microscopy



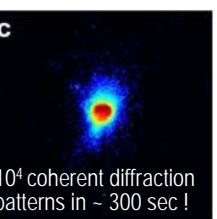
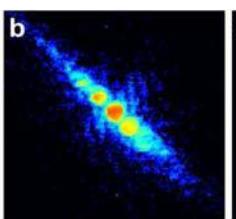
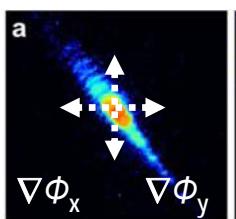
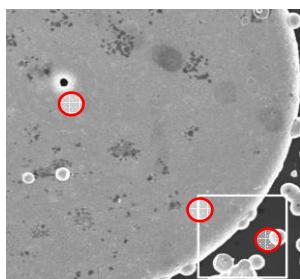
Experiment at cSAXS beamline, Swiss Light Source, energy 6.8 keV



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>

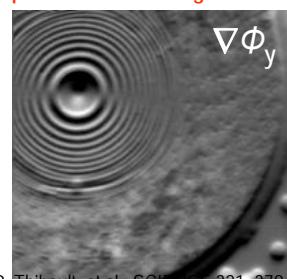
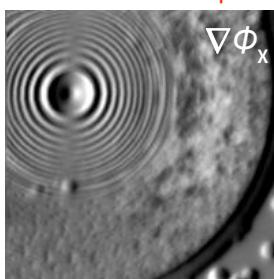
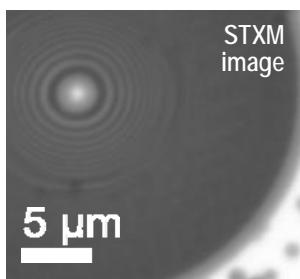


## 'Super-Resolution' Scanning X-Ray Transmission Microscopy



$10^4$  coherent diffraction patterns in ~ 300 sec !

'conventional' STXM analysis of  $> 10^4$  diffraction patterns yields  
'low-resolution' absorption & phase-contrast images



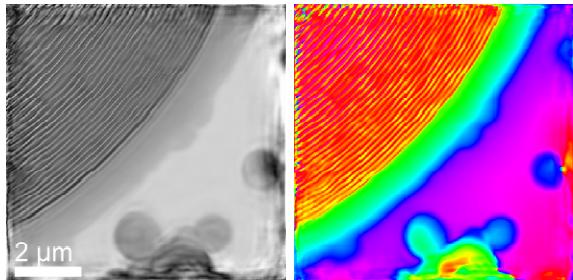
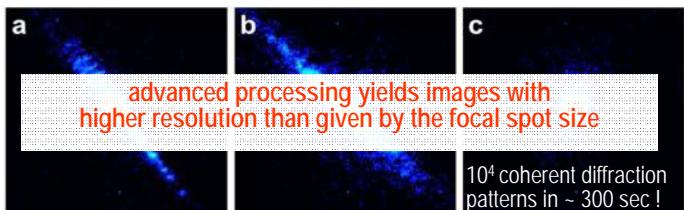
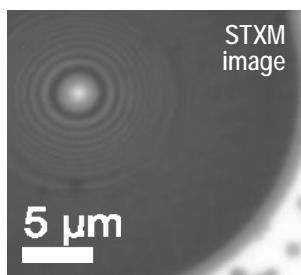
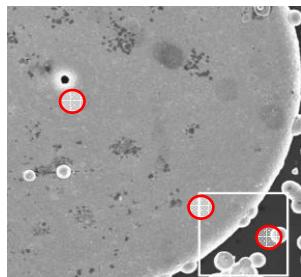
P. Thibault, et al., SCIENCE 321, 379-382 (2008)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# 'Super-Resolution' Scanning X-Ray Transmission Microscopy



P. Thibault, et al., SCIENCE 321, 379-382 (2008)

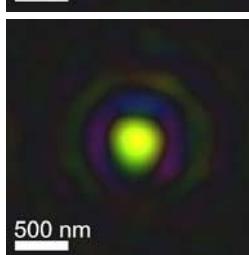
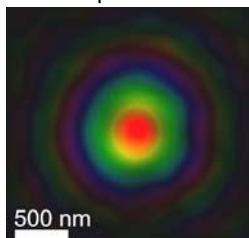


Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



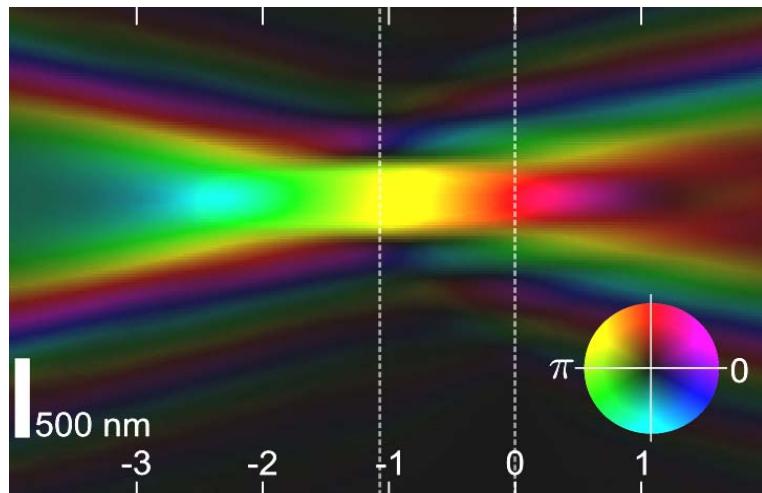
## Simultaneous reconstruction of probe & specimen

probe



in focus

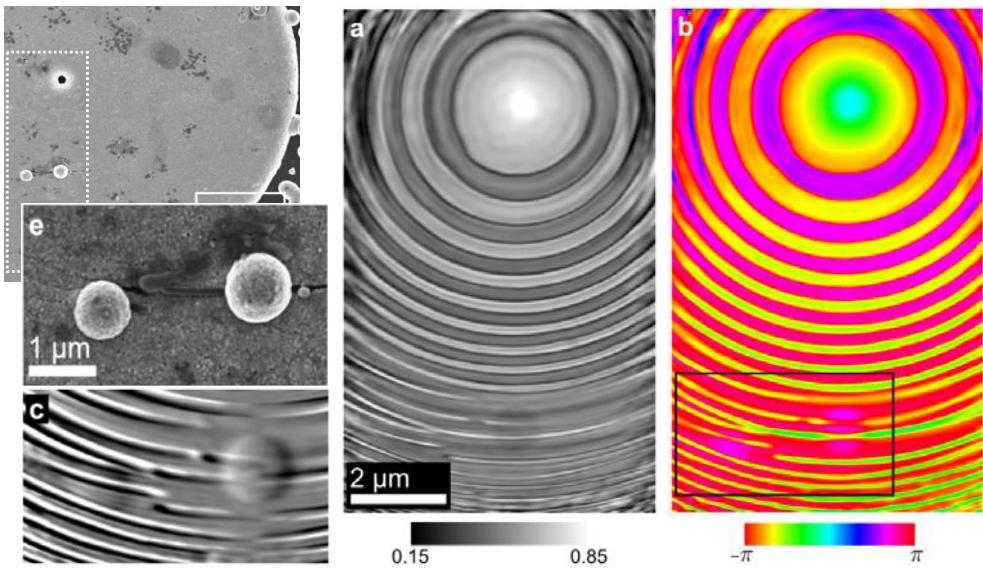
P. Thibault, et al., SCIENCE 321, 379-382 (2008)



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



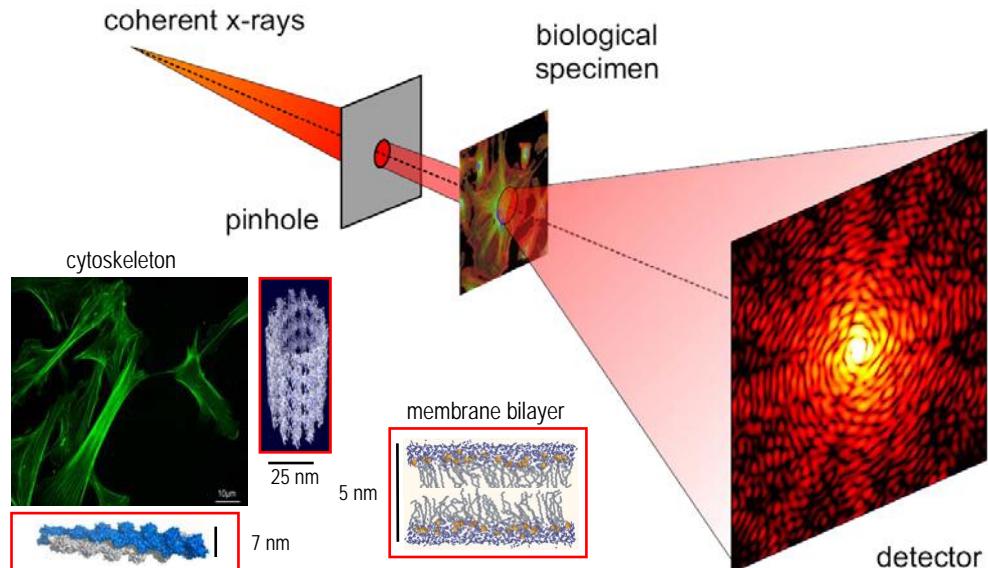
# 'Super-Resolution' X-Ray Microscopy



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



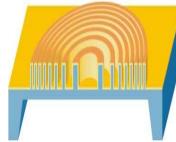
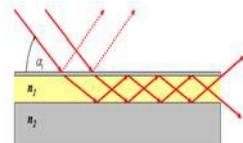
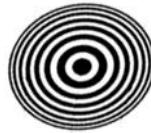
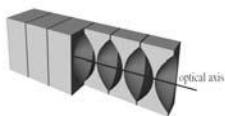
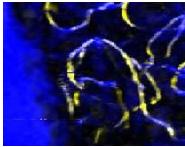
## Near future: High-resolution x-ray imaging of cells ?



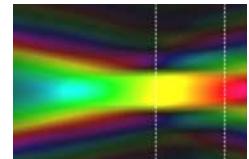
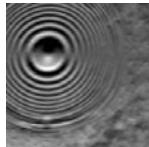
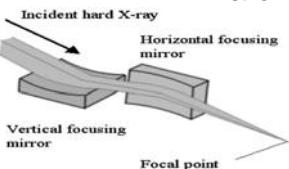
Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



# Summary



1. X-ray focusing – Why
2. Methods overview – focus on X-ray waveguides
3. Recent advances at Paul Scherrer Institut
4. 'Super-Resolution' coherent X-ray microscopy & characterization of focused wave-fields



Email: franz.pfeiffer@psi.ch - Web: <http://people.epfl.ch/franz.pfeiffer>



**SWISS LIGHT SOURCE** **SLS**

Coherent Imaging group  
at PSI & EPFL

Franz Pfeiffer      Oliver Bunk      Andreas Menzel      Xavier Donath      Pierre Thibault      Cameron Kewish      Martin Dierolf      Tobias Boehlen

Swiss Light Source

PAUL SCHERRER INSTITUT **PSI**

Christian David, Joan Vila, Konstantins Jefimovs, Vitaliy Guzenko, Harun Solak, Sankha Sarkar,  
Laboratory for Micro- and Nanotechnology,  
Paul Scherrer Institut, CH

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# X-ray focusing with Kirkpatrick-Baez optics

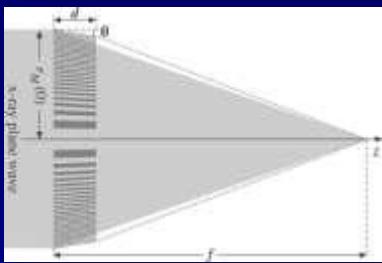
K. Yamauchi  
Osaka University

# Contents

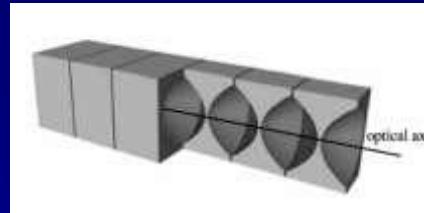
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1. Introduction
2. Accuracy criteria to realize 50nm-level focusing
3. Fabrication technology (@Osaka University)
4. Recent achievements
5. Challenges to realize sub-10nm focusing in hard X-rays
6. Other topics including XFEL optic
7. Summary

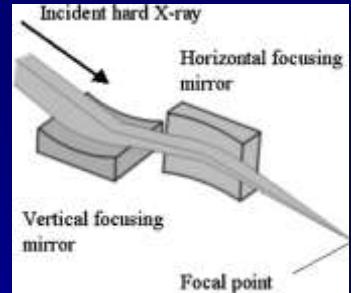
# Advantages of KB mirror optic



Fresnel zone plate



Refractive lens



K-B mirror optics

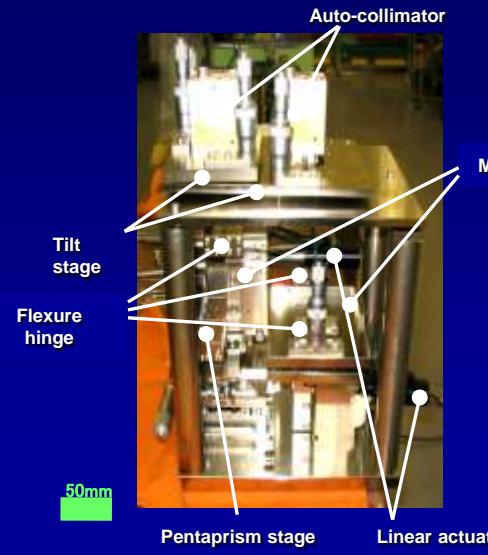
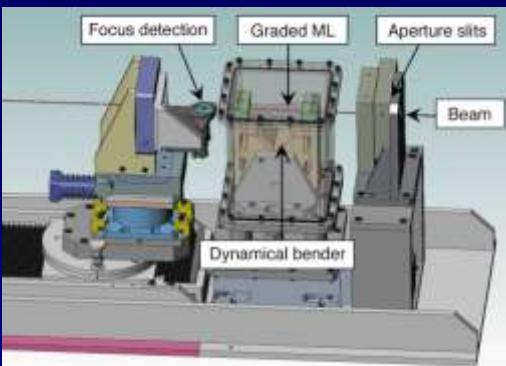
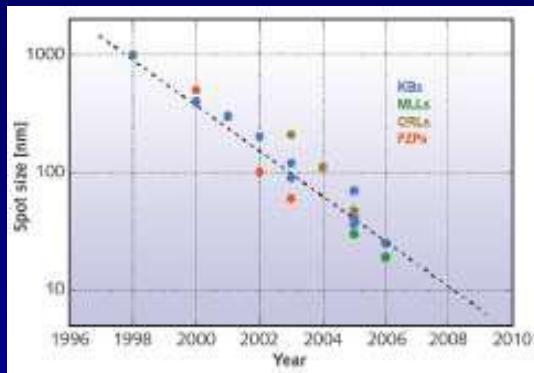
Achromatic optic (total reflection mirrors)

High efficiency >90%

Large aperture  $\approx 500\mu\text{m}$

Long working distance 10mm  $\sim$  500mm

# Recent achievement in 50nm-level focusing



90nm x 90nm, 45nm focusing were achieved at ESRF by a graded multilayer coating and a fine bending system

Efficient sub 100 nm focusing of hard x rays

O. Hignette, P. Cloetens, G. Rostaing, P. Bernard and C. Morawe  
Rev. Sci. Instrum. 76, 063709 (2005)

Ch. Morawe et al,  
Proc. SPIE 6317 (2006)

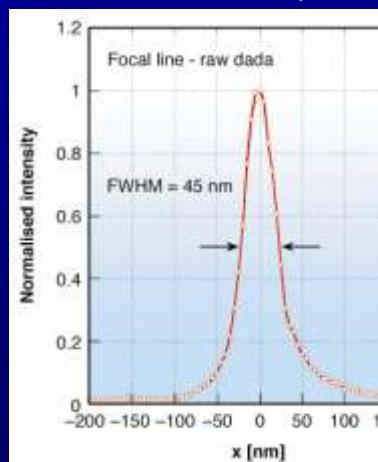
75nm x 85nm focusing was achieved at APS by a optical figuring and a differential deposition.

Short focal length Kirkpatrick-Baez mirrors for a hard x-ray nanoprobe  
W. Liu, G. Ice, J. Tischler, A. Khounsary, C. Liu, L. Assoufid  
and A. Macrander, Rev. Sci. Instrum. 76 (11), 2005, p.113701

36nm x 48nm, 25nm focusing were achieved by SPring-8 and Osaka Univ. group by EEM, P-CVM, MSI and RADSI.

H. Mimura et al., Hard X-ray Diffraction-Limited Nanofocusing with Kirkpatrick-Baez Mirrors, Japanese Journal of Applied Physics Part 2, 44 (18), L539-L542 (2005).

H. Mimura et al., Efficient focusing of hard x rays to 25 nm by a total reflection mirror, Applied Physics Letters 89, 051903 (2006).

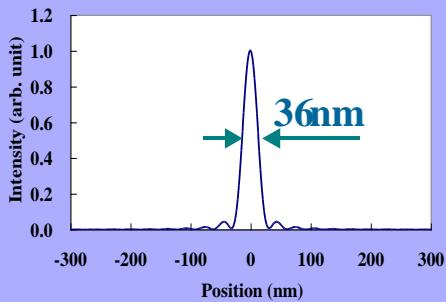
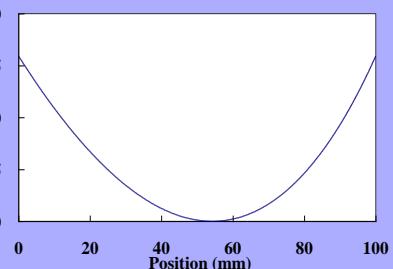
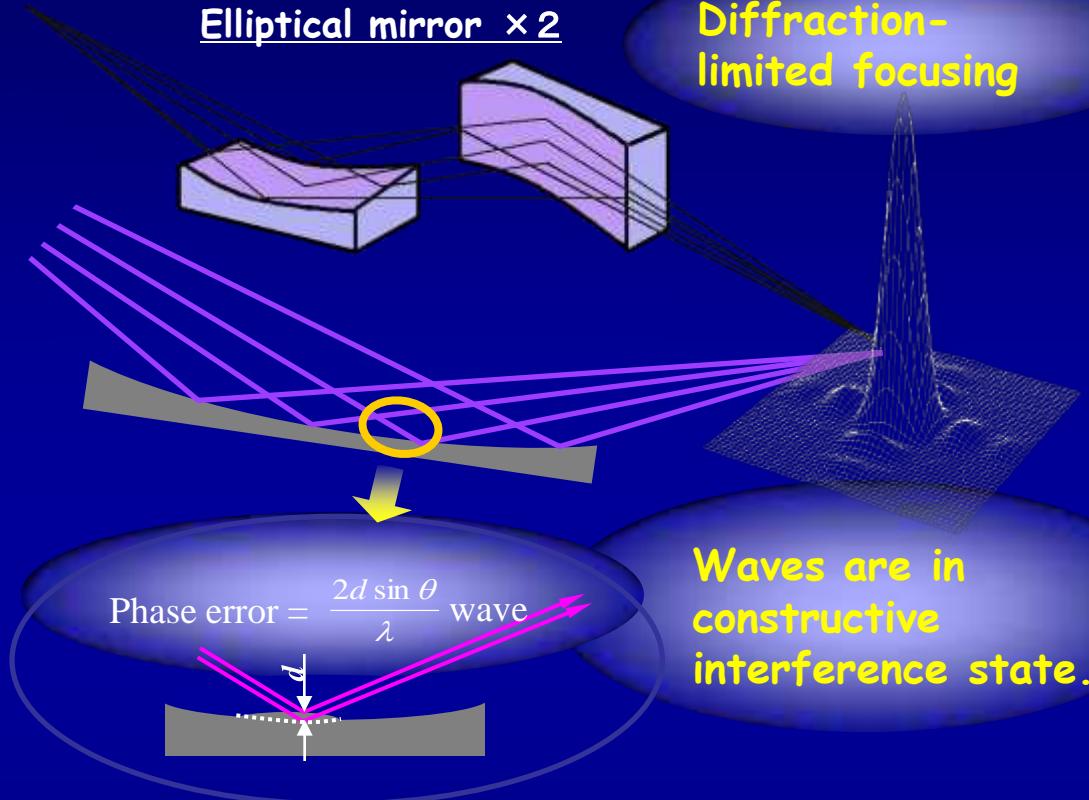


# Required accuracy for nano-focusing under D-limited condition

## Kirkpatrick-Baez mirrors

Elliptical mirror × 2

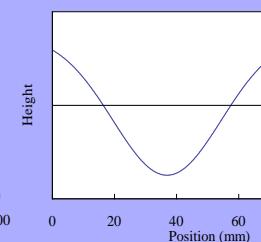
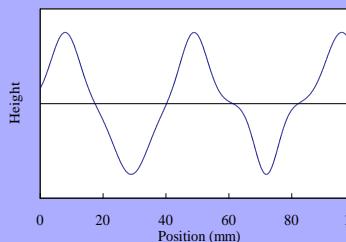
Diffraction-limited focusing



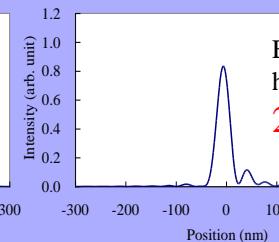
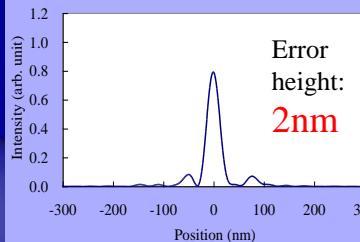
Designed profile (ellipse)

Beam profile

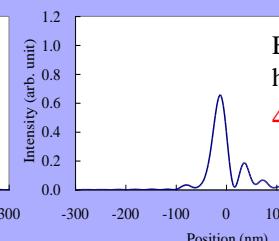
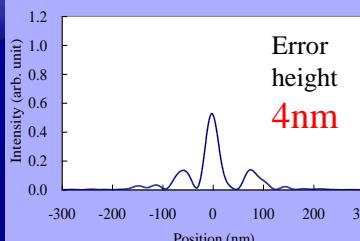
40mm < Ls < 50mm



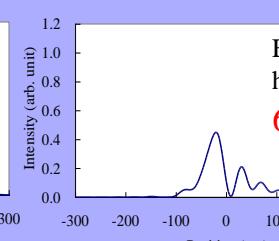
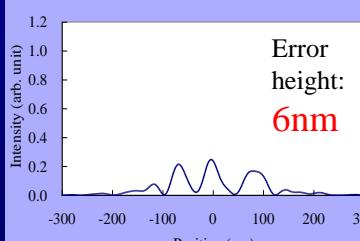
Error height:  
2nm



Error height:  
4nm



Error height:  
6nm



# Fabrication and figure testing technologies of Osaka University

## ◎ Plasma CVM (chemical vaporization machining)

→ Rough figuring (Rapid figuring with sub-10nm (P-V) accuracy)  
K. Yamamura et al., Rev. Sci. Instrum. 71 (2000), 4627

## ◎ EEM (elastic emission machining)

→ Final figuring and smoothing (Fine figuring and atomic smoothness)  
K. Yamauchi et al., Rev. Sci. Instrum. 73 (2002), 4028

## ◎ MSI (microstitching interferometry)

→ Figure tester with spatial resolution close to  $1\mu\text{m}$   
K. Yamauchi et al., Rev. Sci. Instrum. 74 (2003), 2894

## ◎ RADSI (relative-angle determinable stitching interferometry)

→ Figure tester for steeply curved ellipse of large NA mirror  
H. Mimura et al., Rev. Sci. Instrum. 76 (2005), 045102

J-tec URL <http://www.j-tec.co.jp>

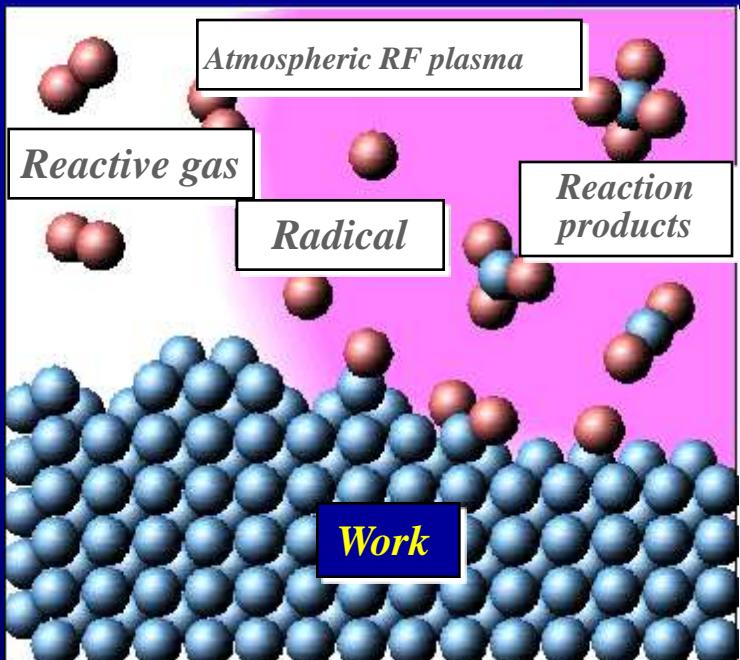
Sub-100nm focusing mirrors have already been commercially available

# Plasma CVM (Chemical Vaporization Machining)

*A chemical removal process utilizing reactive species generated in the atmospheric pressure plasma*



- **High density reactive species  $\Rightarrow$  High removal rate**
- **Chemical reaction  $\Rightarrow$  No damage on the surface**
- **Non contact  $\Rightarrow$  Insensitive against external disturbance**



Material	Removal rate ( $\mu\text{m}/\text{min}$ )
Fused silica	170
Silicon	94
Molybdenum	36
Tungsten	32
Silicon carbide	6.4
Diamond	2.5

# Plasma CVM (continued)

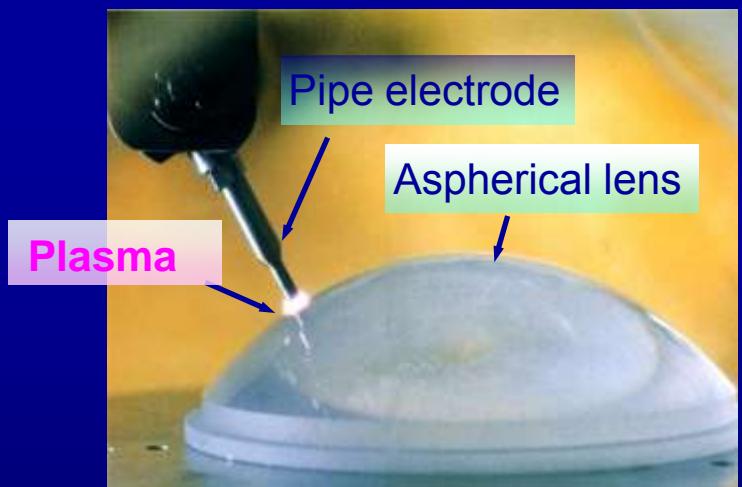
## Atmospheric pressure plasma



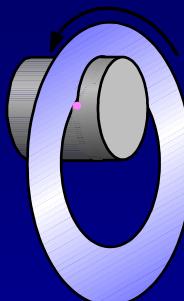
Plasma is localized around the electrode



***High spatial resolution figuring  
is possible without mask***

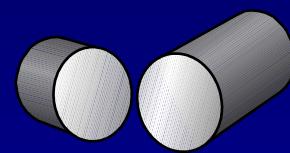


Pipe electrode is utilized for high-spatial resolution figuring

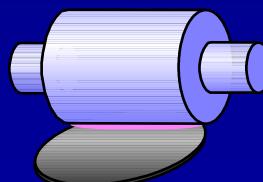


Slicing

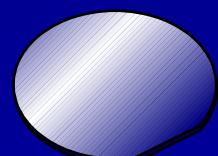
Inner diameter blade type



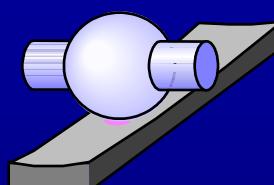
Si, in  
ot  
SiC



Cylindrical type Planarization

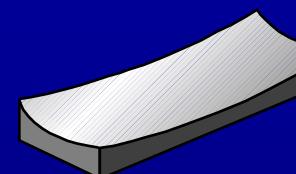


Si wafer  
SOI  
wafer



Spherical type

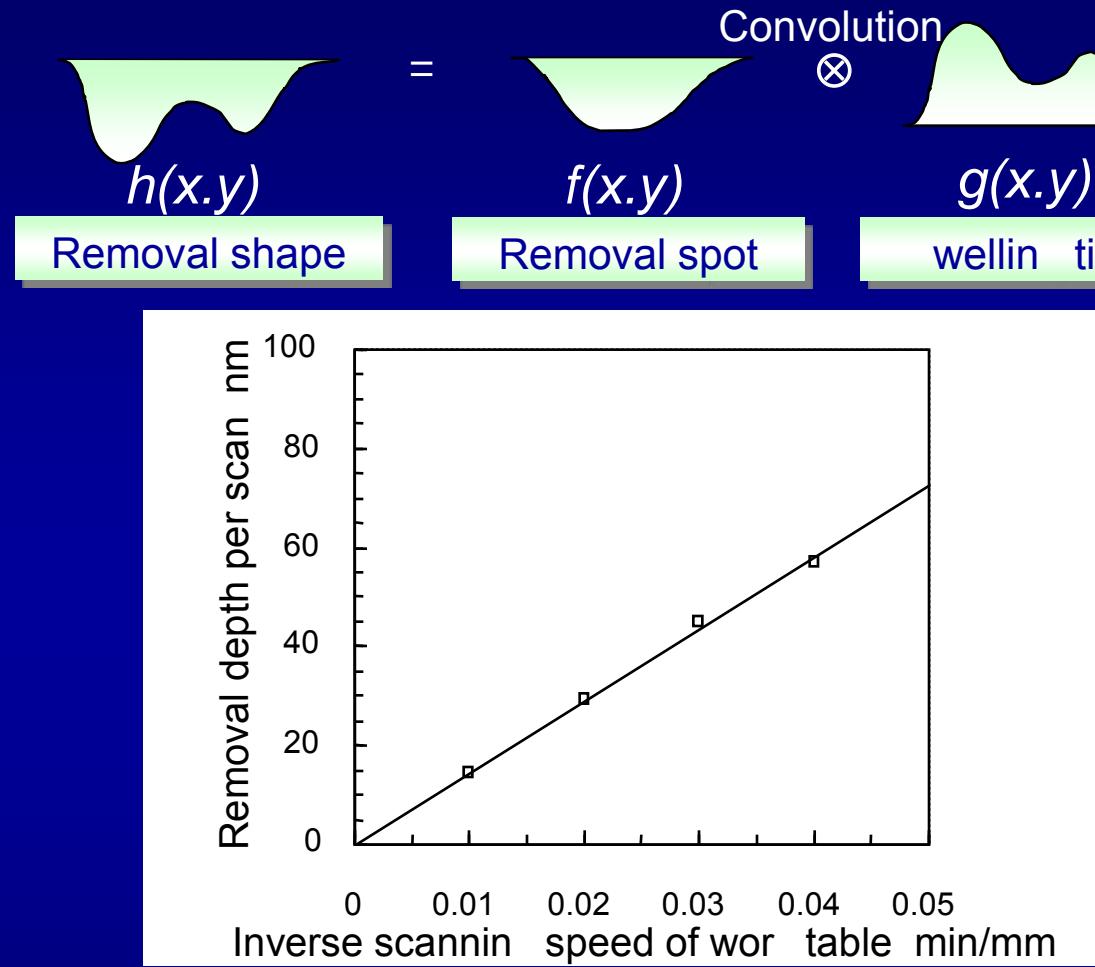
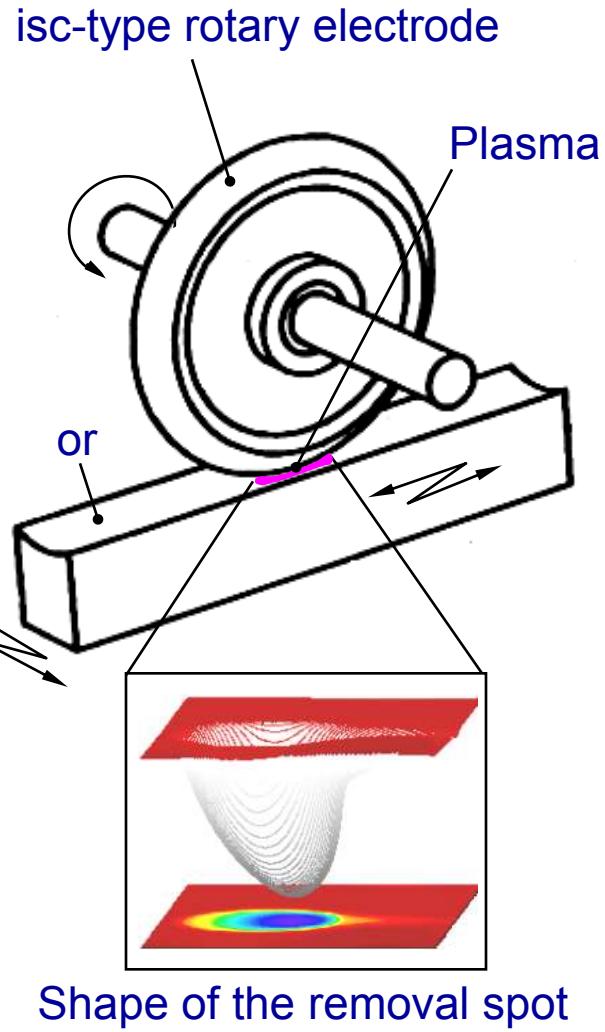
Figuring



X-ray mirror  
Aspherical  
SOI wafer

Rotary electrode is utilized for high-efficiency machining

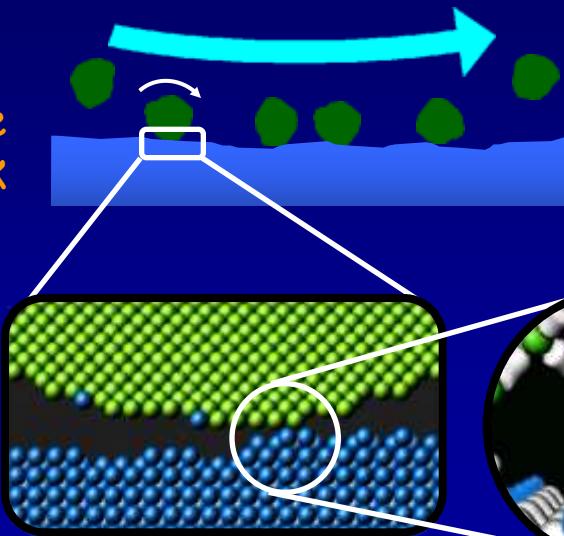
# Figuring by Numerically Controlled Plasma CVM



*Removal depth is proportional to dwell time so that figuring is controlled by scanning speed.*

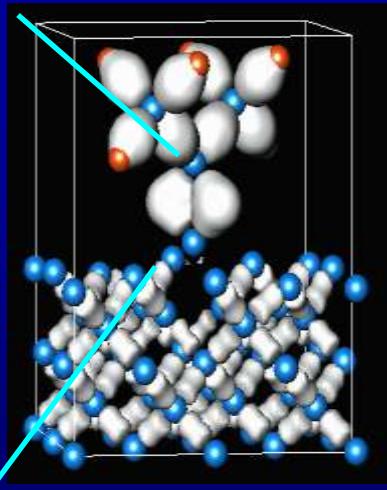
# EEM (Elastic Emission Machining)

The ultra-fine particle is supplied to the work surface by ultrapure water flow



In EEM, chemical reaction between sol surfaces is utilized.

$\text{SiO}_2$  powder particle



$\text{Si}(001)$  surface

Atom removal occurs selectively at the top site of the work surface

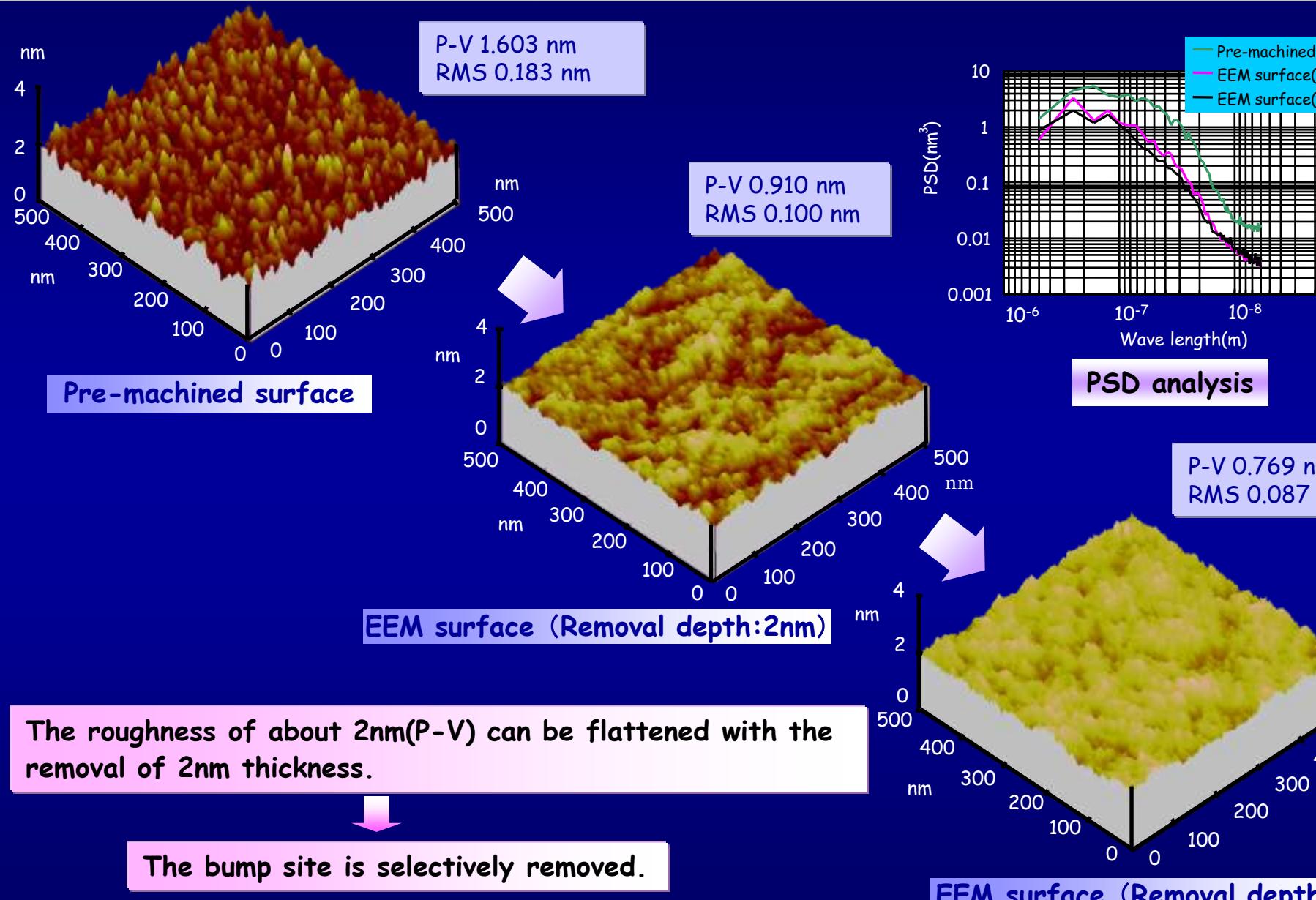
Bump site is preferentially removed



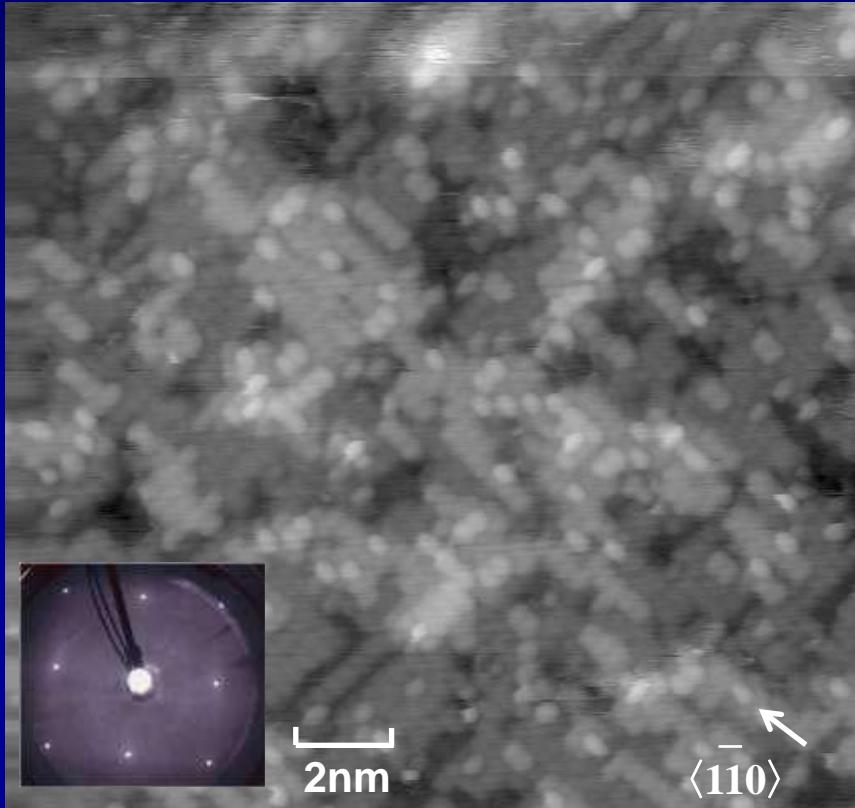
Atomically flat surface can be obtained

Removal mechanism is verified to be chemical by first-principles molecular dynamics simulation

# Surfaces smoothing properties in EEM



# STM image of EEM processed surface



95% of the EEM processed surface is constructed with only 3 atomic layers.

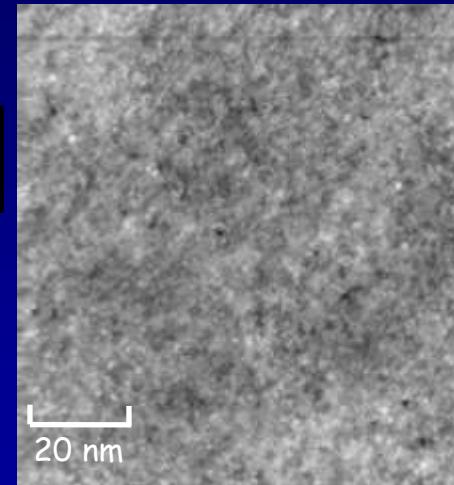
K. Arima et al,

Science 31, 11–20 (2001) DOI 10.1126/science.1025410 (2001)

Distribution of atom classified for every atomic layer



1st layer (0.034%)

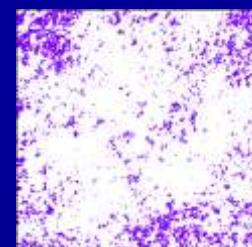


20 nm

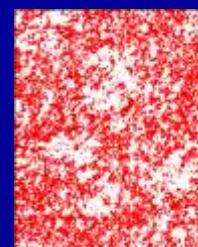
STM image (100nm × 100nm)



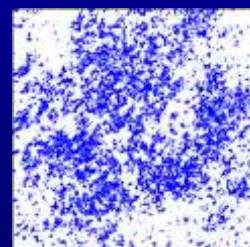
2nd layer (1.4%)



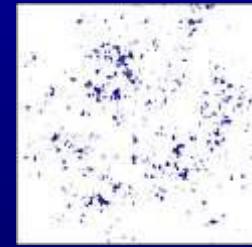
3rd layer (16.0%)



4th layer (47.0%)



5th layer (30.7%)

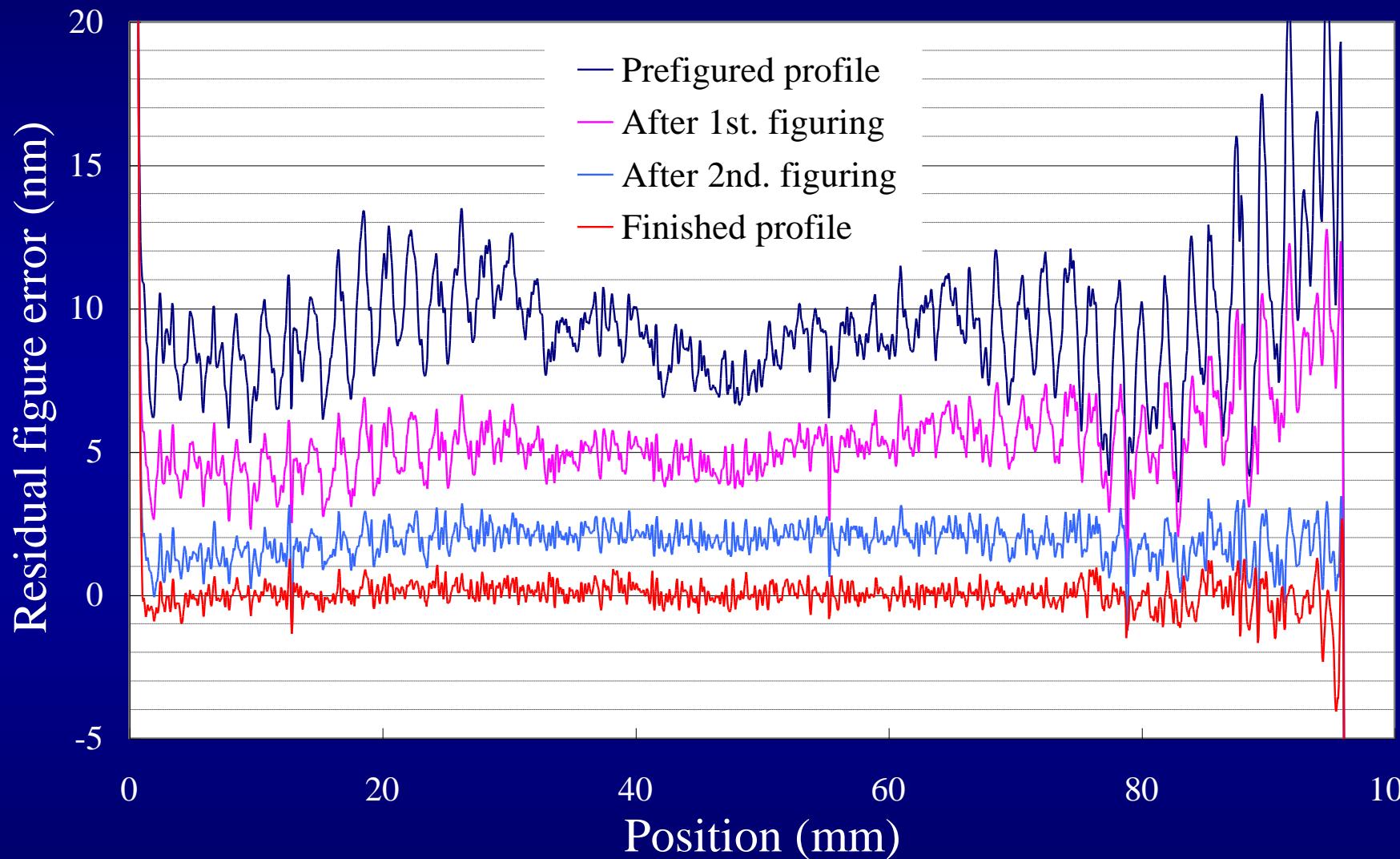


6th layer (4.0%)

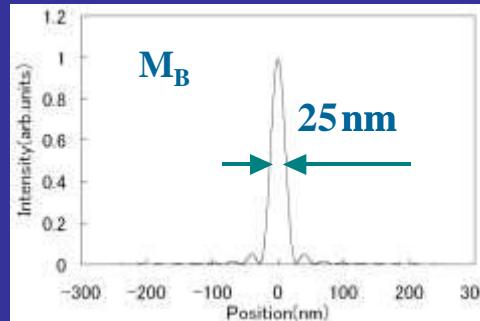
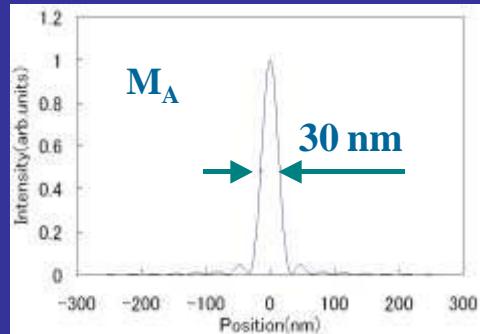


Others (0.1%)

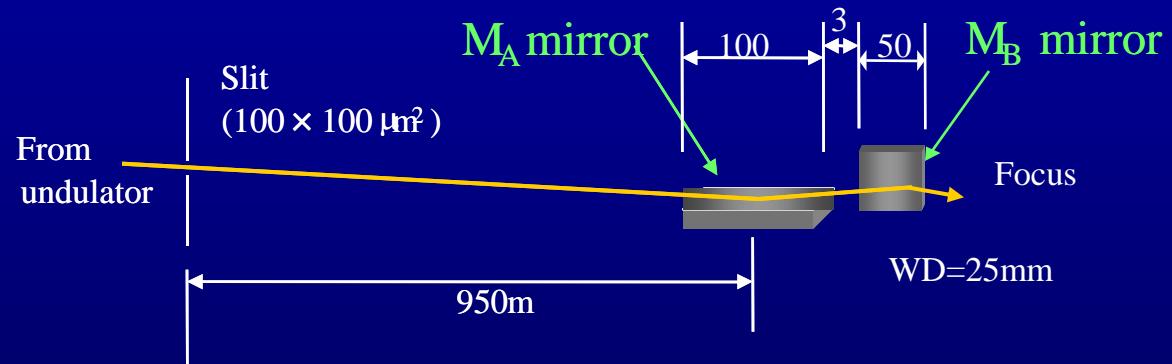
# Typical figuring properties using EEM



# Sub-30nm focusing

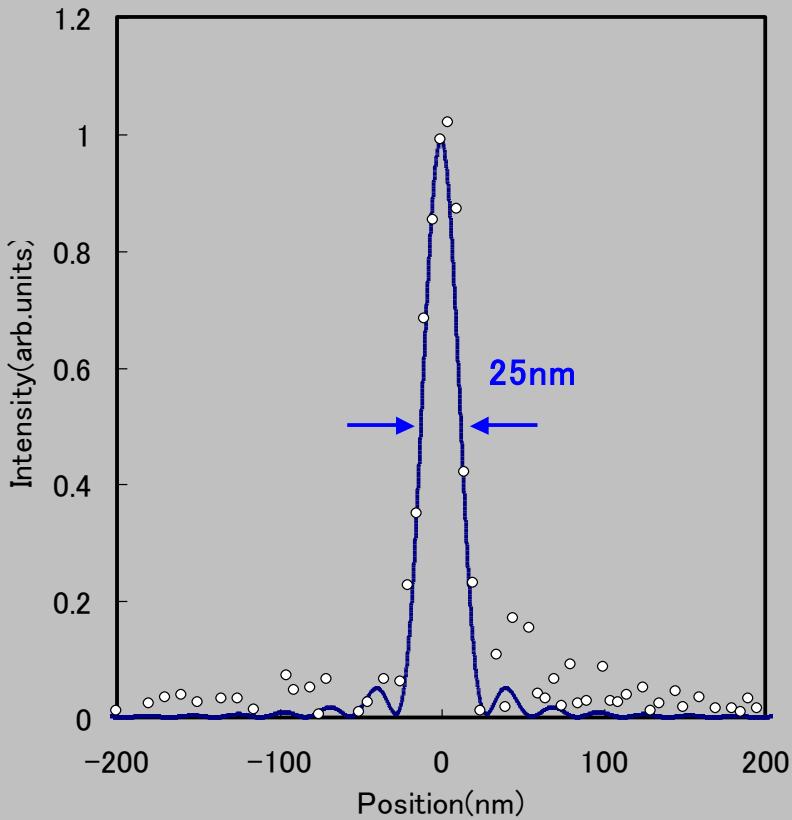
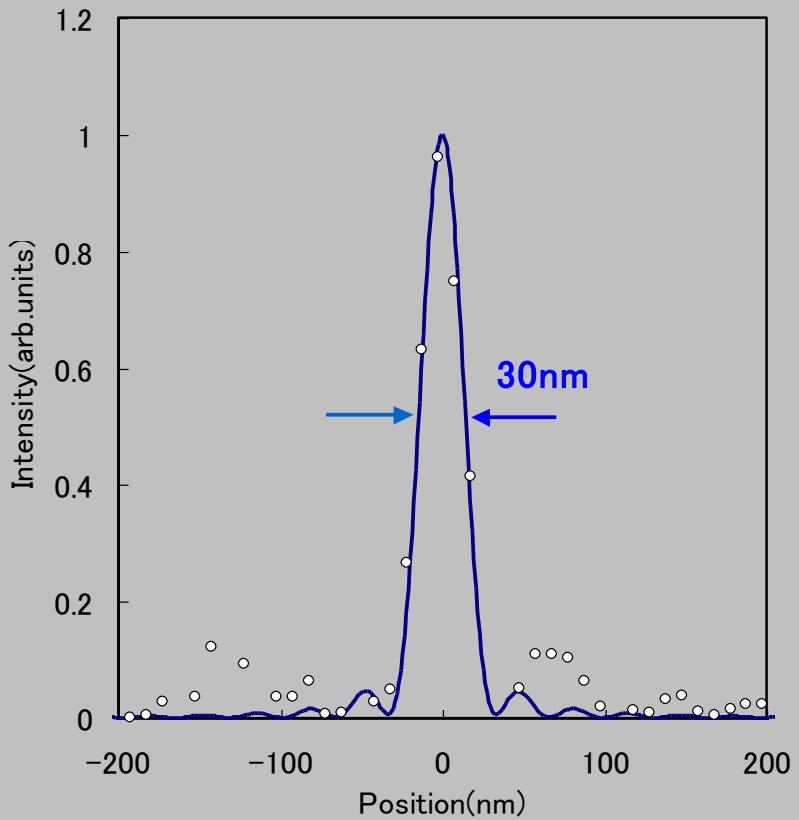


## Designed configuration



< Wave-optically expected beam profile >

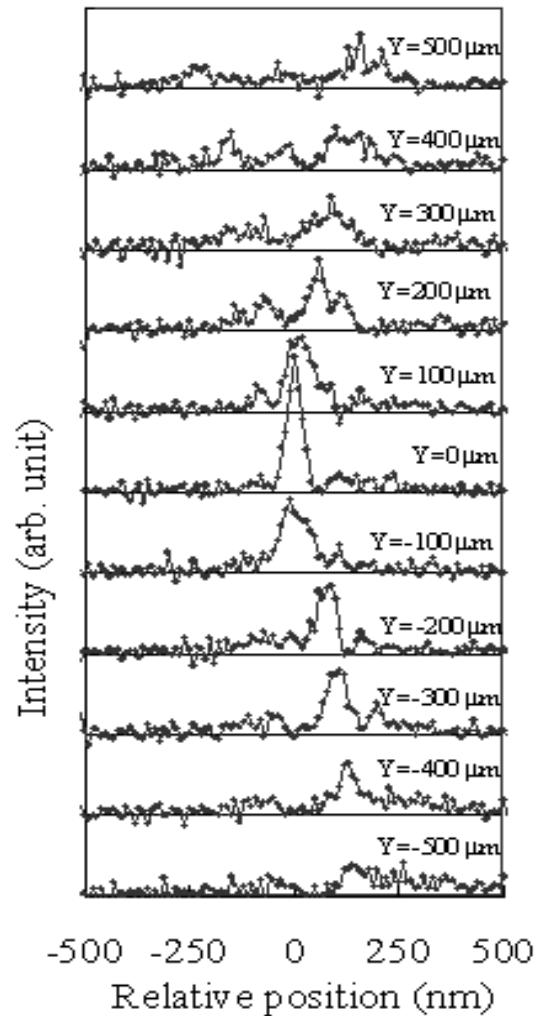
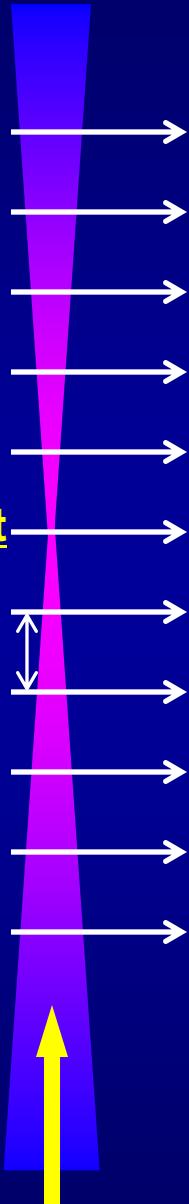
# Focusing performance



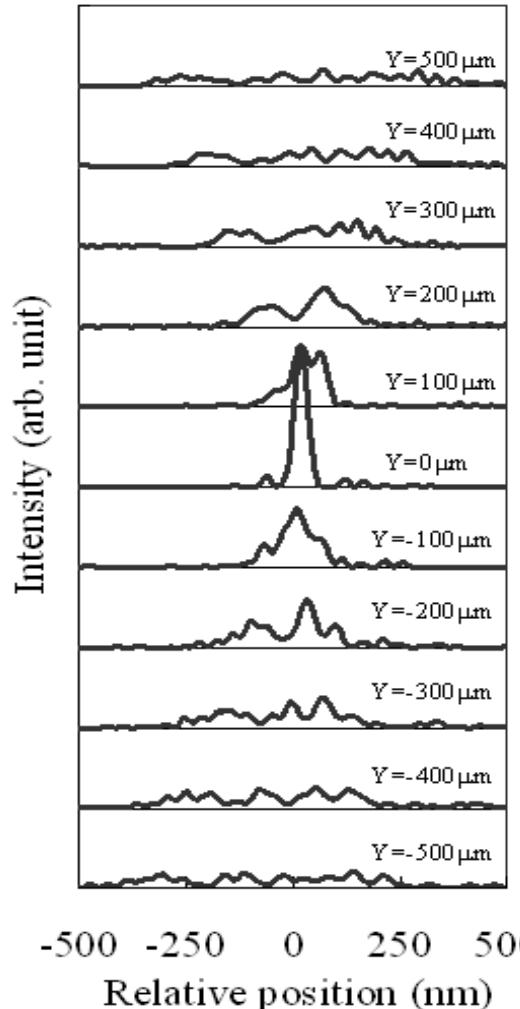
# Beam waist structures

Focal point

100 $\mu\text{m}$

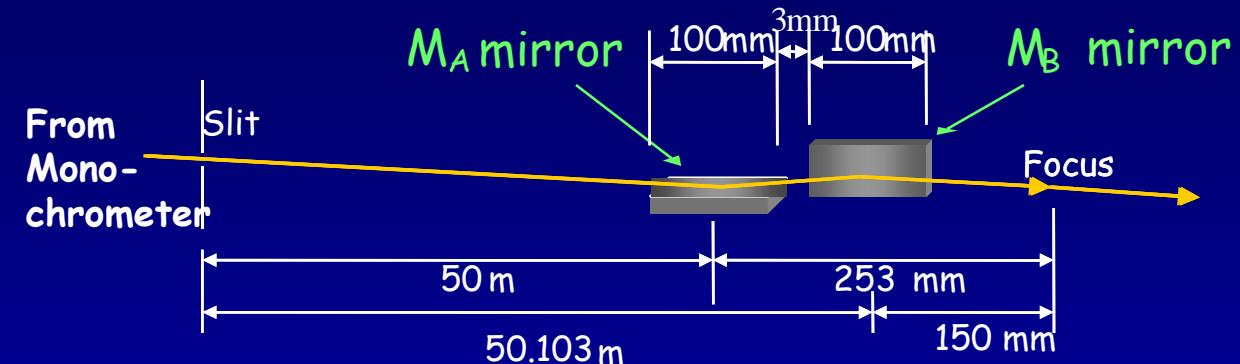


Measured profile



Calculated profile  
using measured shape

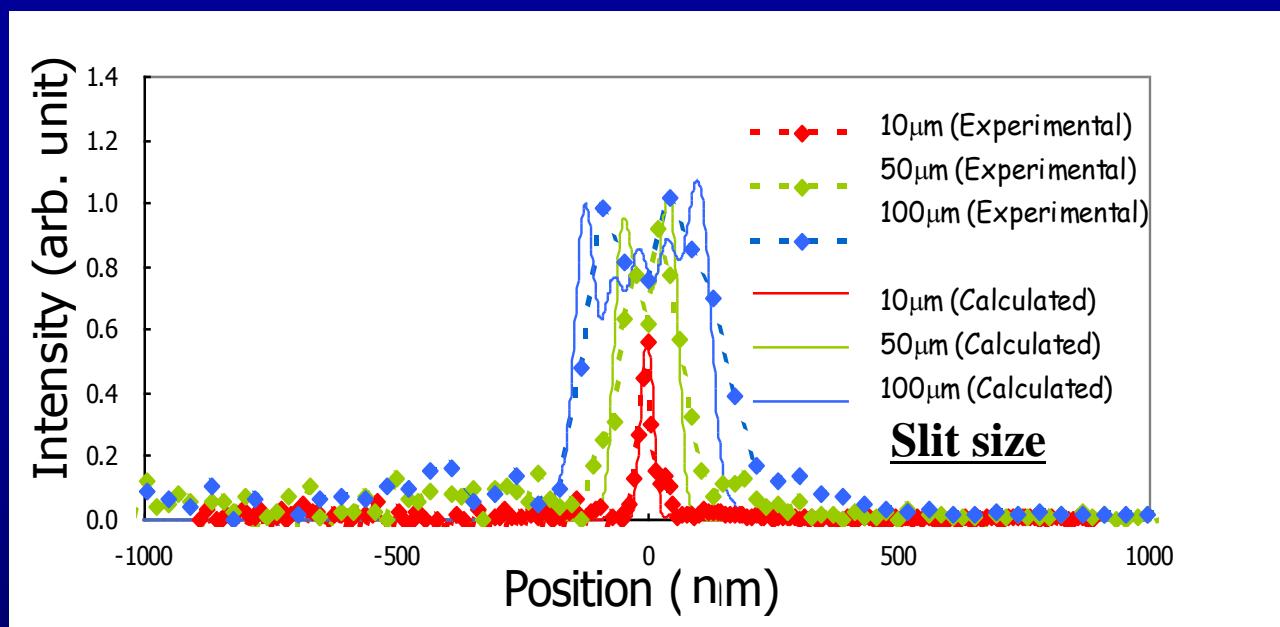
# Tunability of beam size and photon flux



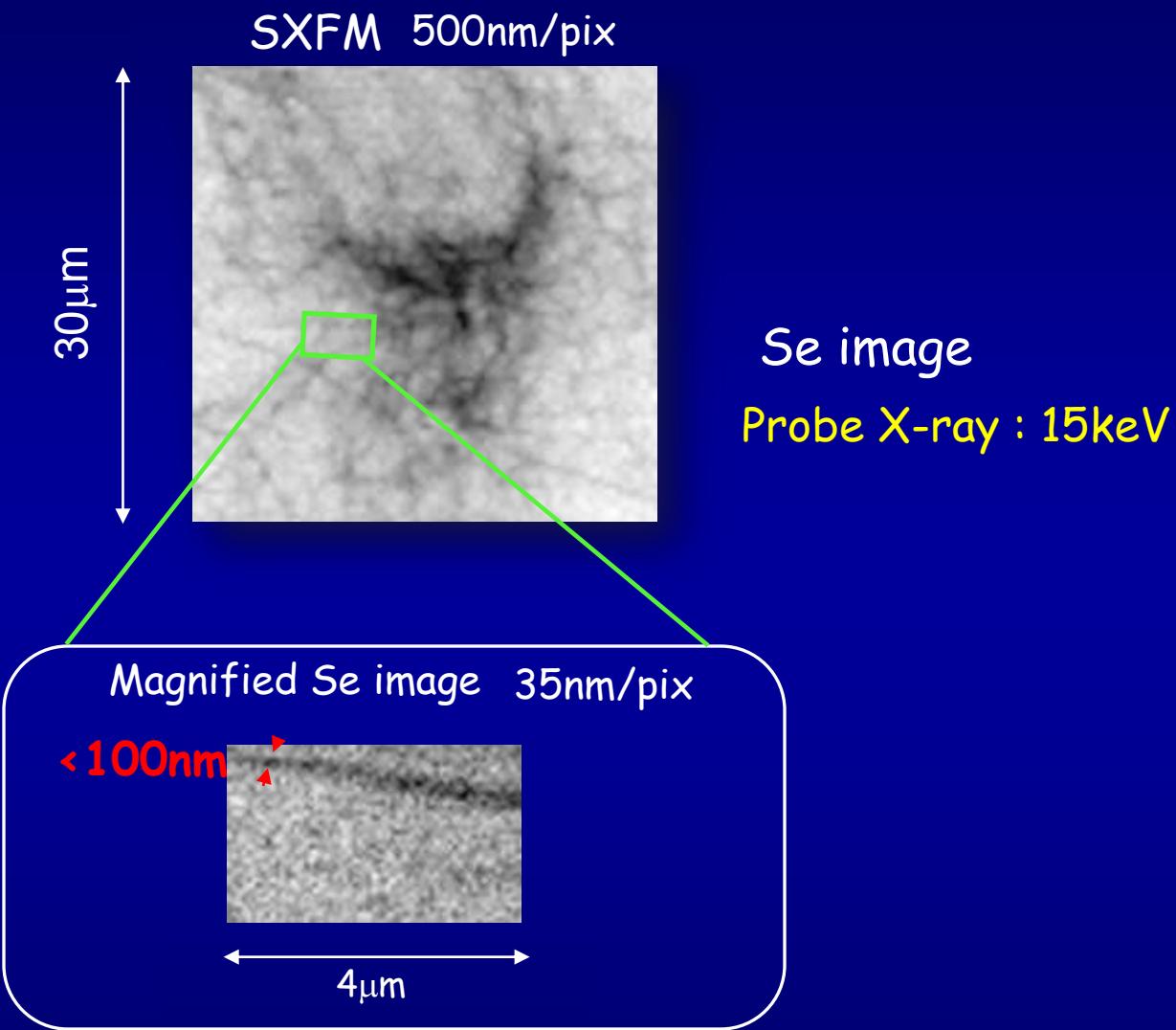
Photon flux:

$$5 \times 10^9 \sim 10^{12} \text{ (1/s)}$$

Installed in a new hutch of BL29



# Demonstration of oomin performance

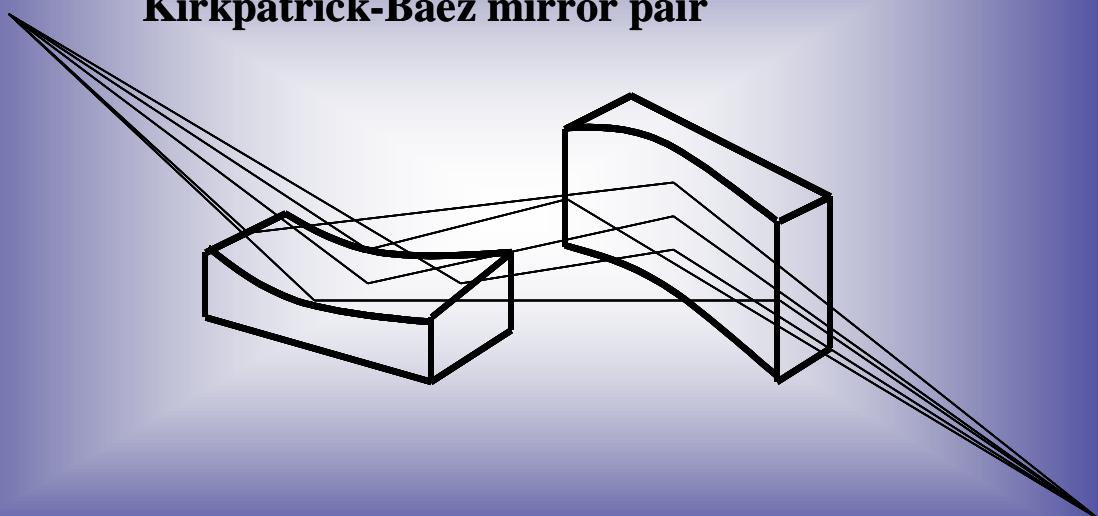


Mouse cell tubulin was stained with nanocrystals of CdSe/ZnS.

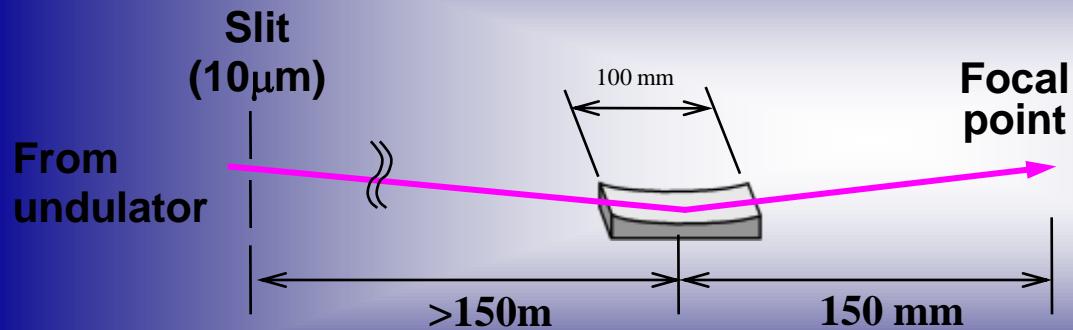
# “Hard-X-ray sub-10nm focusing

## By KB mirrors”

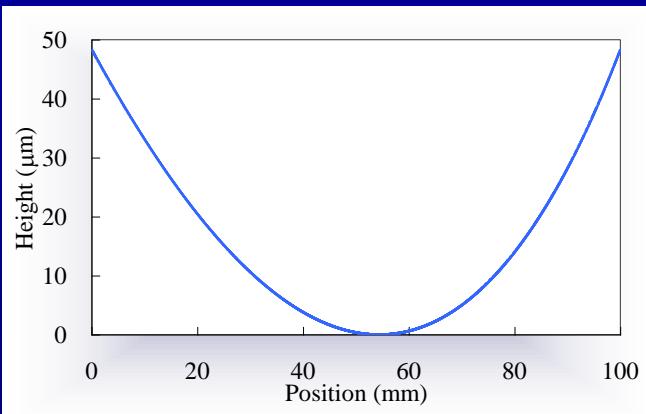
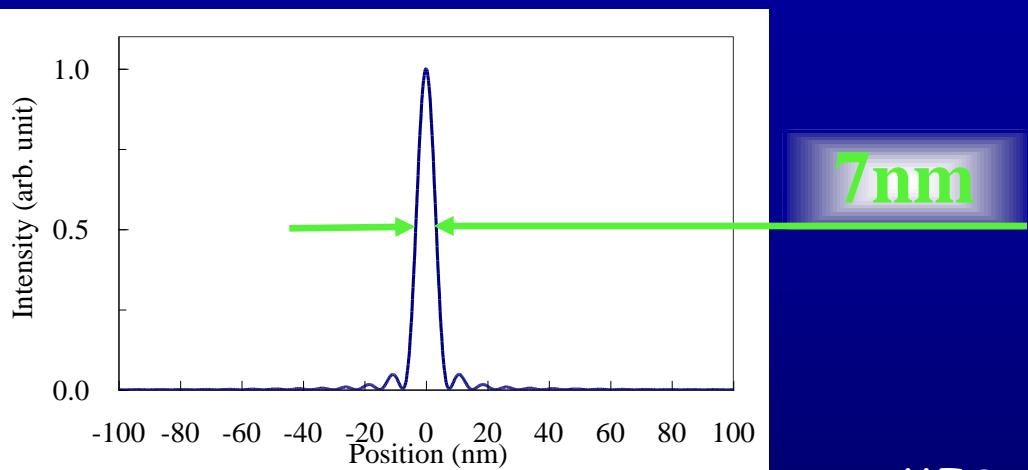
Kirkpatrick-Baez mirror pair



# To realize Sub-10nm focusing K-B mirrors



**X-ray energy : 20keV**  
**Focal length : 150mm**  
**Acceptance width : 1.1mm**  
**Incidence angle : 11.1mrad**



MIS with RADSI and EEM can prepare  
surface figure within 1~2nm (P-V) error

# Required accuracy

@20keV Mirror length: 100mm, Focal length: 150mm

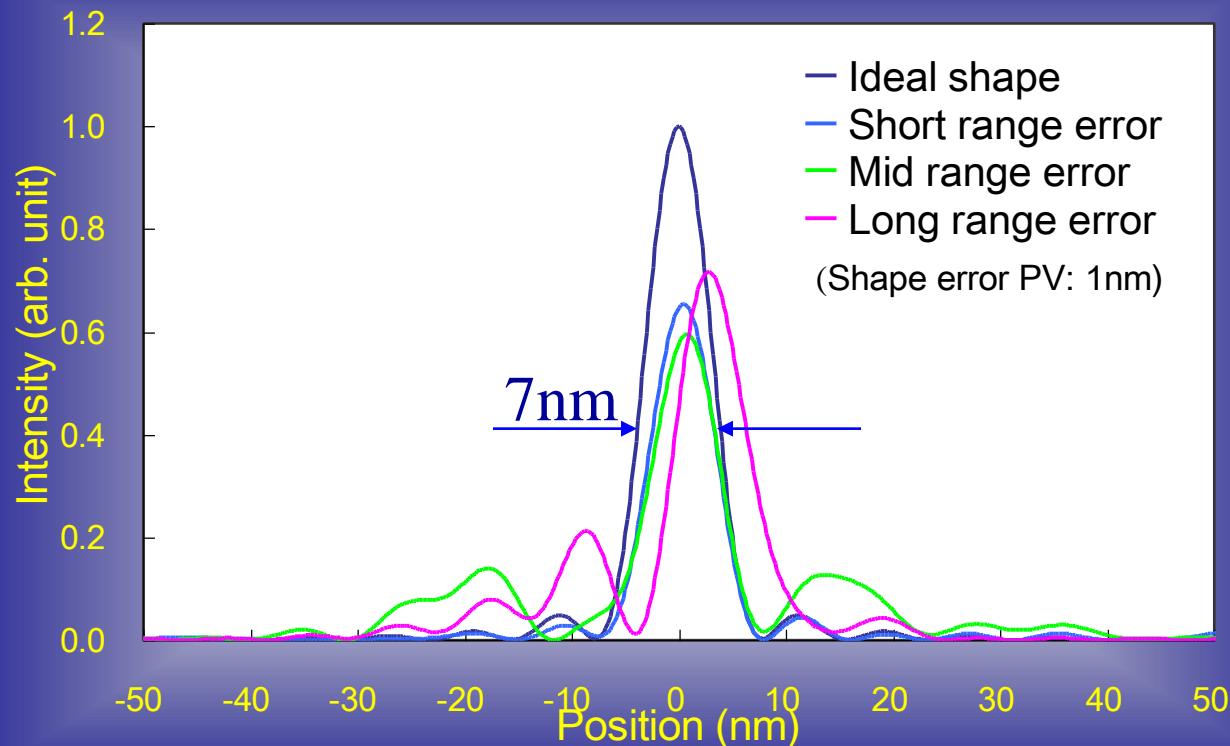
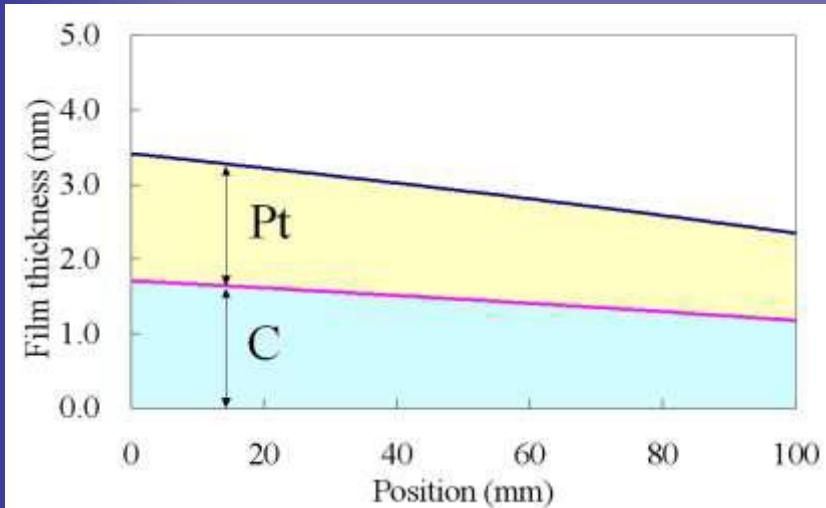


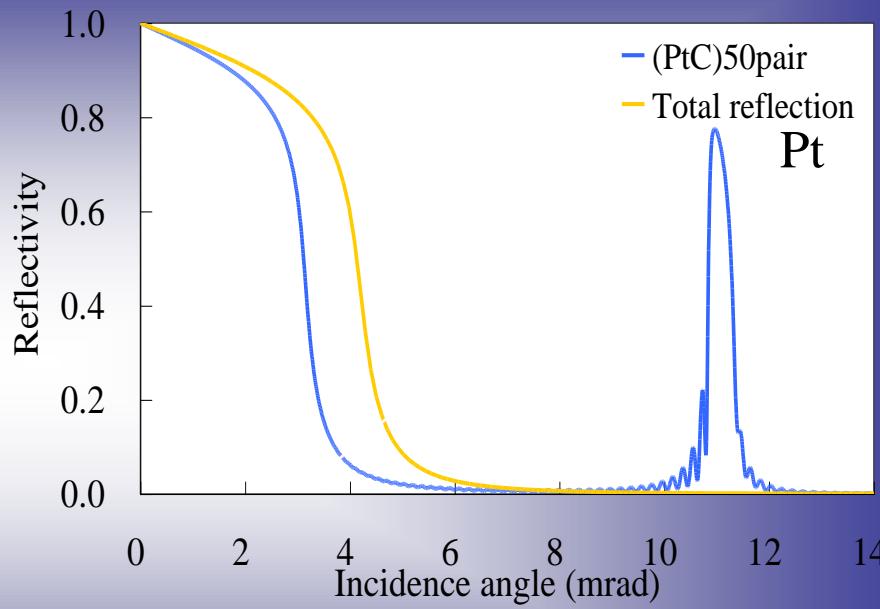
Figure error of 1nm is not allowable in this case

Off-line figure testing might be impossible?

# Multi-layer technology is needed to realize large NA



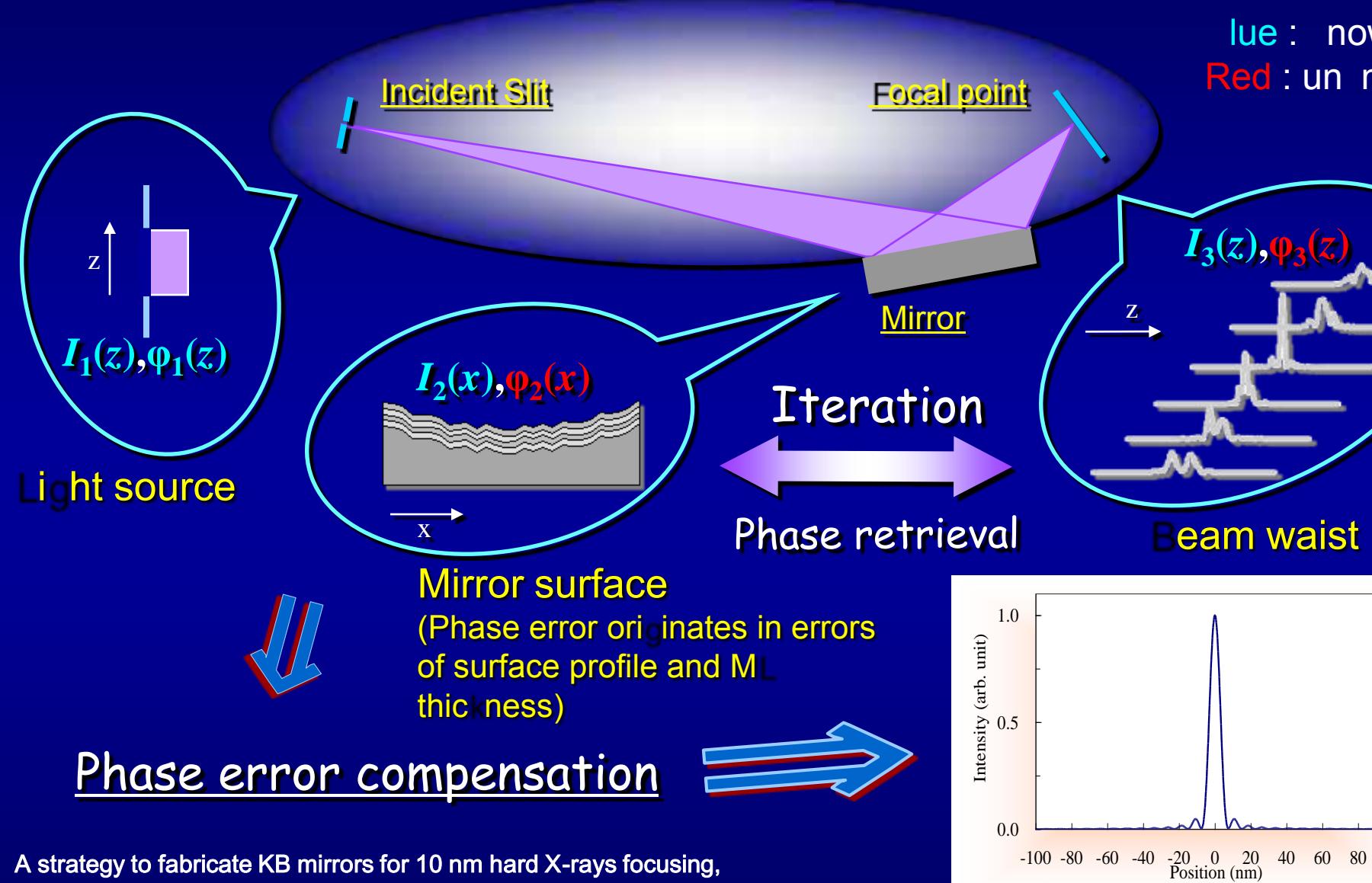
**Graded multi-layer**



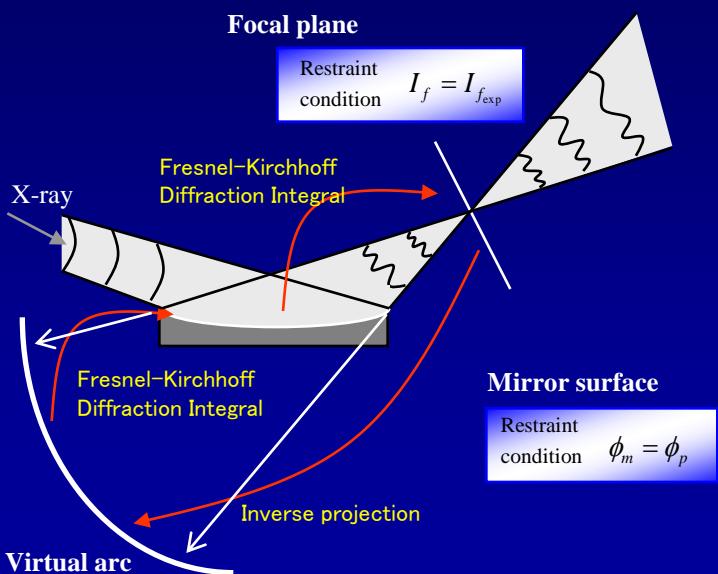
**Reflectivity**

Not only figure error but also thickness deviation of the multilayer induce the wavefront phase error.

# At-wavelength phase-retrieval interferometry



# Phase retrieval properties



## On focal plane

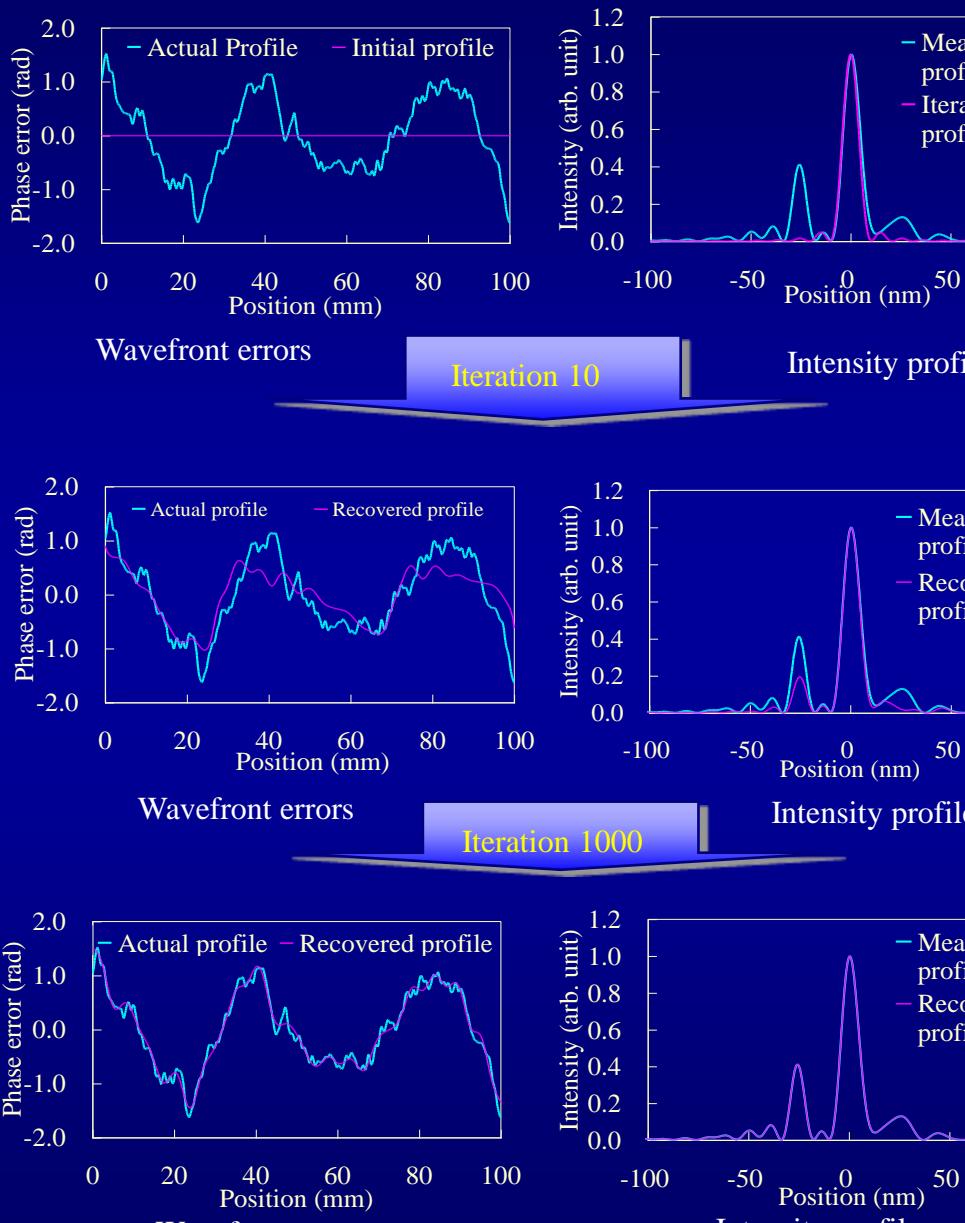
Intensity is changed to experimental value.

Phase is kept to be recovered value.

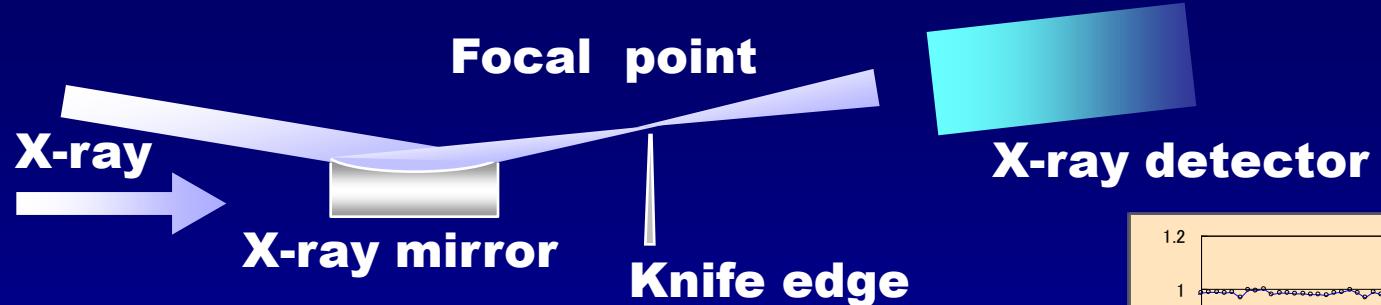
## On mirror surface

Intensity is changed to theoretical value.

Phase is kept to be recovered value.

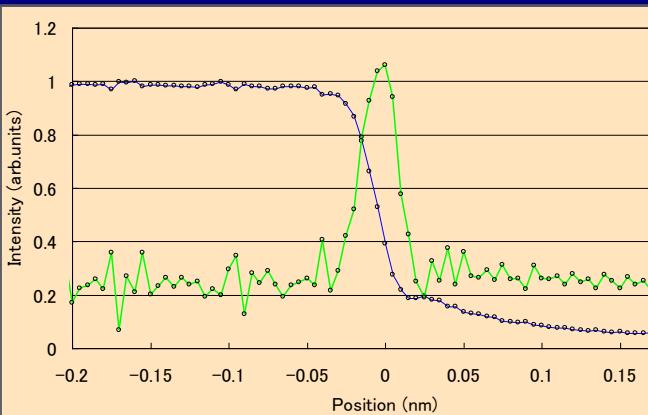
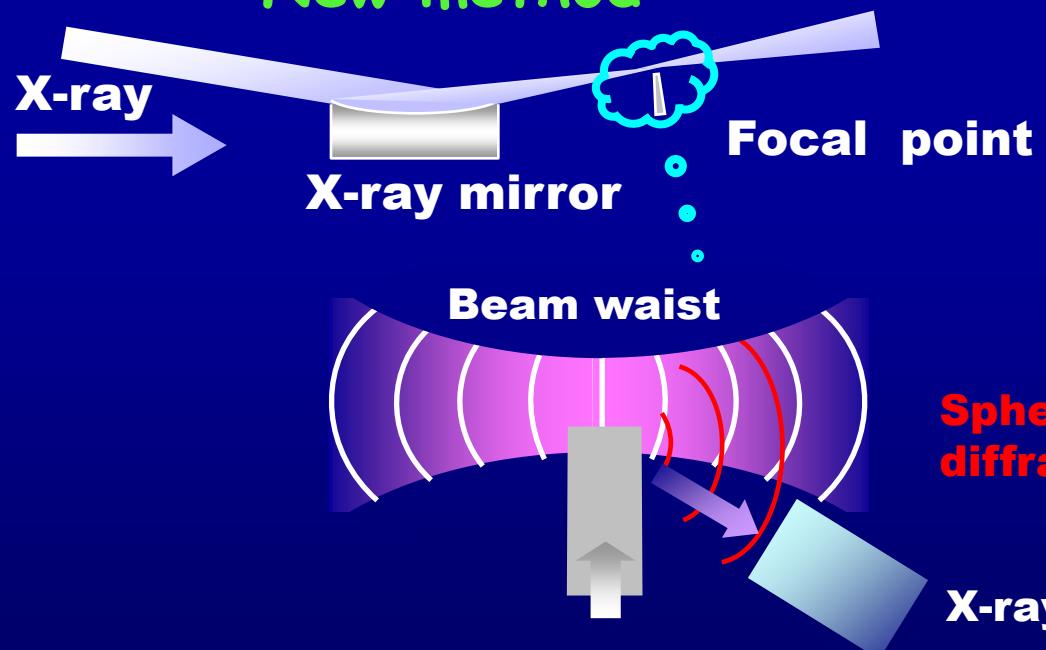


# New knife-edge method



Conventional knife-edge method

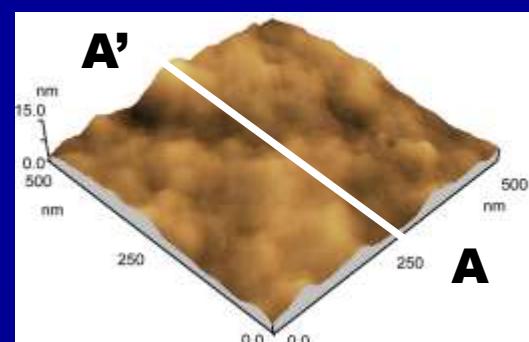
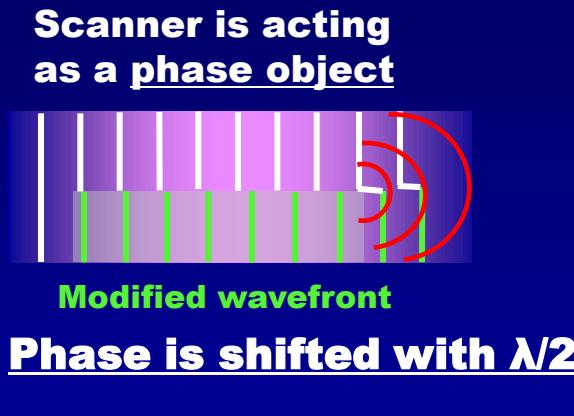
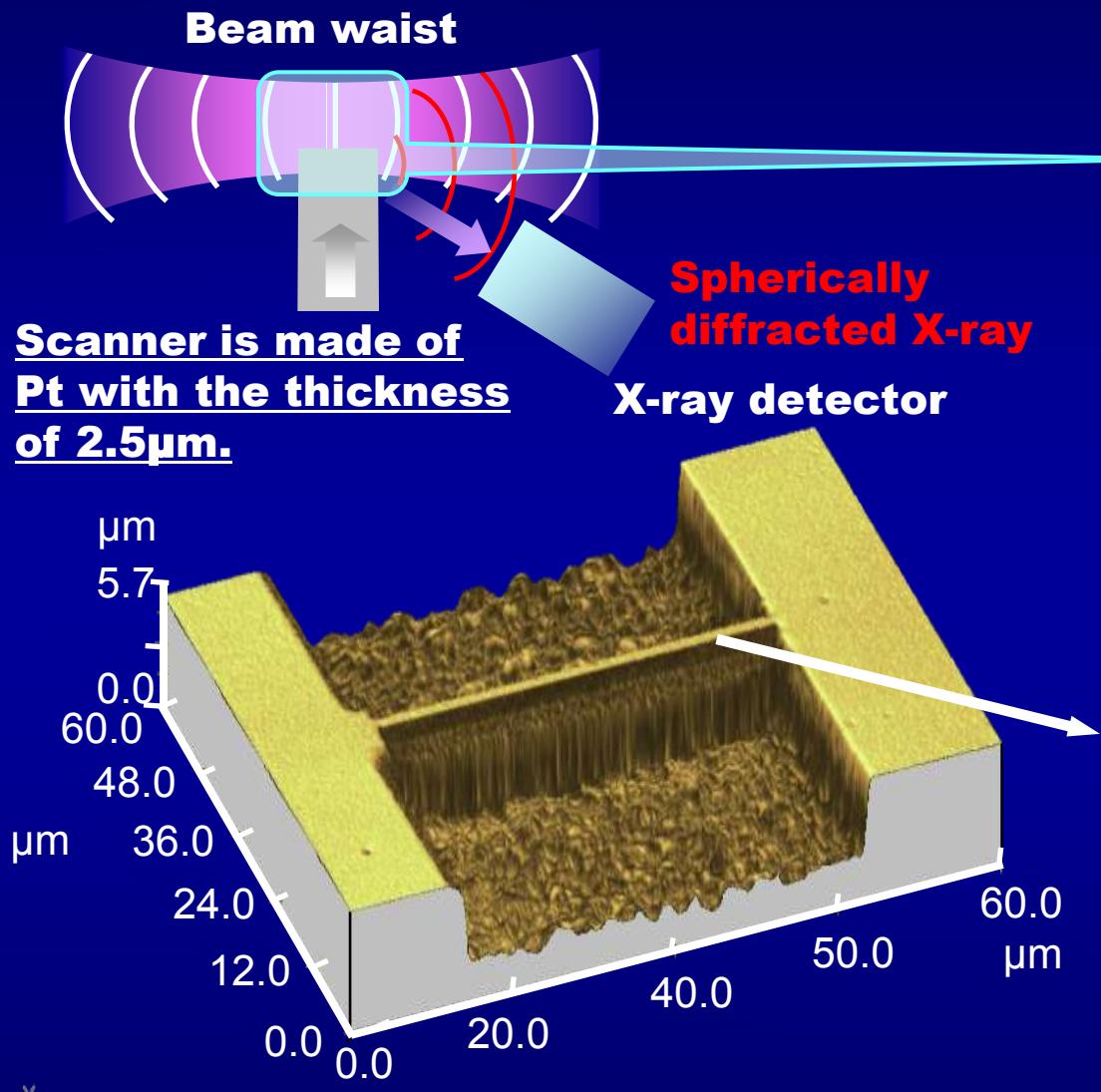
New method



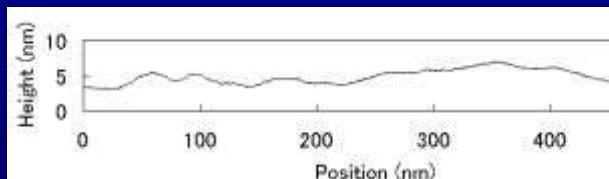
Spherically  
diffracted X-ray

X-ray detector

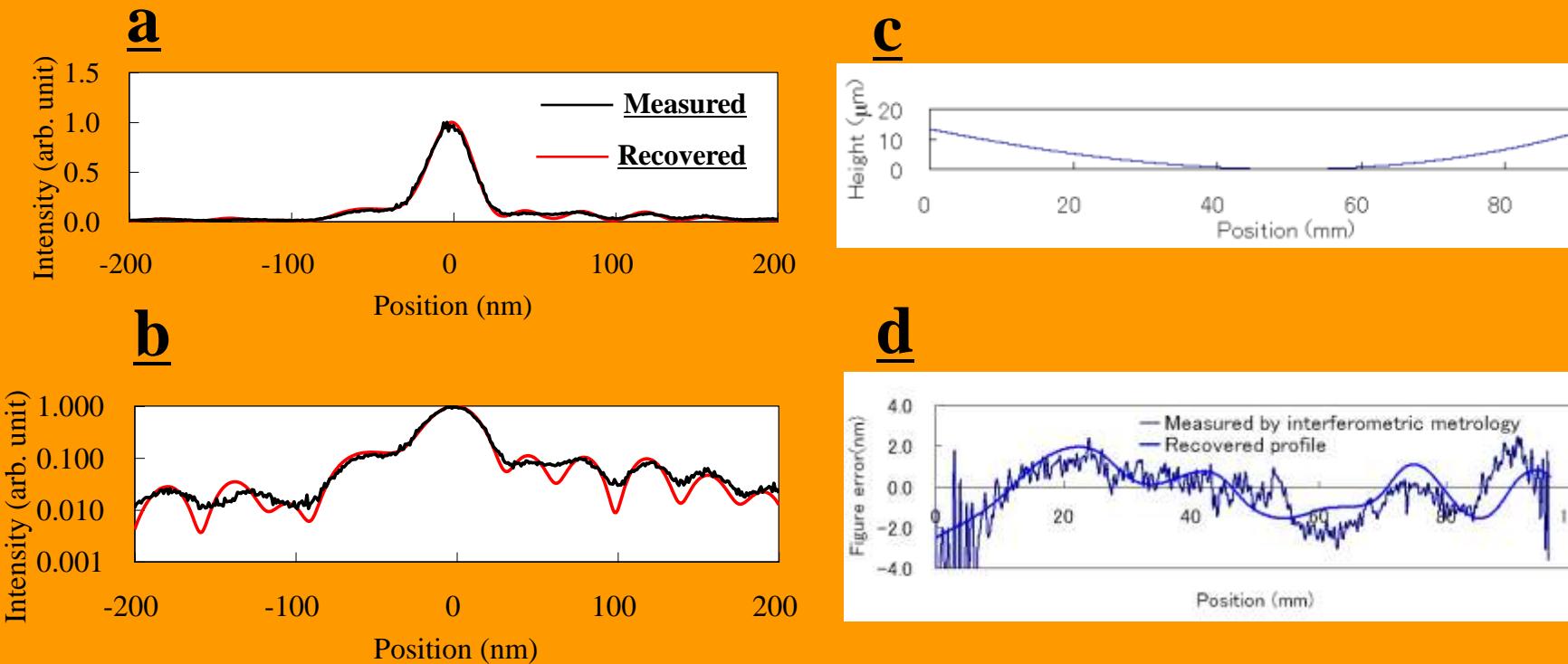
# Details of the new knife-edge method



**Microroughness at the bridge**

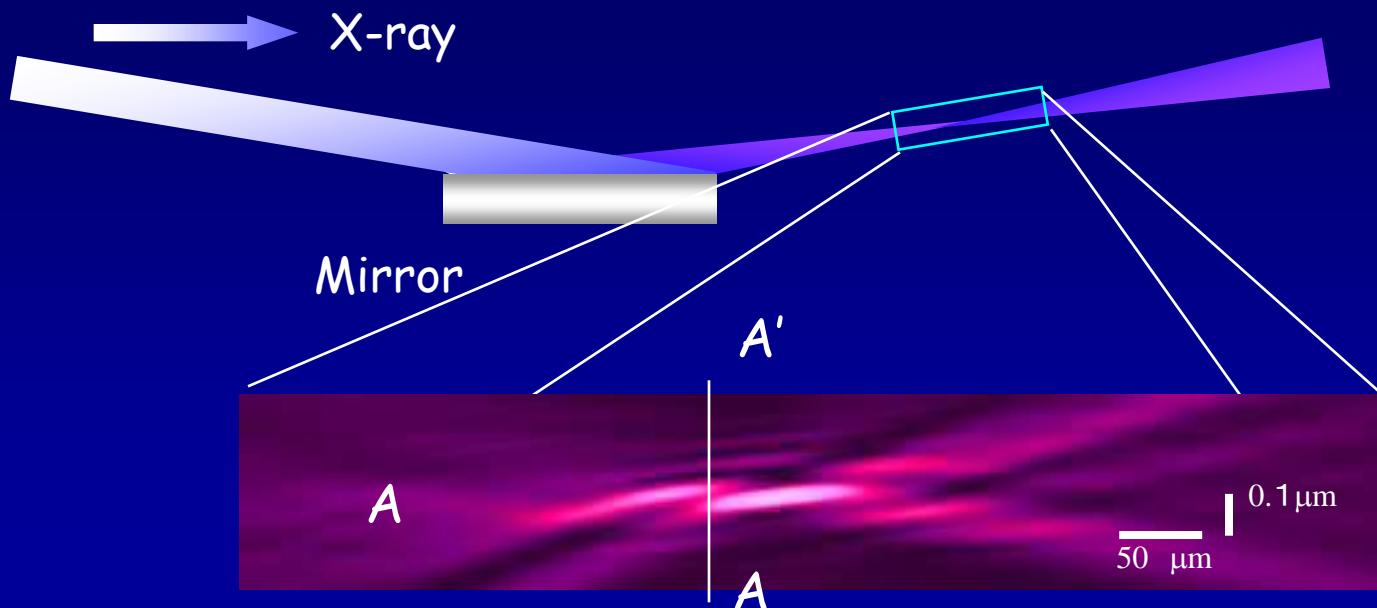


# A demonstration of at-wavelength measurement (30nm-focusing mirror was employed)

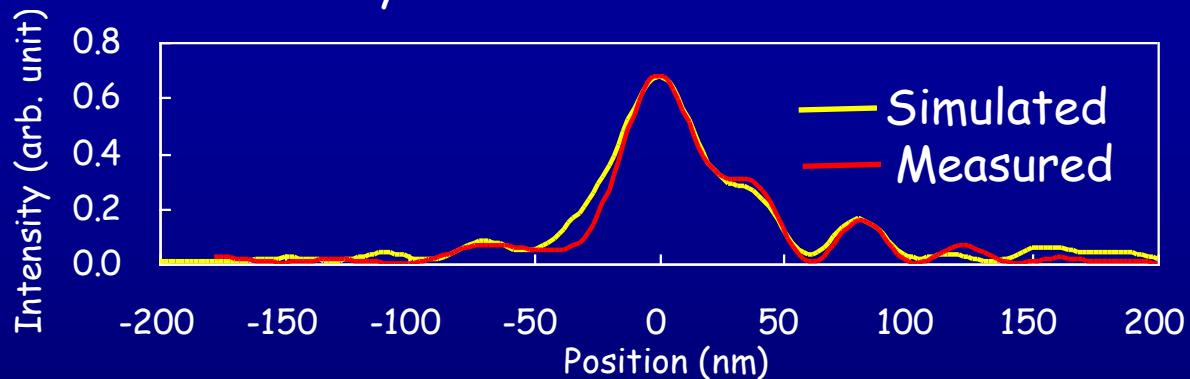


**FIG. 3. Results of measuring intensity profiles in the focal plane and phase retrieval calculations.** A Intensity profiles in the focal plane. The black line is the profile measured by scanning the microbridge, while the red line was obtained using phase retrieval calculations for determining the mirror surface profile. The plot interval is 1 nm. b Single logarithmic plot of graph in a. c Ideal profile of x-ray mirror. d Comparison of measured and reconstructed figure error profiles.

# To avoid local-minimum problem

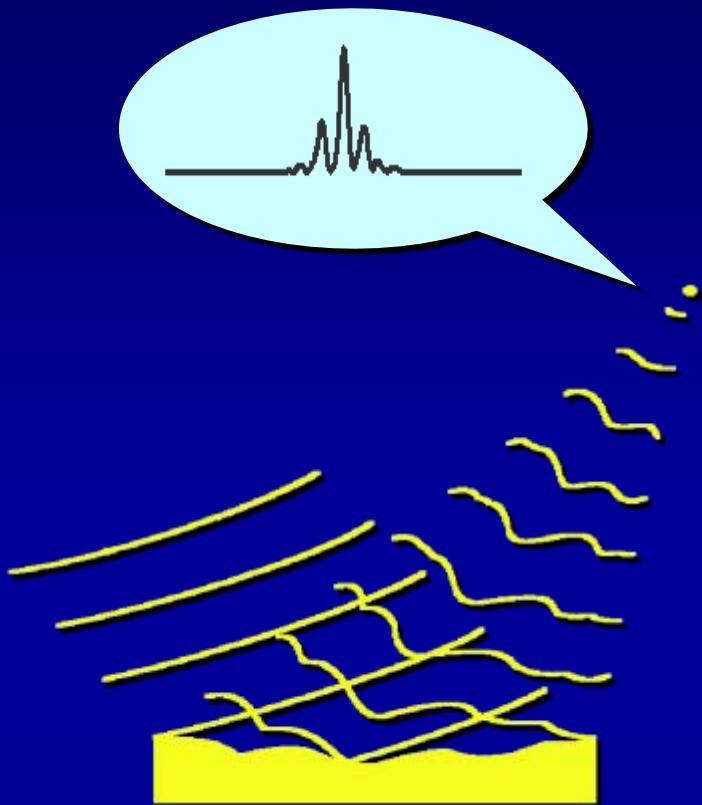


Intensity distribution at beamwaist



Calculated and measured intensity profiles on A-A' line.  
(50 μm upstream from the focal point)

# On-line compensation of wavefront

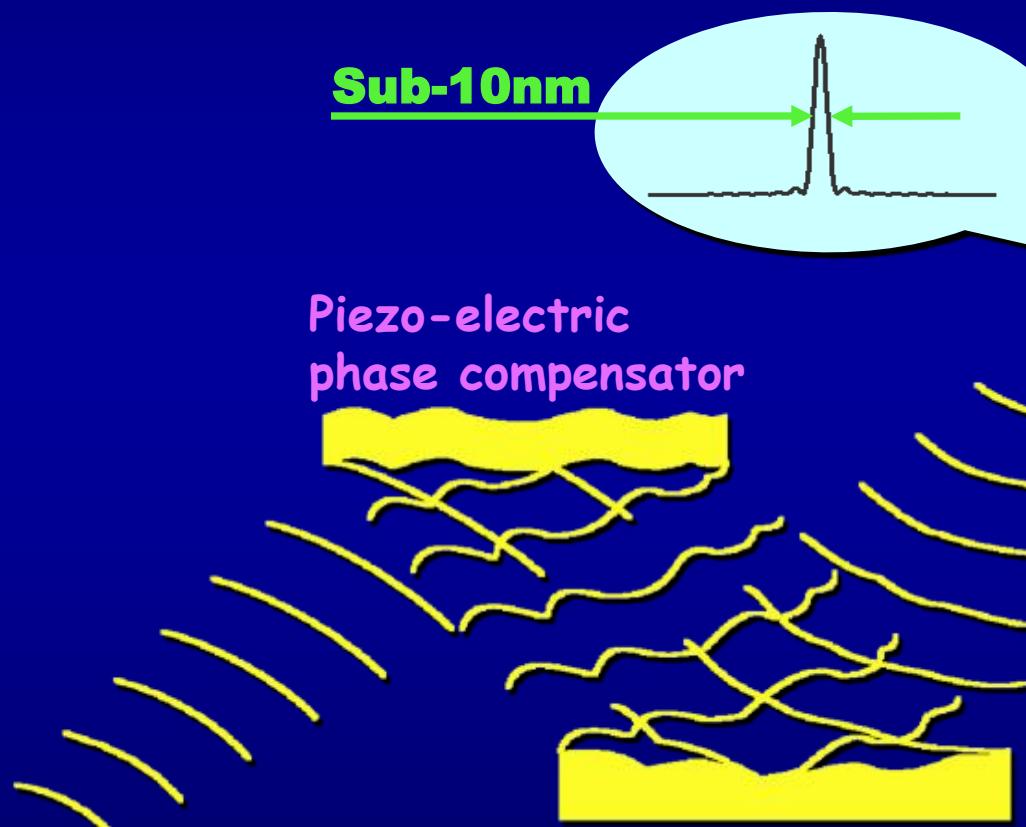


Focusing mirror with phase error

In-situ phase compensation

**Sub-10nm**

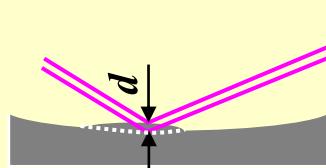
Piezo-electric  
phase compensator



Focusing mirror with phase

# Designing 1 (reduction of required accuracy)

$$\text{Phase error} = 2kd \sin \theta$$



$d$ : Shape error  
 $\theta$ : Glancing angle  
 $k=2\pi/\lambda$  : Wave number



## An example

Glancing angle of 10nm-level focusing mirror: 7 [mrad]  
Glancing angle of active mirror: 1.0 [mrad]



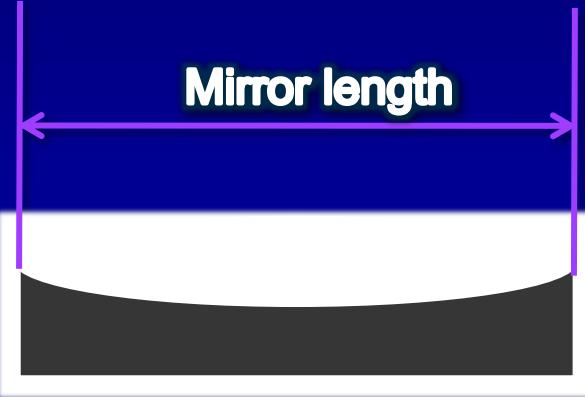
- ★ Required figure accuracy of the 10nm-level focusing mirror is 0.7nm (PV).
- ★ Glancing angle of the active mirror is 7 times smaller than that of the focusing mirror.



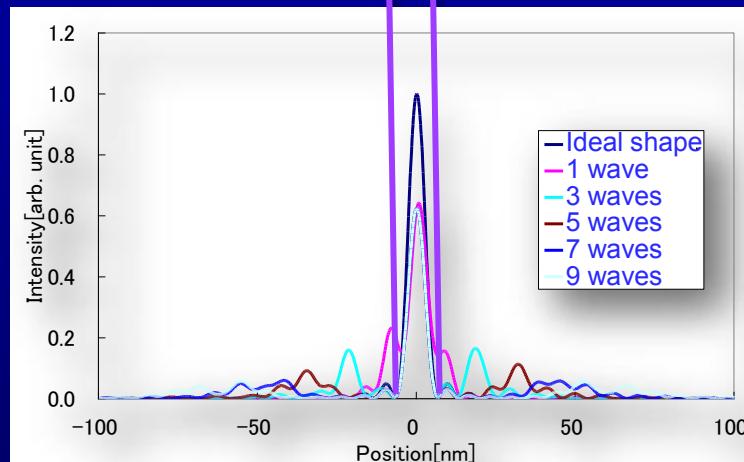
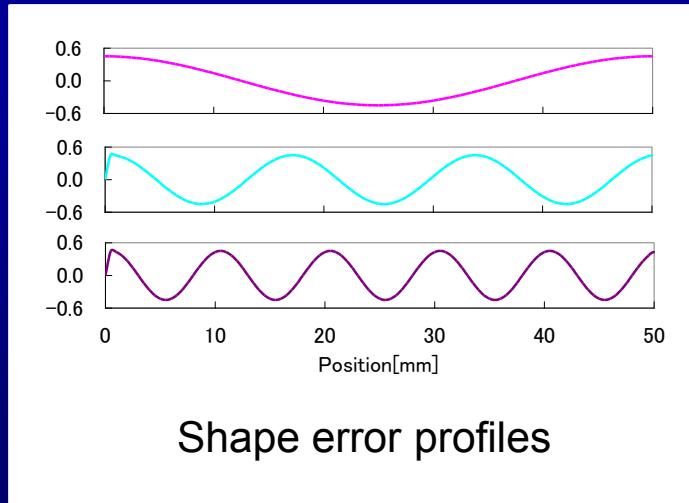
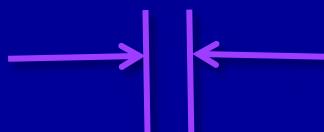
Required figure accuracy of the active mirror becomes 4.9nm (PV).

# Designing 2 (How many waves should be generated by the active mirror?)

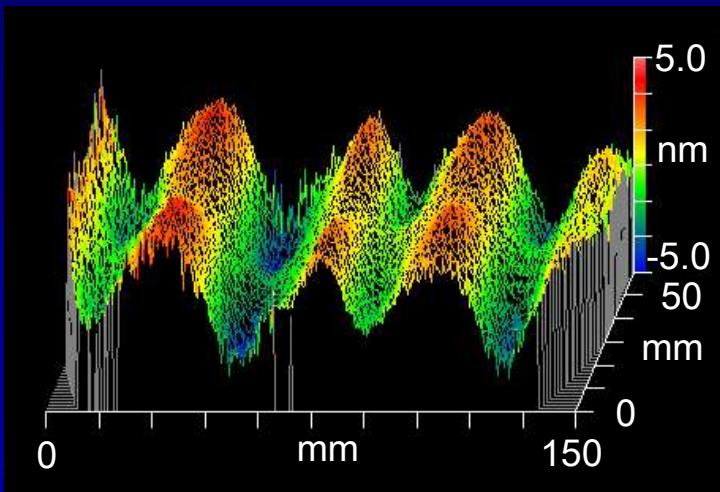
**Spatial wavelength of the figure error and the position of the satellite peak are wave-optically correlated.**



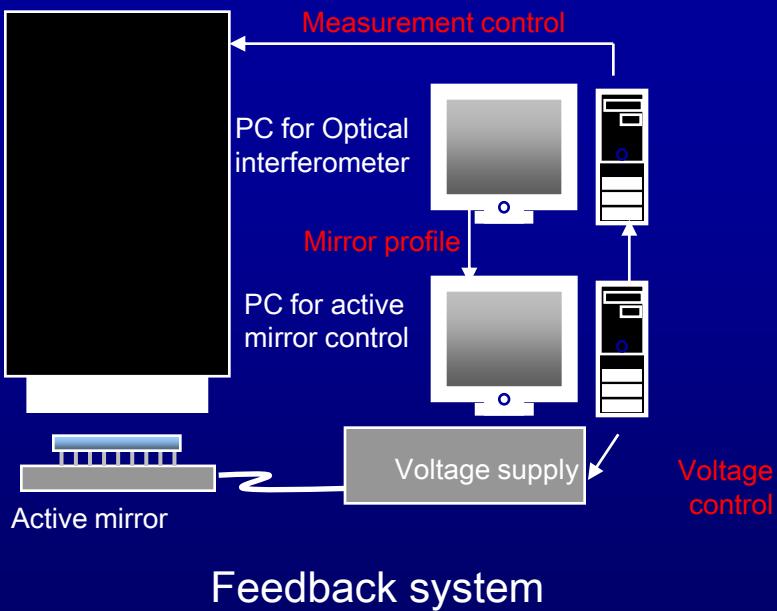
**Beam size**



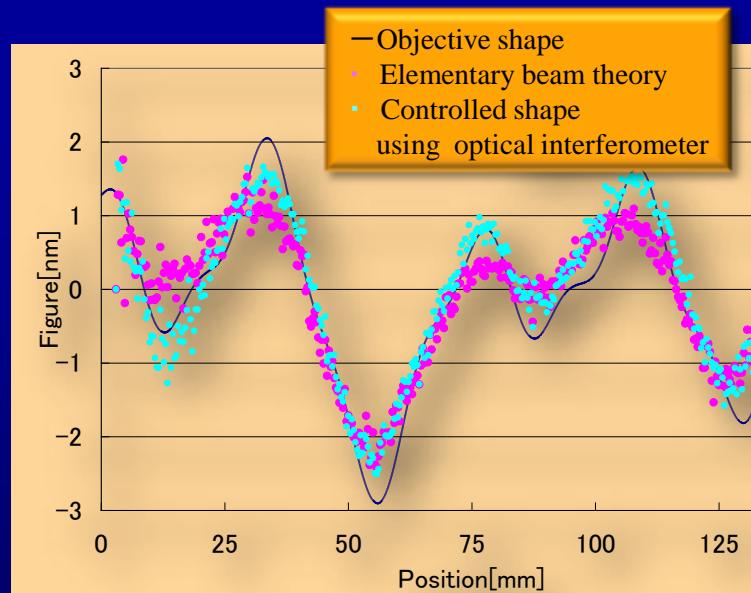
# Phase compensator



Optical interferometer

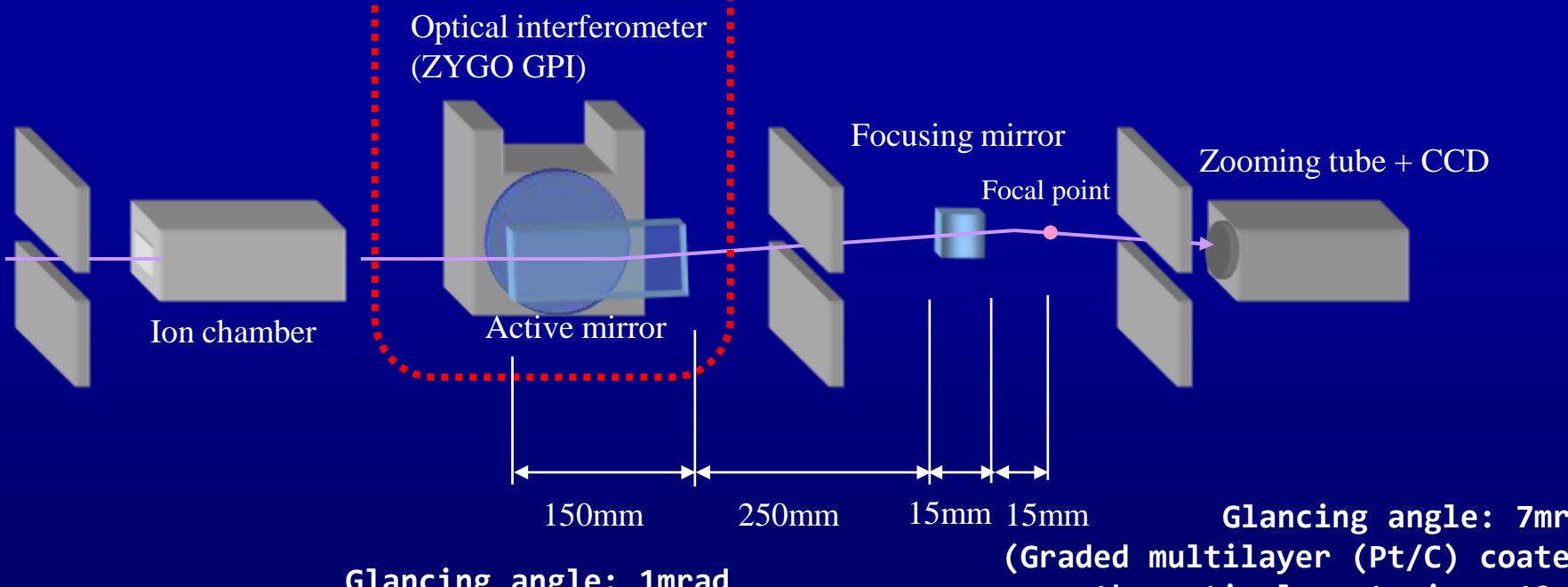


Feedback system

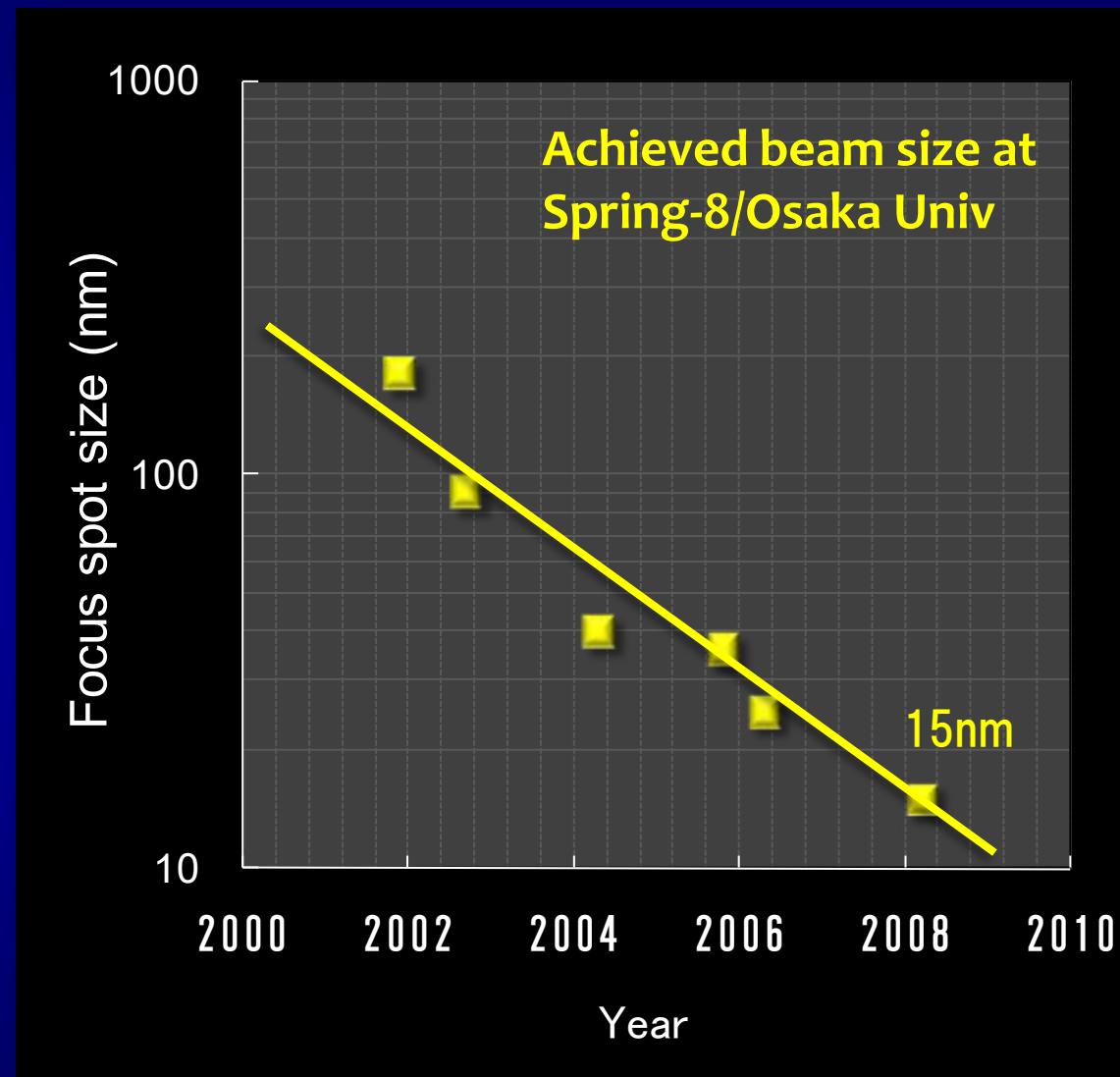
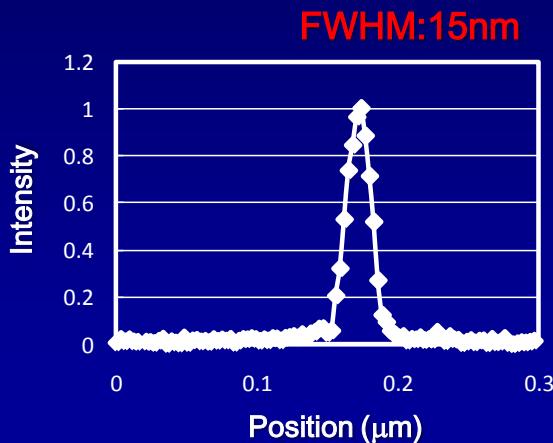


# Optical configuration of 10nm-level focusing with AM

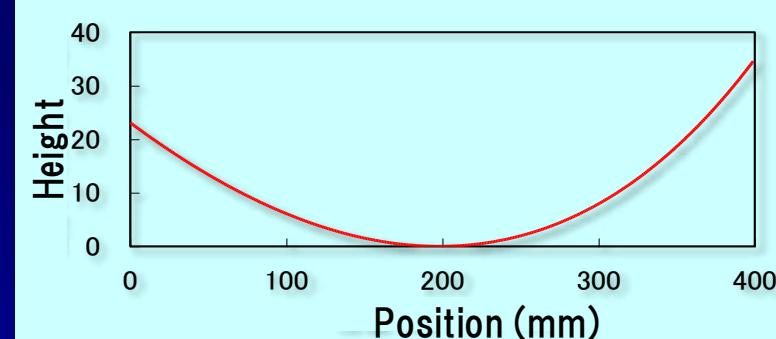
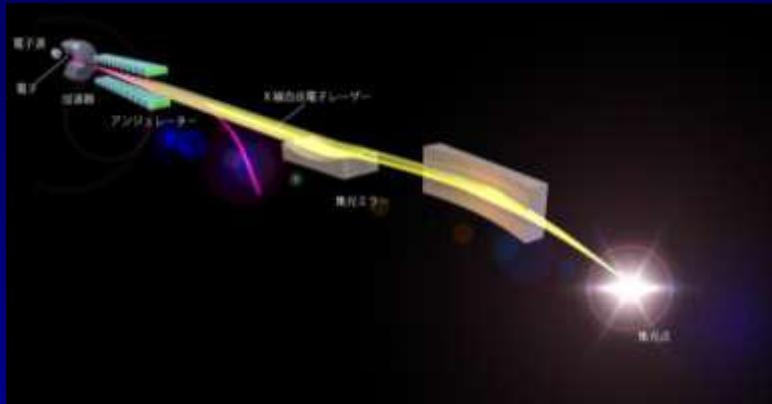
Compensator (AM: Active mirror)



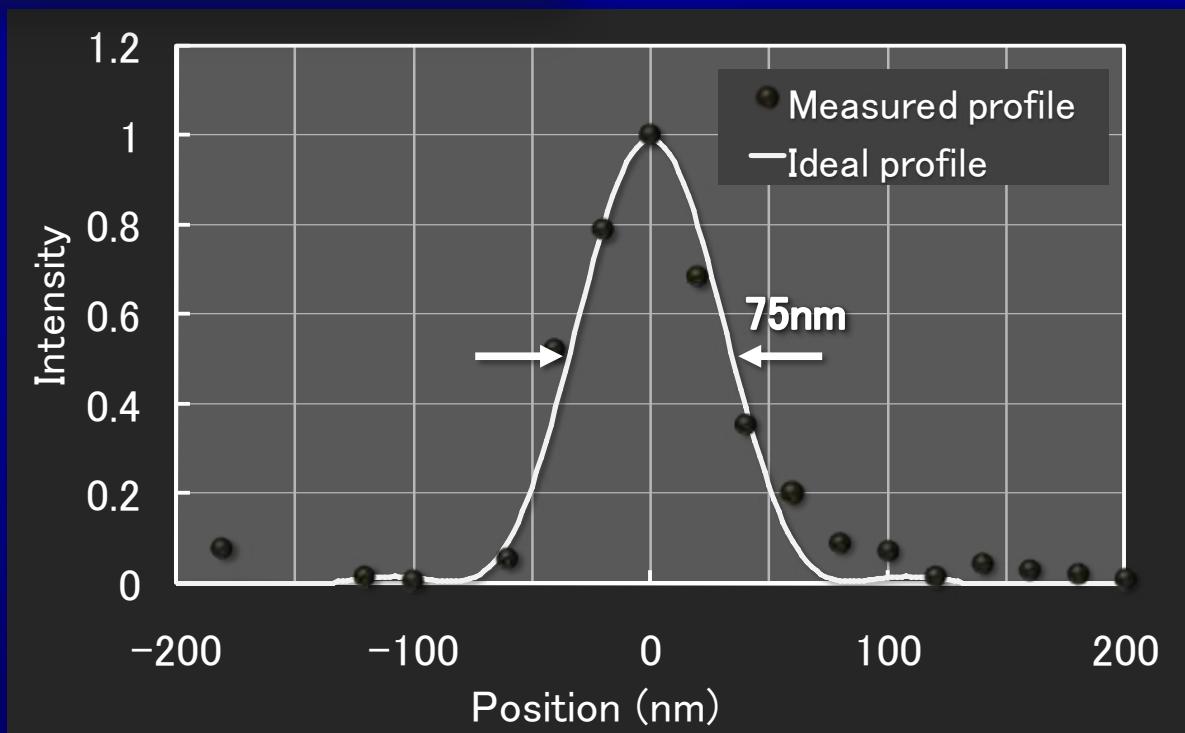
# Achieved beam size at Spring-8



# 400mm-long mirror for XFEL



WD: 350m



# Conclusion

1. Mirror optic has many advantages against the other optics, such as long WD, no chromatic aberration (in case of total reflection mirror), high focusing-efficiency, and relatively large aperture.
2. Diffraction-limited focusing performance has been already realized in mirror focusing.
3. Sub-50nm focusing mirrors become ordinary devices.
4. Phase retrieval interferometry will become a possible technique for the mirror surface testing.
5. Active mirror can control wavefront phase with  $0.1\lambda$ -level accuracy.
6. 10nm-level X-ray beams will be realized in the near future.

# Acknowledgement

## Co-wor ers

Mimura<sup>a</sup>, . umoto<sup>a</sup>, S. Matsuyama<sup>a</sup>, S. anda<sup>a</sup>, . Kimura<sup>a</sup>, . Sano<sup>a</sup>, K. amamura<sup>a</sup>, . ishino<sup>b</sup>, M. abashi<sup>c</sup>, K. amasa u<sup>b</sup>, and . Ishi awa<sup>b,c</sup>

a: Osa a University b: RIKE /SPrin -8

c: ASRI/SPrin -8

This research was supported by

A Grant-in-Aid for Specially Promoted Research 18002009, 2006 from the Ministry of Education, Sports, Culture, Science and Technology, Japan,

A 21st Century COE Research, Center for Atomistic Fabrication Technology, 2003 from the Ministry of Education, Sports, Culture, Science and Technology, Japan,

A Global COE Research, Center for Atomically Controlled Fabrication Technology, 2008 from the Ministry of Education, Sports, Culture, Science and Technology, Japan,

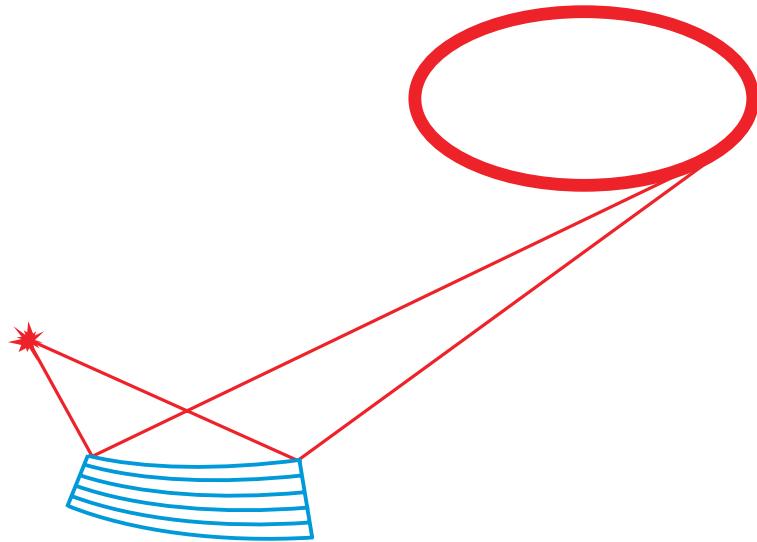
The use of BL29XU of the SPring-8 was supported by RIKEN.

# Hard X-ray focusing with curved reflective multilayers

Ch. Morawe, ESRF (France)

## Outline:

- Basic focusing considerations
- Theoretical models
- Multilayer properties
- Technological options
- Experimental progress
- Summary



# Basic considerations

**Diffraction limit**

$$D_{FWHM} = C \frac{\lambda}{NA}$$

Numerical aperture

$$NA = n \cdot \sin \varepsilon$$

Straight aperture

$$C = 0.44$$

**Source size limit**

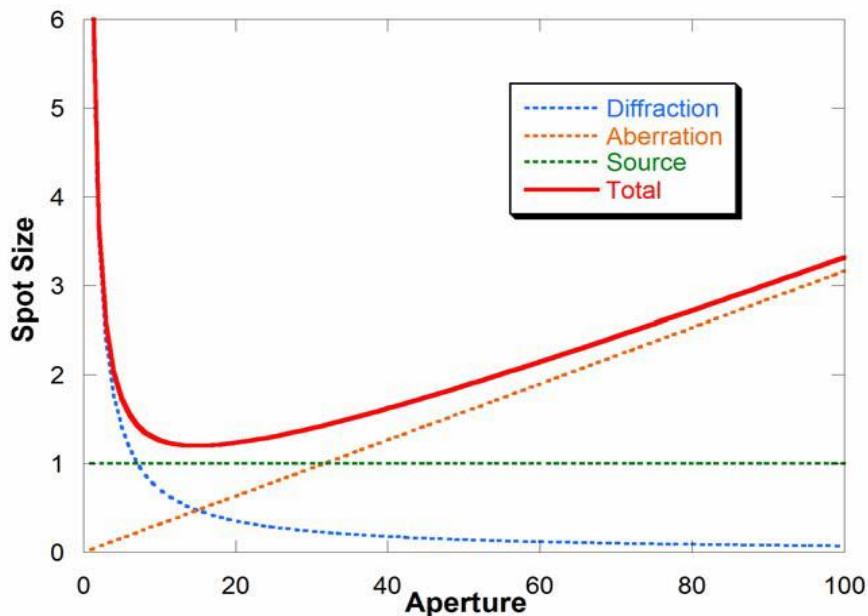
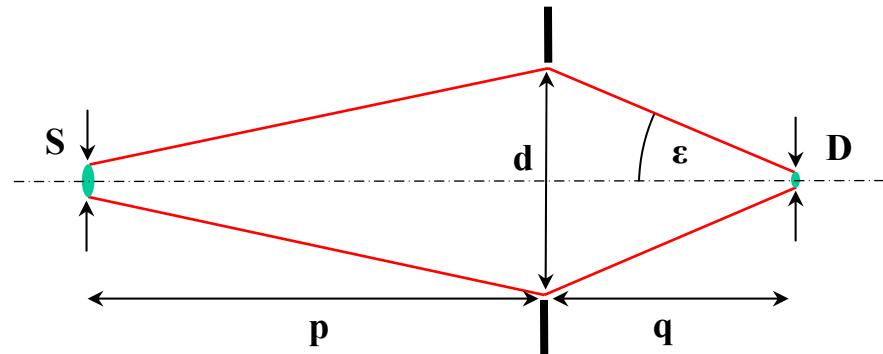
$$D = \frac{q}{p} \cdot S$$

**Further physical limitations**

- Volume diffraction
- Scattering

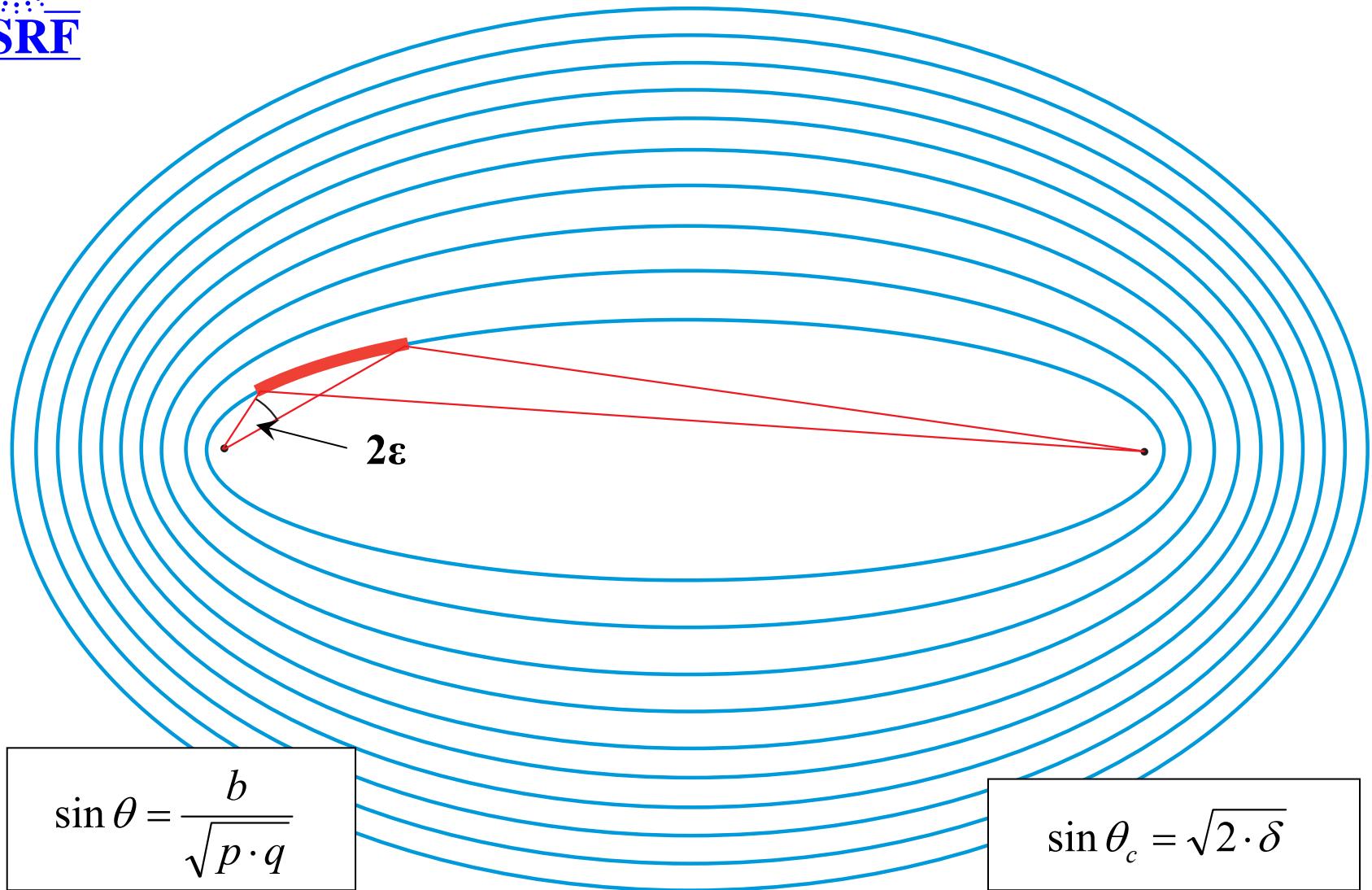
**Technological limitations**

- Non-trivial design
- Fabrication accuracy
- Alignment



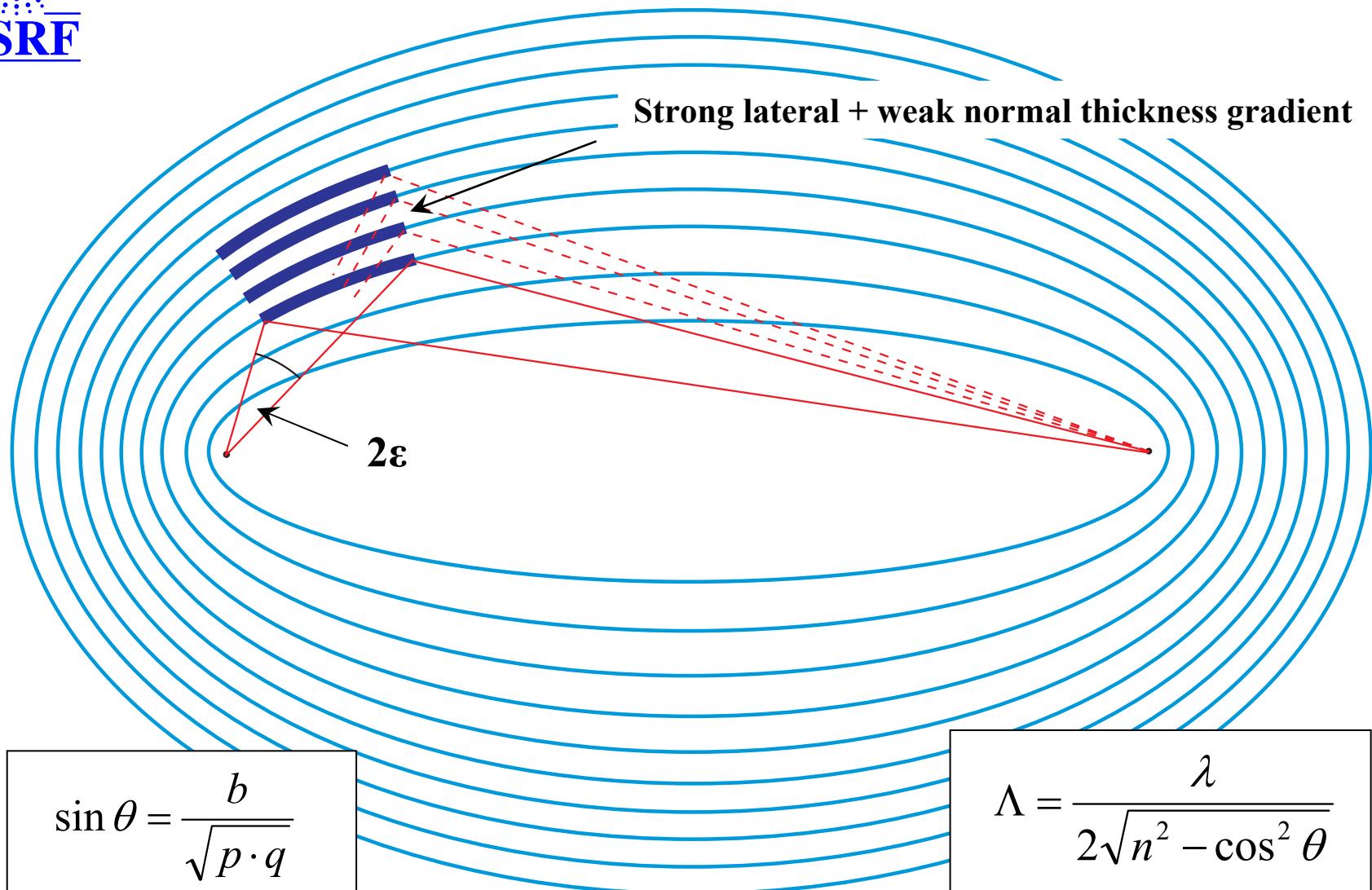
## Geometrical approximation

## Total reflection mirrors



## Geometrical approximation

## Multilayer mirrors



# Basic considerations

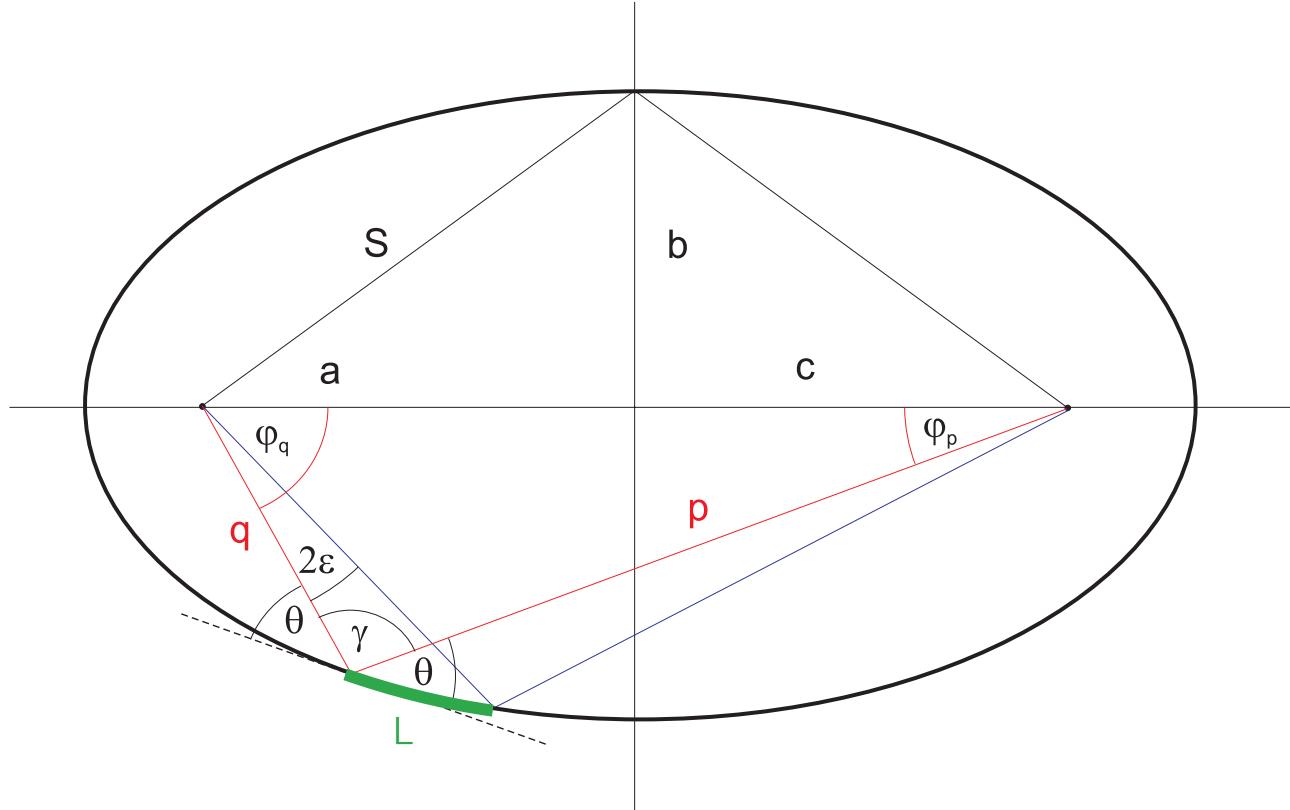
## Ellipse geometry

$$2\varepsilon = \varphi_q(\theta_2) - \varphi_q(\theta_1)$$

$$\sin \varphi_q = \frac{p \cdot \sin 2\theta}{2 \cdot c}$$



$$NA = n \cdot \sin \varepsilon$$



Correct only for flat aperture !

# Basic considerations

## Simple approximation:

### a) Total reflection mirror

$$\sin \varepsilon \approx \frac{1}{4} \sin \theta_c = \frac{\sqrt{2 \cdot \delta}}{4} = \frac{\lambda}{4} \sqrt{\frac{r_0 \rho_e}{\pi}}$$

$$\Rightarrow D_{FWHM} \approx 1.76 \cdot \sqrt{\frac{\pi}{r_0 \rho_e}}$$

**D<sub>FWHM</sub> ≈ 25 nm (Pt)**

### b) Multilayer mirror

$$\sin \varepsilon = \frac{1}{4 \cdot c} (p_2 \cdot \sin 2\theta_2 - p_1 \cdot \sin 2\theta_1)$$

$$\sin 2\theta \approx 2 \cdot \sin \theta \approx \frac{\lambda}{\Lambda}, p \approx 2 \cdot c$$

$$\Rightarrow \sin \varepsilon \approx \frac{\lambda}{2} (1/\Lambda_2 - 1/\Lambda_1)$$

$$\Rightarrow D_{FWHM} \approx \frac{0.88}{1/\Lambda_2 - 1/\Lambda_1}$$

**D<sub>FWHM</sub> ≈ 5 nm**

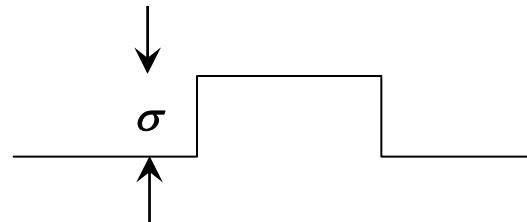
No explicit energy dependence !

# Theoretical models

## Geometrical phase shift due to height/slope errors

$$\varphi_h = \frac{4\pi \cdot \sigma \cdot \sin \theta}{\lambda}$$

$\sigma$ : height error



Reasonable values for ML mirrors with 80% flux in focal spot

$$\sigma_{RMS} \leq \frac{\lambda}{27 \cdot \sin \theta} \approx \frac{\Lambda}{13.5} \quad \Rightarrow \sigma_{RMS} \stackrel{!}{<<} 1 \text{ nm}$$

O. Hignette et al, SPIE 4501 (2001)

Similar results from wave optical simulations

H. Yumoto et al, SPIE 6317 (2006)

**Challenge for fabrication and metrology !**

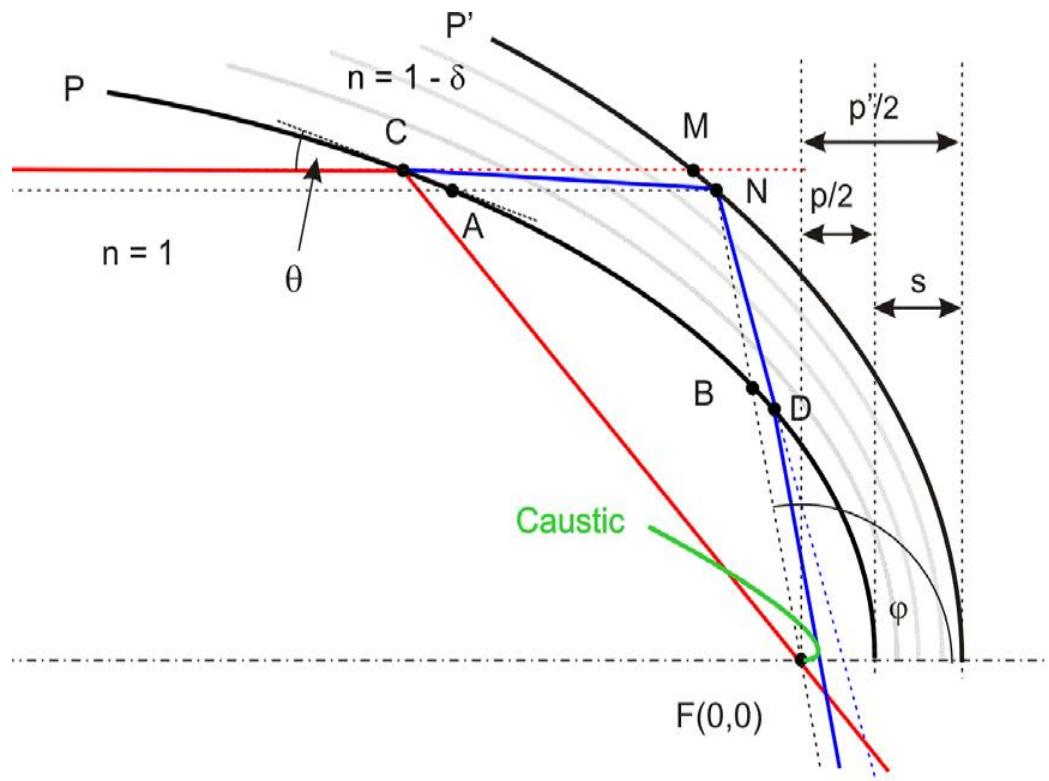
# Theoretical models

## Geometrical ray tracing

- Analytical approach
- Parabolic/elliptic shape
- $ML \cong$  Two-interface slab
- Linear approximation for refraction
- Simple expressions for caustic and beam intersections

## Goals

- Caustic shape
- Beam intersections
- Chromatic behavior

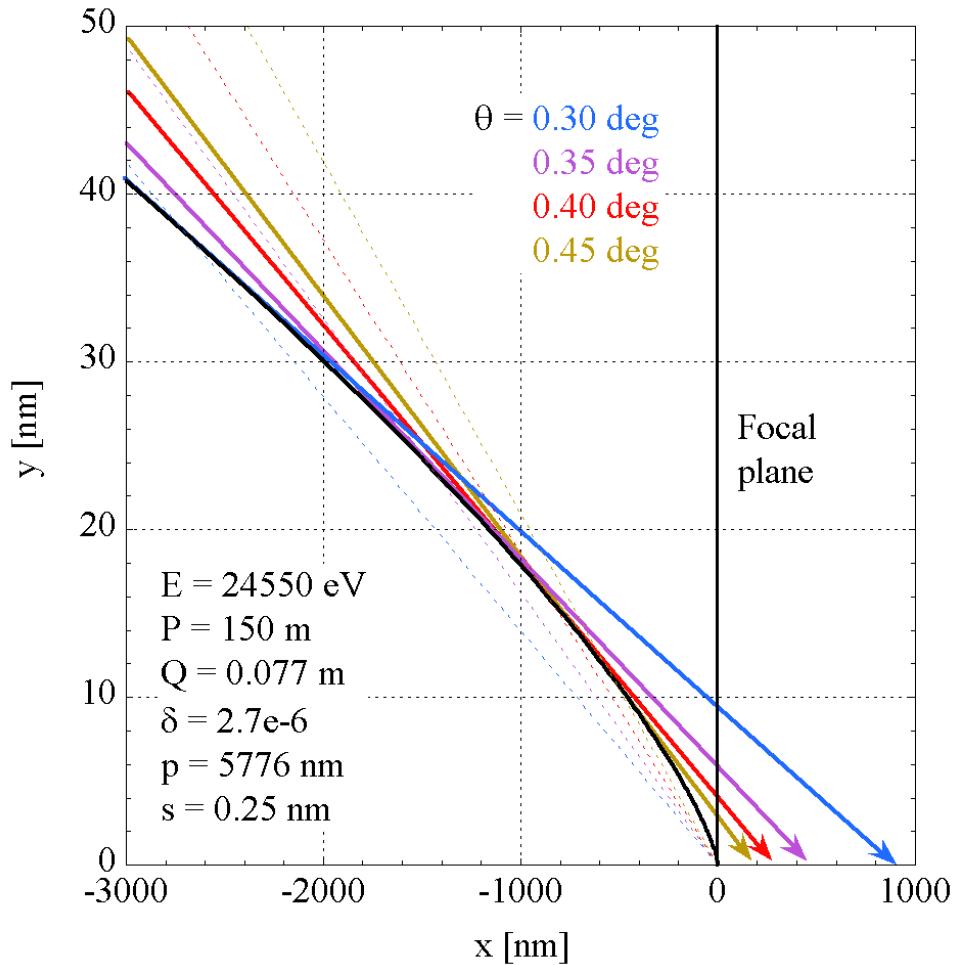


J-P. Guigay et al, Opt. Express 16, 12050 (2008)

# Theoretical models

## Caustic and beam intersections

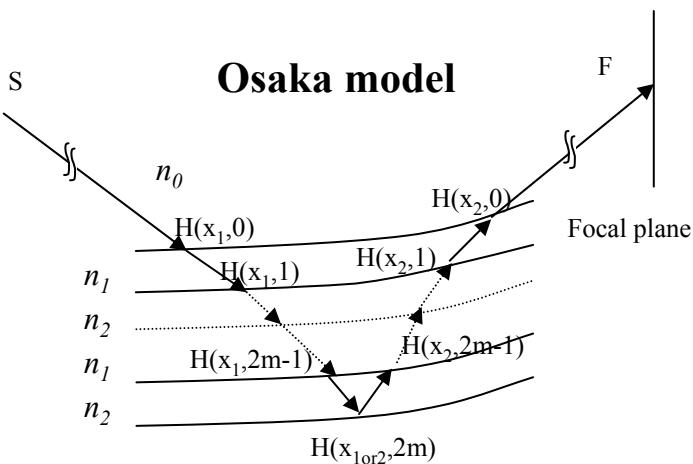
- x and y diverge at grazing incidence
- Refraction and penetration amplify the effect
- Reduced aberration for increased angles of incidence
- Order of magnitude:  
 $\Delta x \leq 1000 \text{ nm}$   
 $\Delta y \leq 10 \text{ nm}$



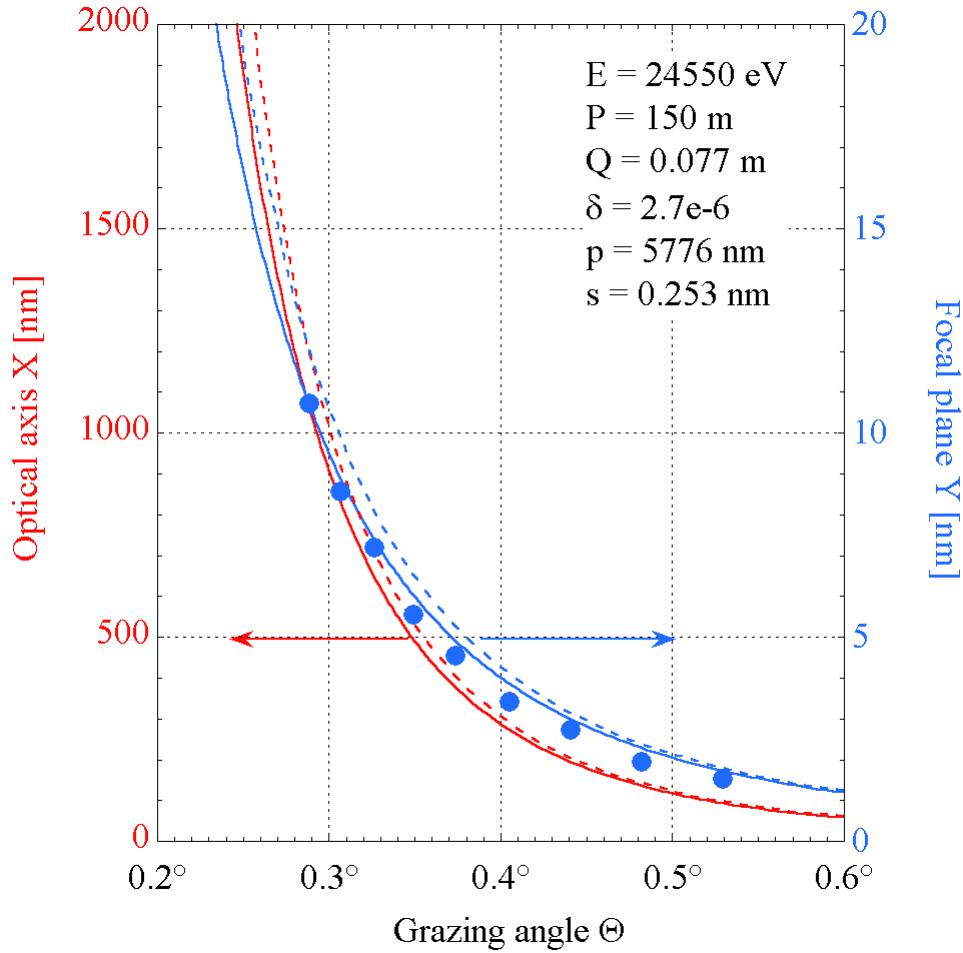
# Theoretical models

## Exact ray tracing

- Snell's law
- No approximations
- Good agreement with analytical model
- Linear approach for refraction fails near critical angle
- Agreement ESRF – Osaka



H. Mimura et al, SPIE 67050L (2007)

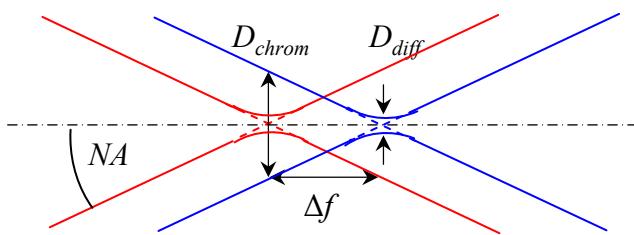


# Theoretical models

## Chromaticity

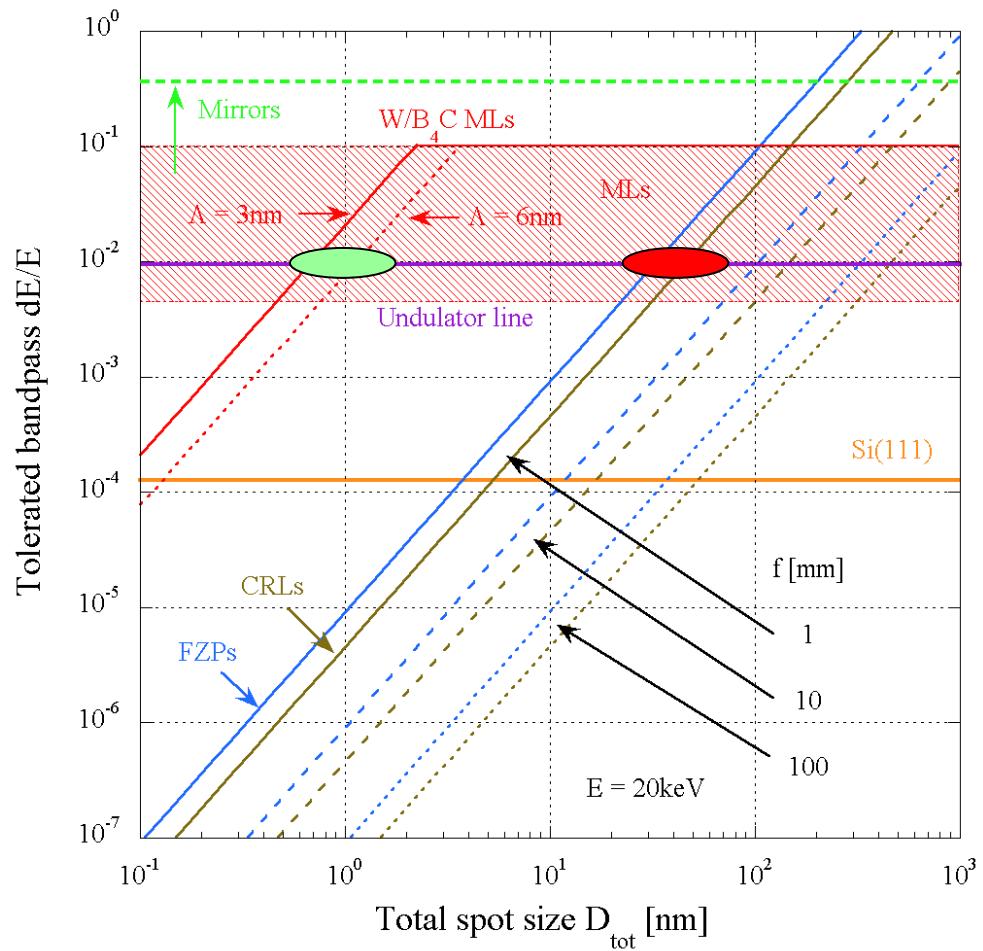
$$\delta \sim \frac{1}{E^2} \rightarrow \left| \frac{df}{dE} \right| = 2 \cdot \frac{\Delta f}{E}$$

$$D_{tot}^2 = D_{diff}^2 + D_{chrom}^2 \stackrel{!}{\leq} 2 \cdot D_{diff}^2$$



	FZP	CRL	RML
$\frac{dE}{E}$	$\frac{D_{tot}^2}{1.76 \cdot f \cdot \lambda}$	$\frac{D_{tot}^2}{3.52 \cdot f \cdot \lambda}$	$\frac{D_{tot}^2}{3.52 \cdot \Delta f \cdot \lambda}$

Secondary effect on focus !



# Theoretical models

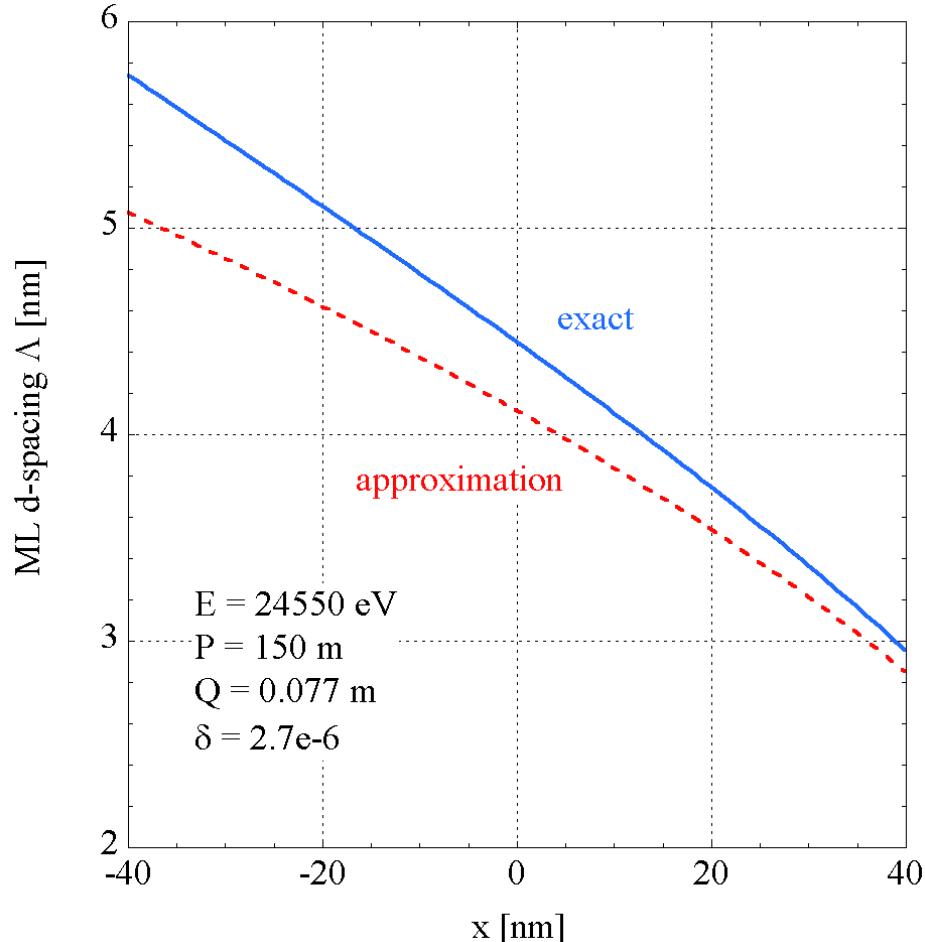
**Are we already doing better ?**

- ML design via corrected Bragg law

$$\Lambda = \frac{\lambda}{2\sqrt{n^2 - \cos^2 \theta}} \left( \approx \frac{\lambda}{2 \cdot \sin \theta} \right)$$

- Refraction implicitly considered
- ML interface shapes **not elliptic** (except for surface layer)
- Difficult analytical access
- Aberrations reduced/suppressed ?

**Need for wave optical calculations !**

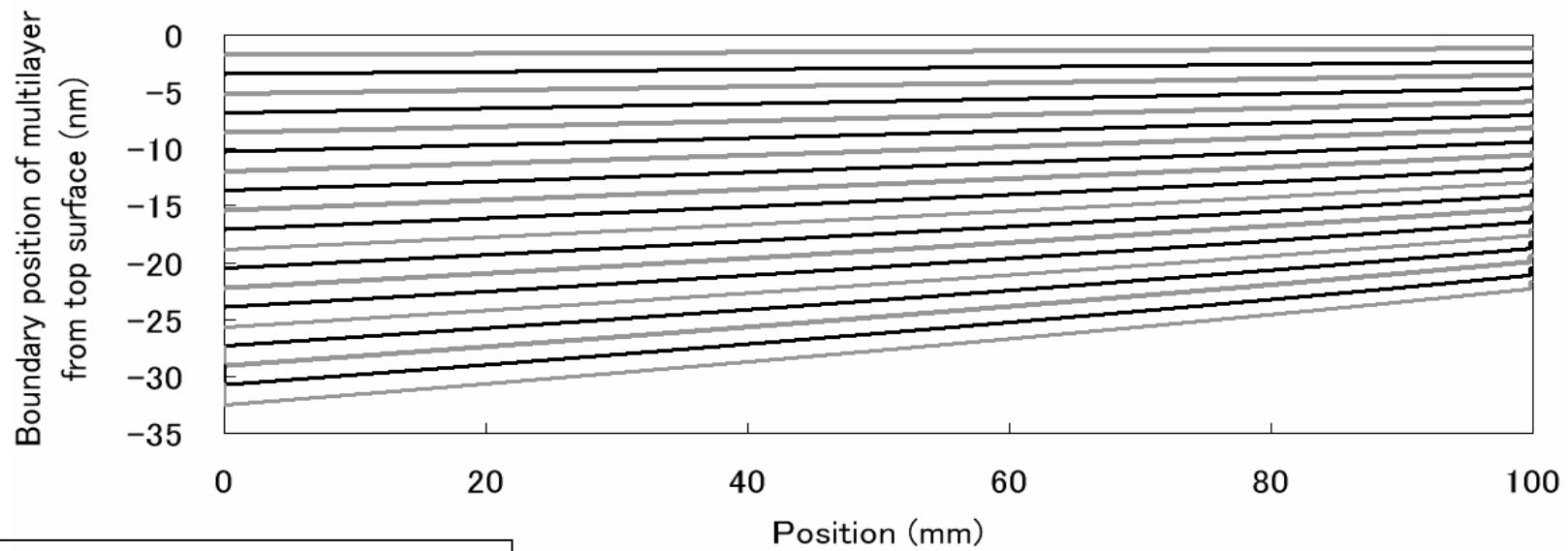


# Theoretical models

## Alternative approach

- ML design via numerical simulation (Osaka University)
- ML ray tracing and optical path optimization
- Equivalent to corrected Bragg equation (?)

$$\Lambda = \frac{\lambda}{2\sqrt{n^2 - \cos^2 \theta}}$$



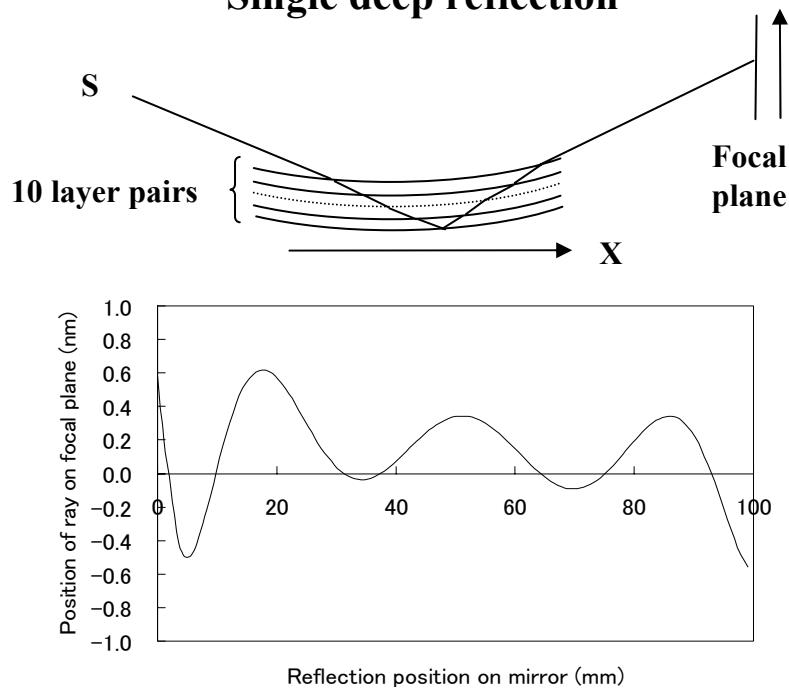
H. Mimura et al, SPIE 67050L (2007)

# Theoretical models

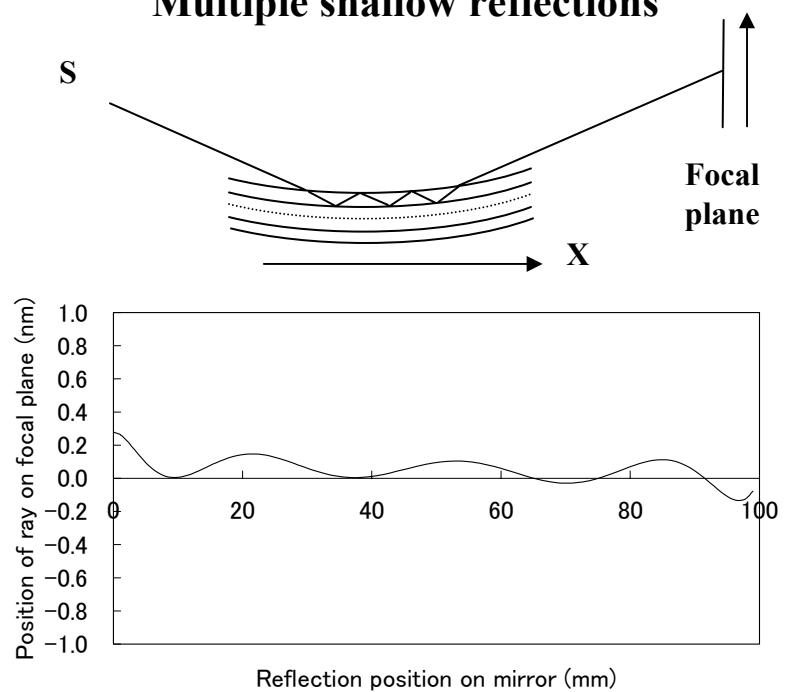
## Results of numerical optimization

H. Mimura et al, SPIE 67050L (2007)

### Single deep reflection



### Multiple shallow reflections

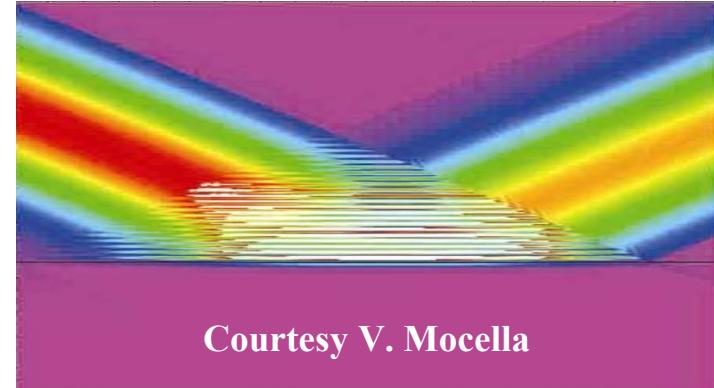


Focal spot blurring < 1 nm !

# Theoretical models

## Wave optical simulations

- Exist for CRLs, FZPs, and MLLs
  - predict diffraction limited focusing
  - spot size down to nm dimensions
- Not yet available for reflecting MLs
- Space for future investigation



## PhD project ESRF/Univ.Göttingen

### PhD Thesis Student (m/f)

**Subject: “Wave optical simulations for x-ray nano-focusing optics”**

**Place of Work:** ESRF Grenoble (France) / University of Göttingen (Germany)

**Supervisors:** ESRF: Dr. Ch. Morawe (+33) (0)4 76 88 25 88  
Göttingen: Prof. Dr. T. Salditt (+49) (0)551 39 9427

**Ref. CFR320 - Deadline for returning application forms: 30 September 2008**

# Multilayer properties

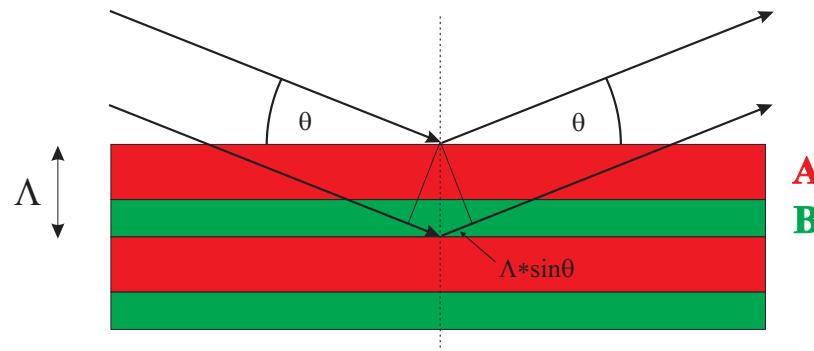
## Numerical calculations: Dynamical theory of flat MLs

- Bragg peaks and fringes due to interference
- Positions depend on E and  $\Lambda$
- Intensities depend on  $\Delta\rho$ , N,  $\sigma$ ...

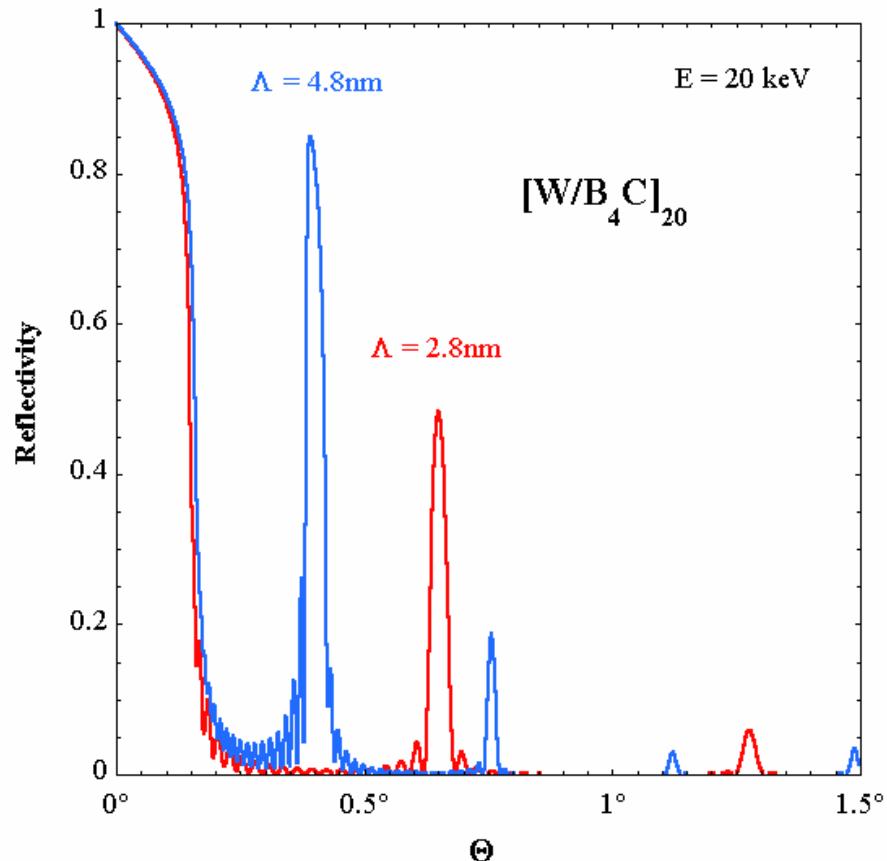
## Corrected Bragg equation

$$m \cdot \lambda = 2 \cdot \Lambda \cdot \sqrt{n_2^2 - n_1^2 \cos^2 \theta}$$

For  $\theta \gg \theta_C \rightarrow m \cdot \lambda \approx 2 \cdot \Lambda \cdot \sin \theta$



L.G. Parratt, Phys. Rev. 95, 359 (1954)



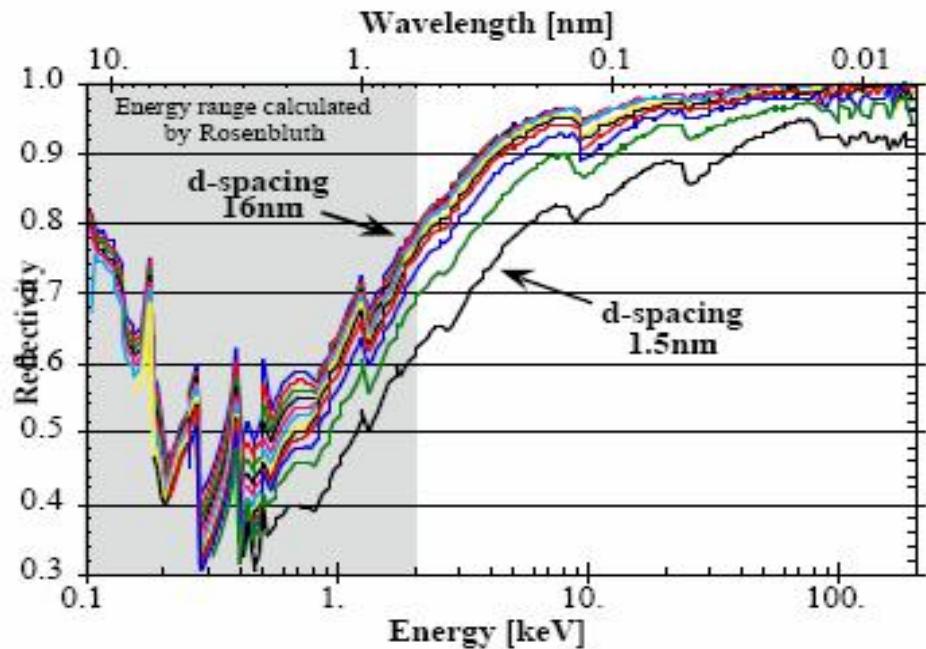
# Multilayer properties

## Materials choice – Basic rules:

1. Select low-Z spacer material with lowest absorption ( $\beta_{\text{spacer}}$ )
2. Select high-Z absorber material with highest reflectivity with spacer ( $\delta_{\text{abs}} - \delta_{\text{spacer}}$ )
3. In case of multiple choices select high-Z material with lowest absorption ( $\beta_{\text{abs}}$ )
4. Make sure that both materials can form stable and sharp interfaces (lower d-spacing limit)

## Computational search algorithms

- Soft X-rays: A.E. Rosenbluth (1988)
- Hard X-rays: K. Vestli (1995)



K. Vestli et al, Rev. Sci. Instr. 67, 3356 (1996)

# Multilayer properties

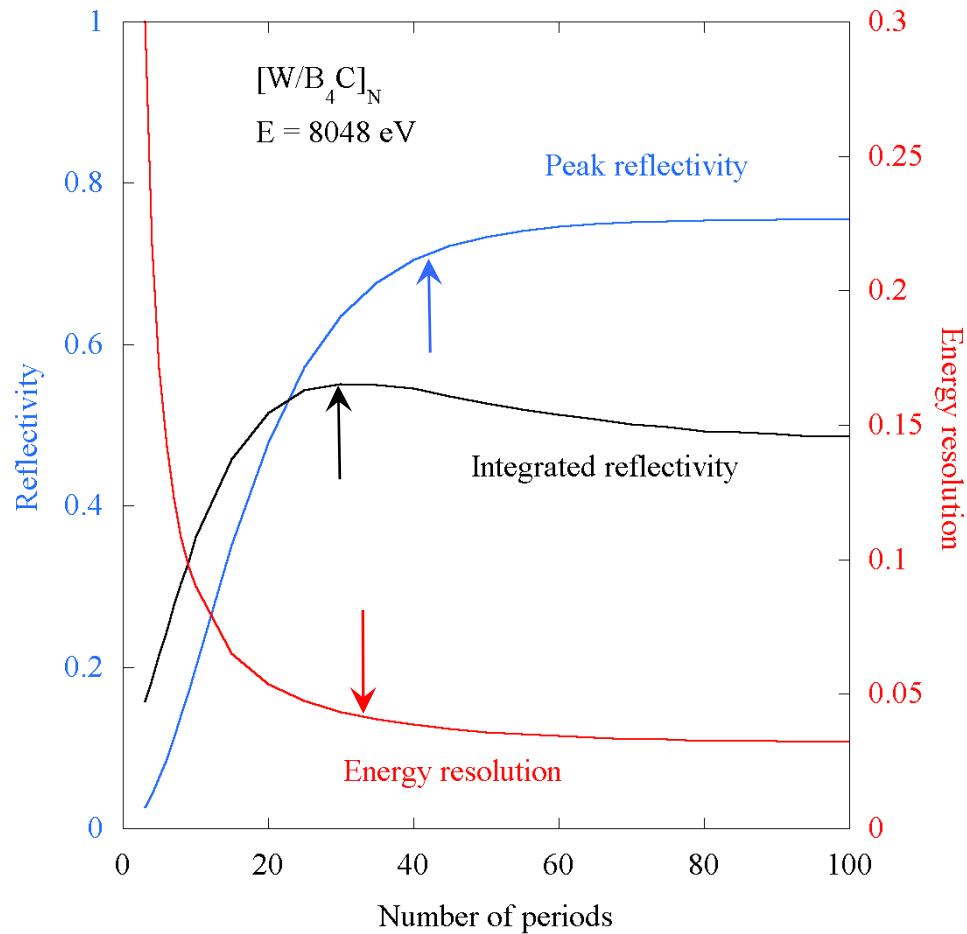
## Period number N:

### Peak versus integrated reflectivity:

- $R_{\text{peak}}$  increases with  $N$  up to extinction
- $\Delta E/E$  decreases  $\sim 1/N$  in kinematical range
- $R_{\text{int}}$  is maximum before extinction

High and low resolution MLs

Optimize  $N$  according to needs !



# Multilayer properties

Filling factor  $\Gamma = t_{abs}/\Lambda$

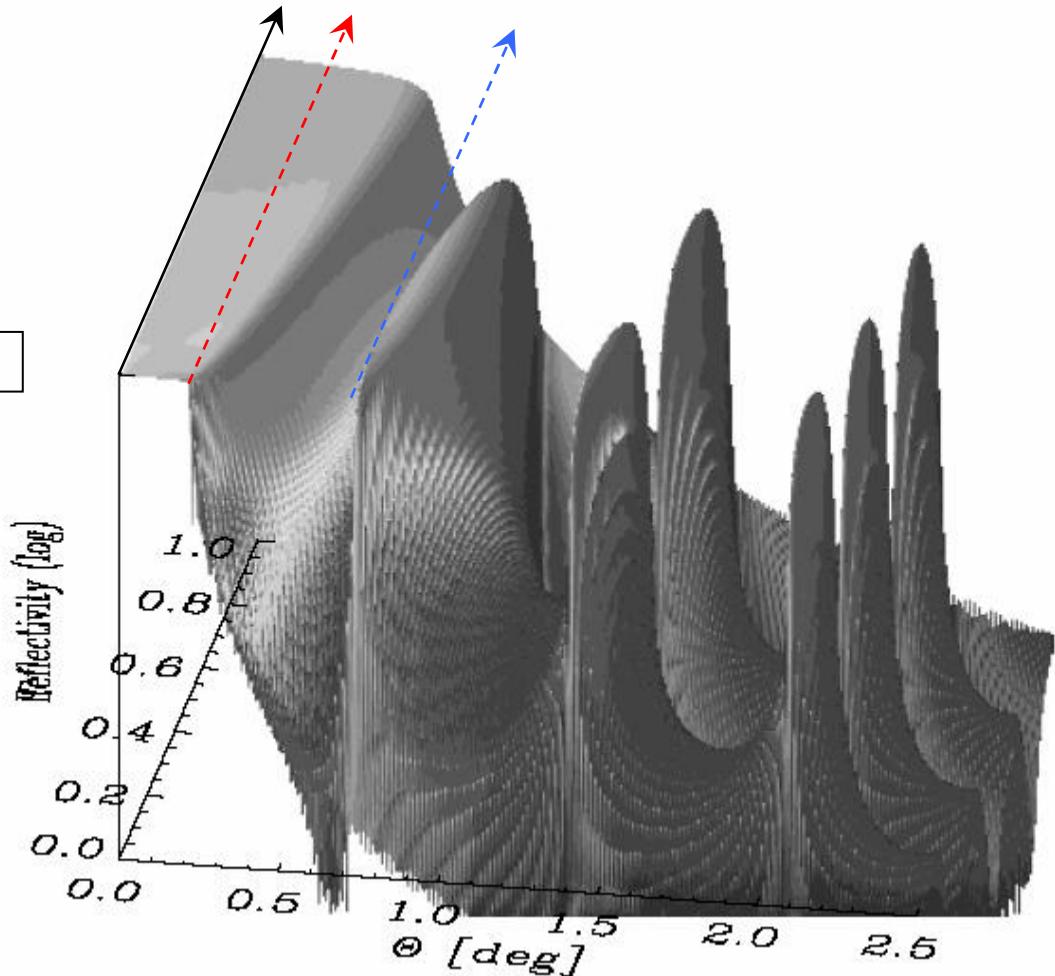
- Harmonics suppression
- Reflectivity enhancement

Optimum  $\Gamma$  for large N

A.V. Vinogradov et al, Appl. Opt. 16, 89 (1977)

$$\tan(\pi \cdot \Gamma_{opt}) \approx \pi \cdot \left( \Gamma_{opt} + \frac{\beta_{abs}}{\beta_{abs} - \beta_{spacer}} \right)$$

Best  $\Gamma$  drops with growing N !



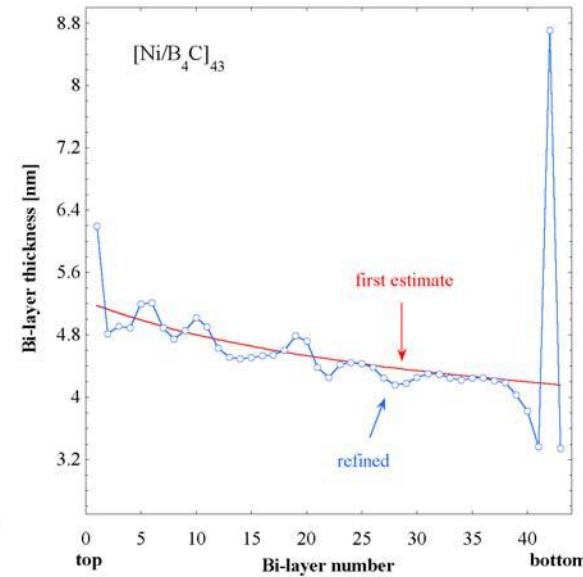
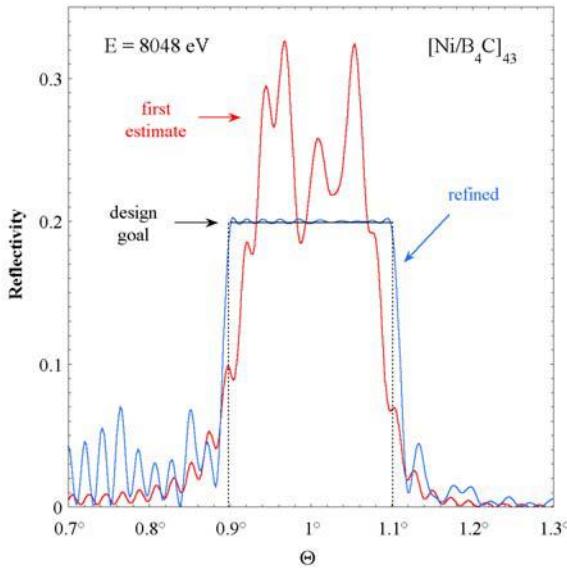
# Multilayer properties

## Non-periodic stacks:

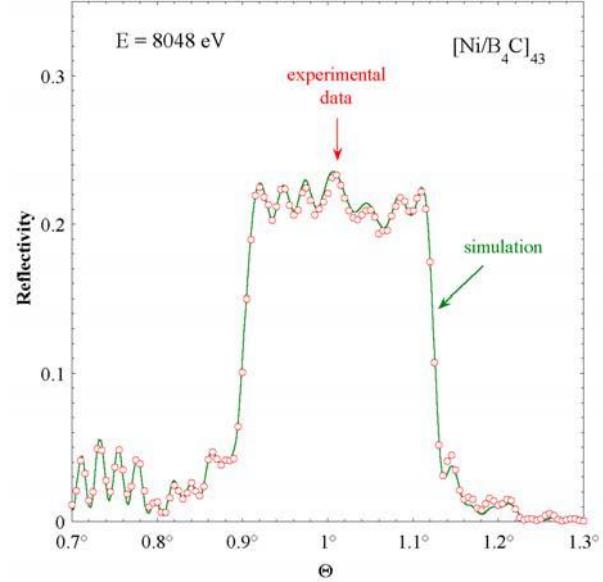
- Ni/B<sub>4</sub>C structure
- R( $\theta$ ) = const over 20% bandwidth

Ch. Morawe et al, Nucl. Instr. and Meth. A 493, 189 (2002)

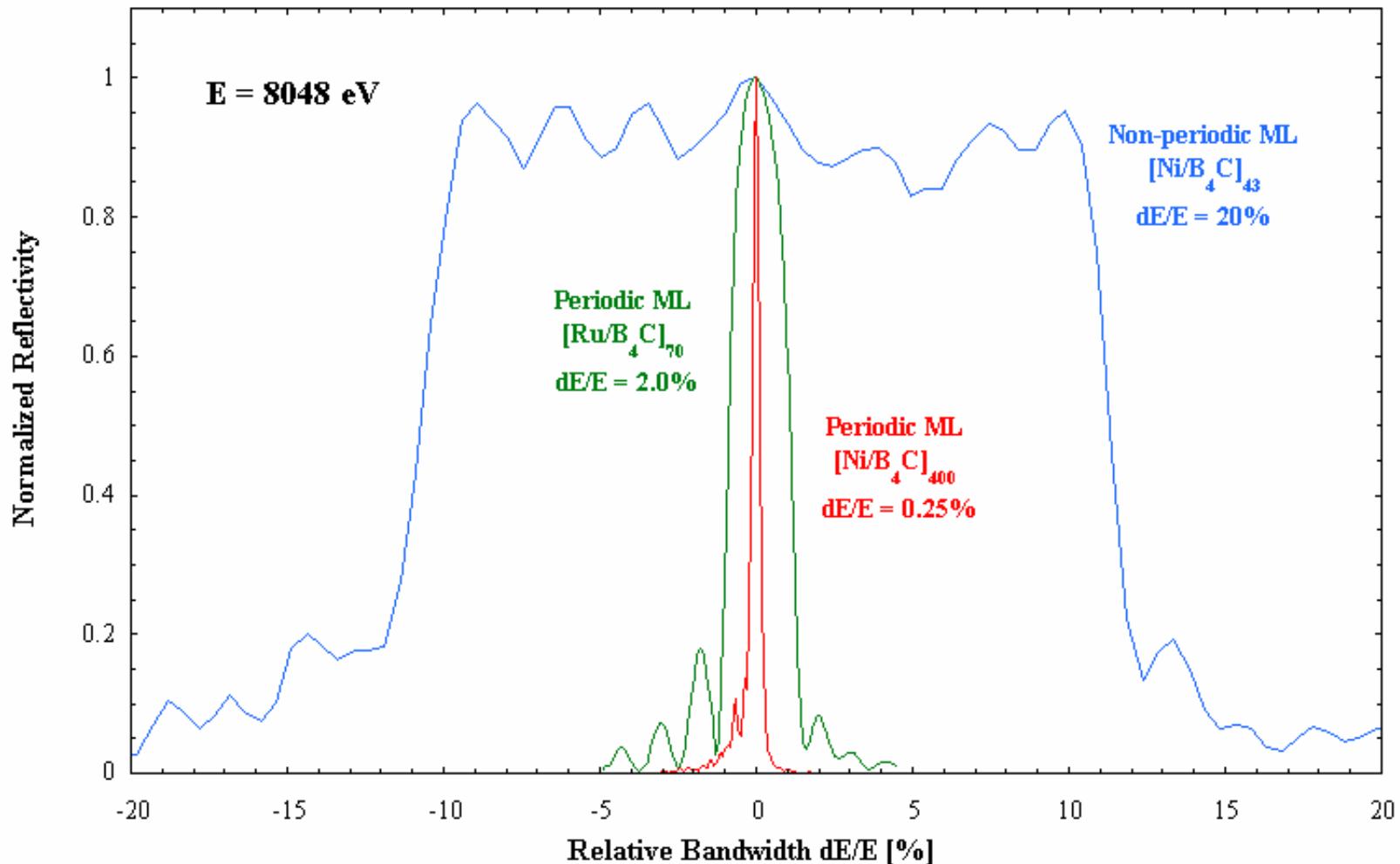
Theoretical design



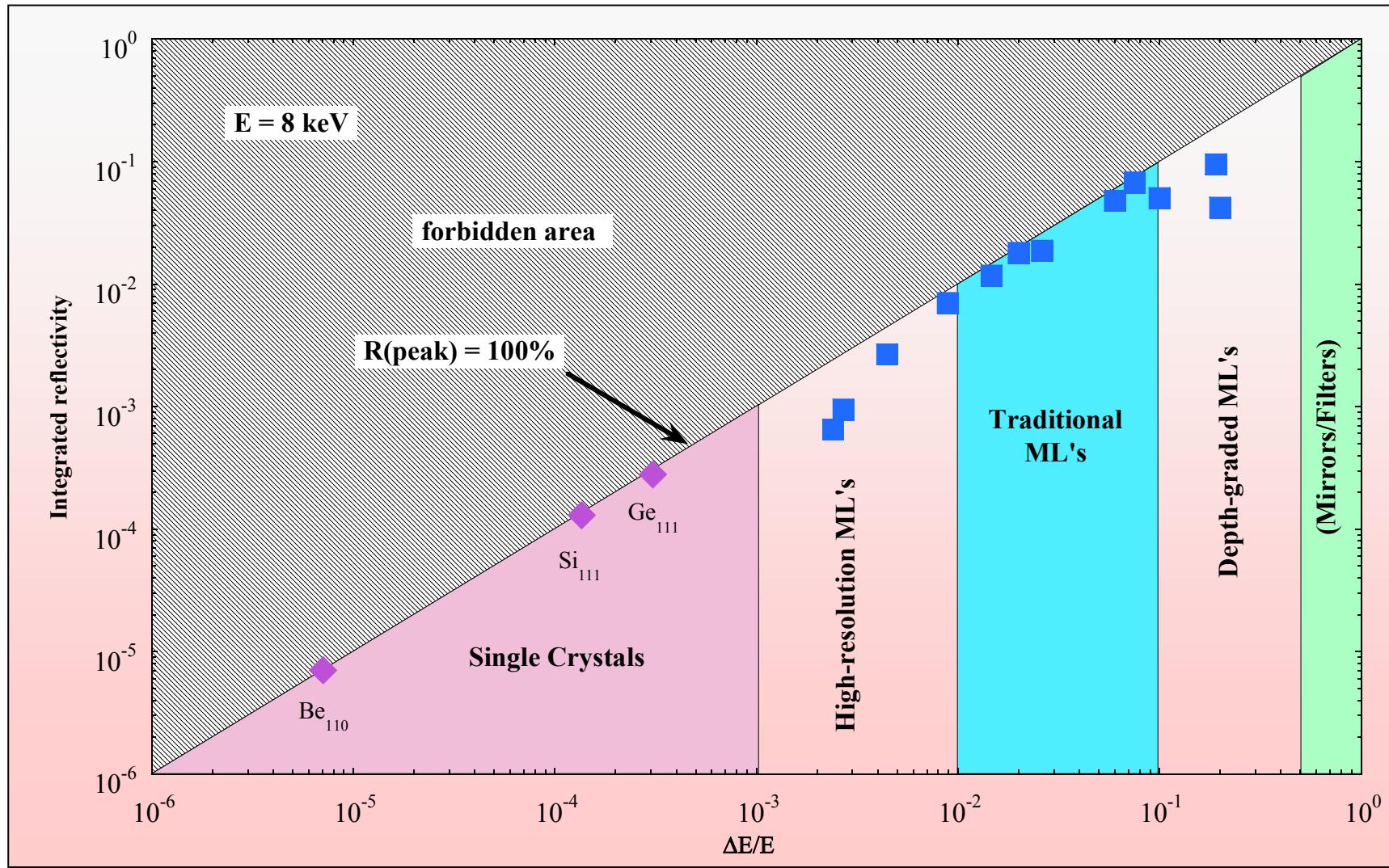
Experimental result



# Multilayer properties



# Multilayer properties



# Multilayer properties

## Energy dispersion:

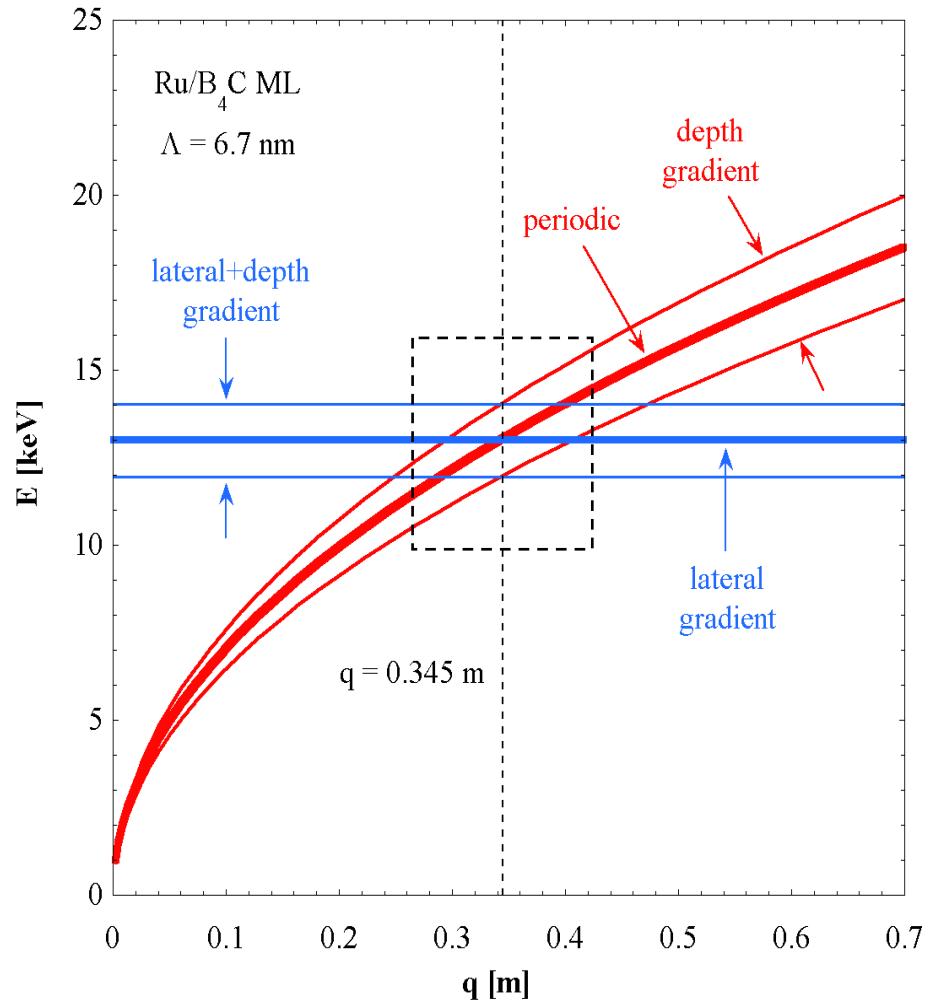
**Bragg equation:**  $E(\theta) = \frac{h \cdot c}{2\Lambda \sqrt{n^2(E) - \cos^2 \theta}}$

**Elliptic mirror:**  $\sin^2 \theta = \frac{b^2}{p \cdot q} \quad p + q = 2 \cdot a$



$$E(q) = \frac{h \cdot c}{2\Lambda \sqrt{n^2(E) - 1 + \frac{b^2}{(2a-q)q}}}$$

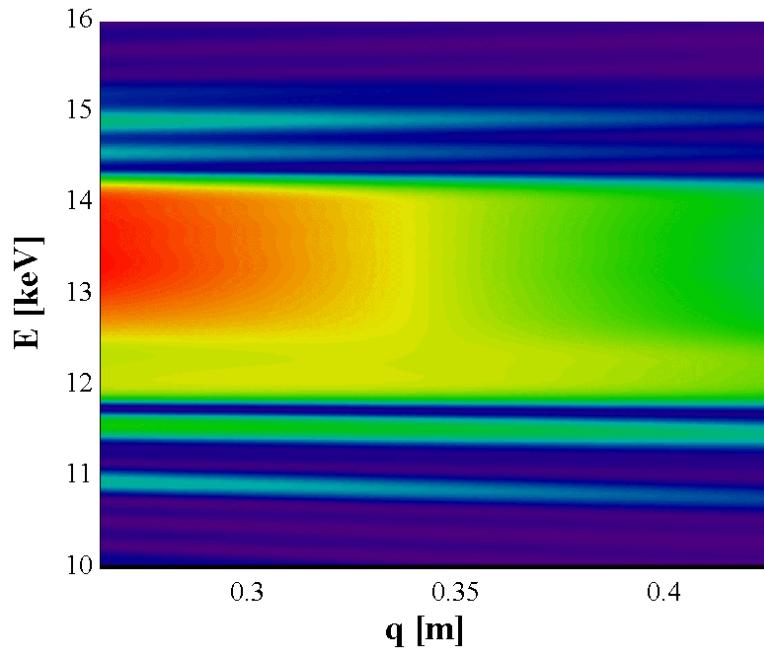
Dispersion “along ML mirror”



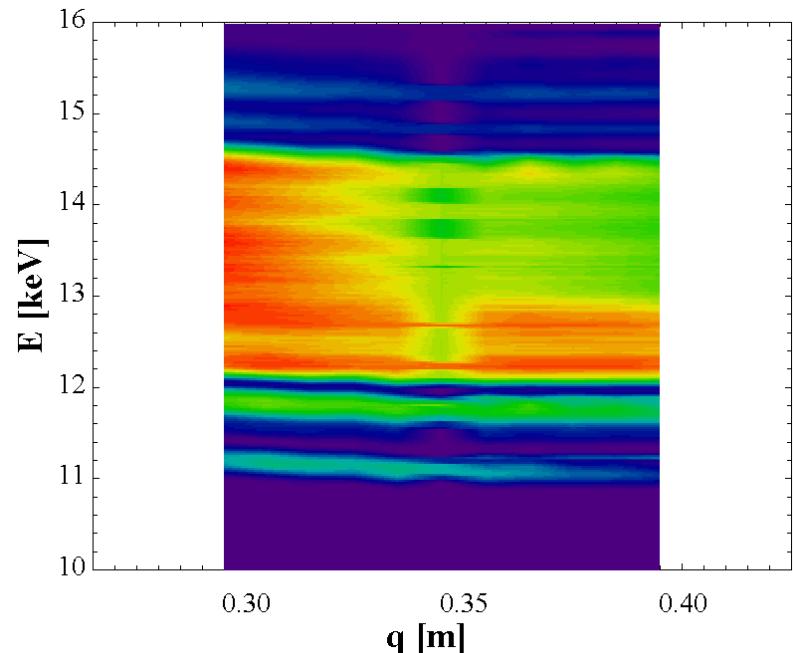
# Multilayer properties

Intensity profiles: (Kirkpatrick-Baez multilayer optics on ESRF BM05)

Theory



Experiment



Ch. Morawe et al, SPIE 5537, 115 (2004)

# Technological options

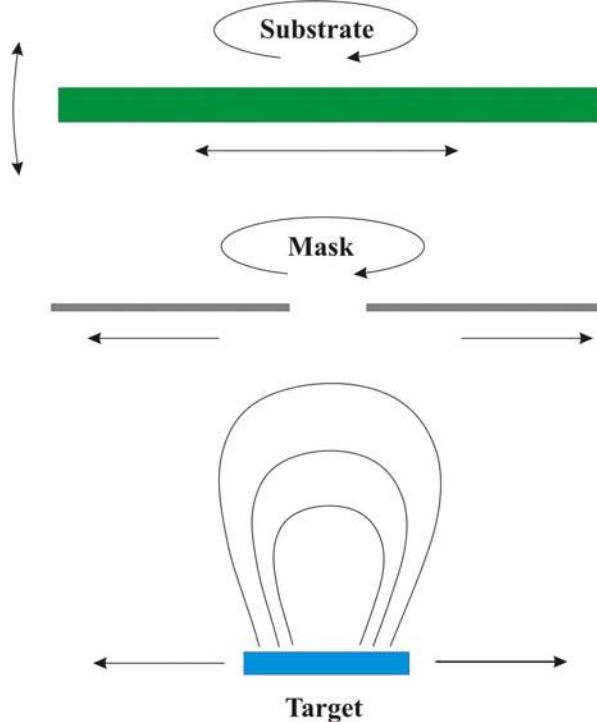
Deposition techniques	Vacuum	Particle energy	Deposition rate	Deposition area
Thermal evaporation	HV (UHV)	Low	Low	Small
E-beam evaporation	UHV	Low	Low	Small
Magnetron sputtering	HV (+Gas)	High	High	Large
DECR sputtering	HV (+Gas)	High	Low	Medium
Ion beam sputtering	UHV (+Gas)	Very high	High	Medium
Pulsed laser deposition	HV	Very high	High	Medium

- Characteristics may vary depending on equipment and application
- Magnetron sputtering most widely used for X-ray multilayer fabrication
- High particle energy favors very thin and uniform layers

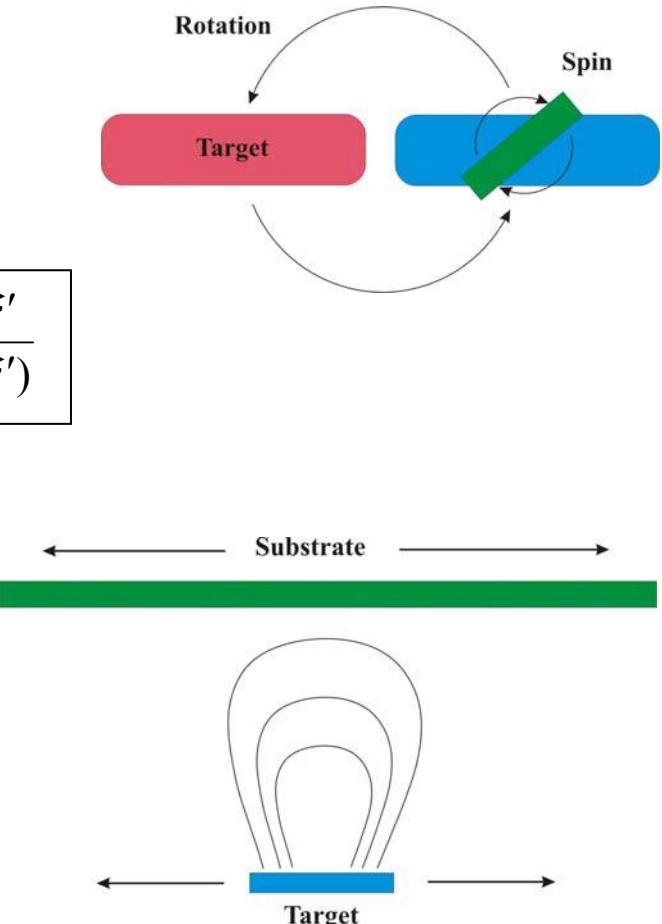
# Technological options

## Large area coatings (uniform, gradient)

- Relative motion source - substrate
- Masking techniques



$$t(\vec{r}) = \int \varphi(\vec{r}, \vec{r}') \frac{d\vec{r}'}{v(\vec{r}')}$$



# Technological options

## Technology and engineering

### Curved MLs

- Figured substrates or bending techniques ?
- Surface finishing (deterministic polishing/etching/coating)

### Stability and stress

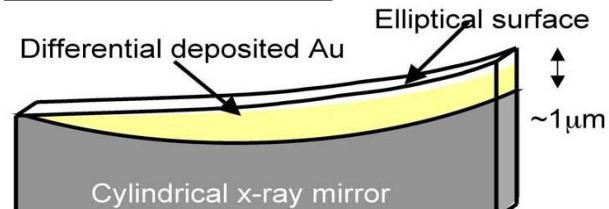
- Intrinsic stress after coating
- Thermal and radiation load (white beam)
- Sample environment (vacuum/He/N<sub>2</sub>)

### Metrology

- Ex-situ techniques reaching limits
- On-line metrology (intensity, phase retrieval)
- Phase correction elements

**Several solutions commercially available!**

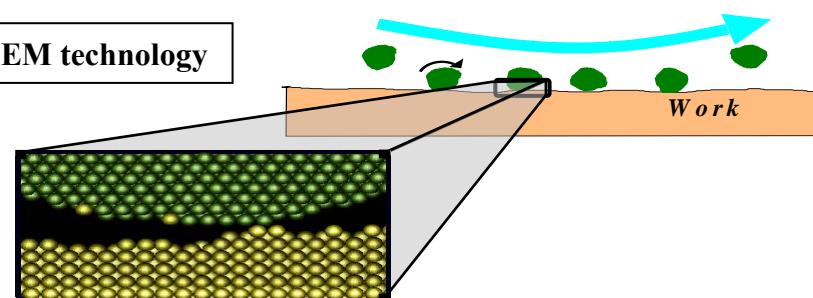
### APS profile coating



### ESRF bender

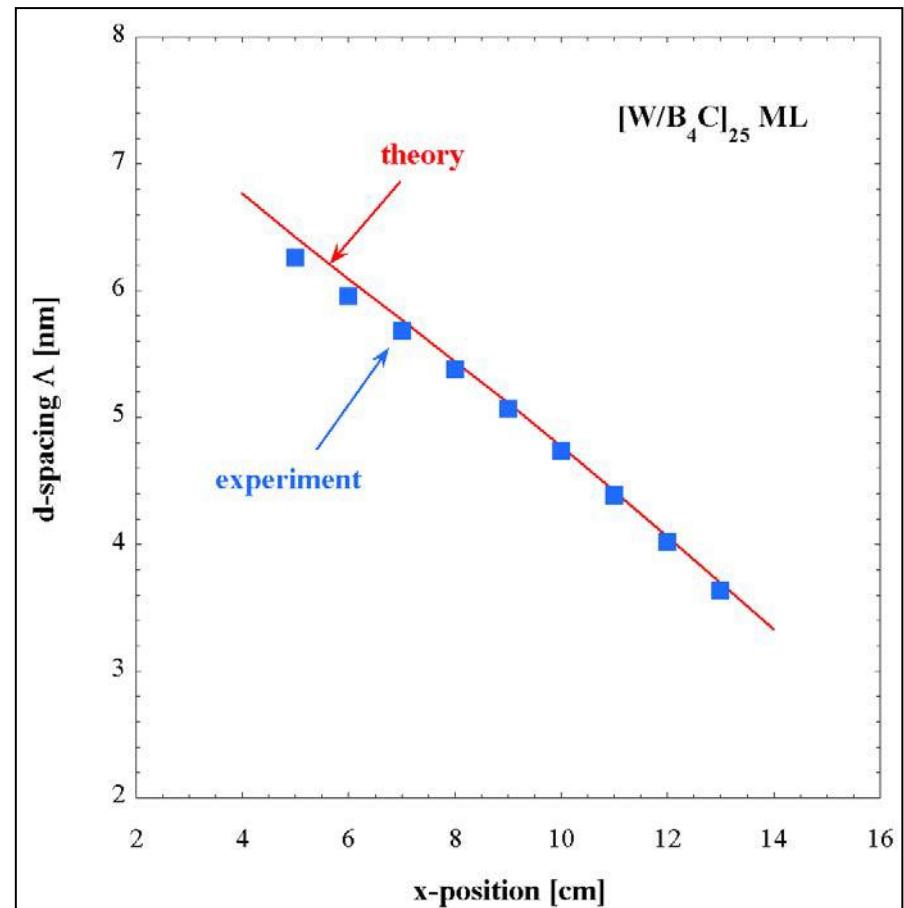
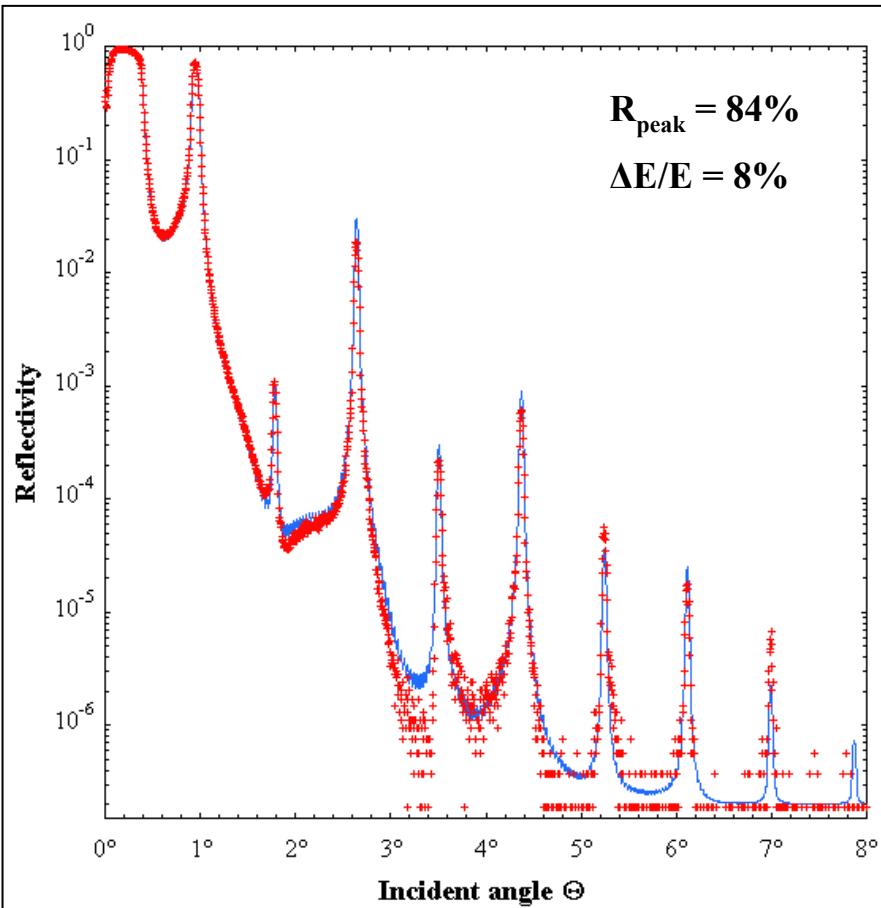


### Osaka EEM technology



# Experimental progress

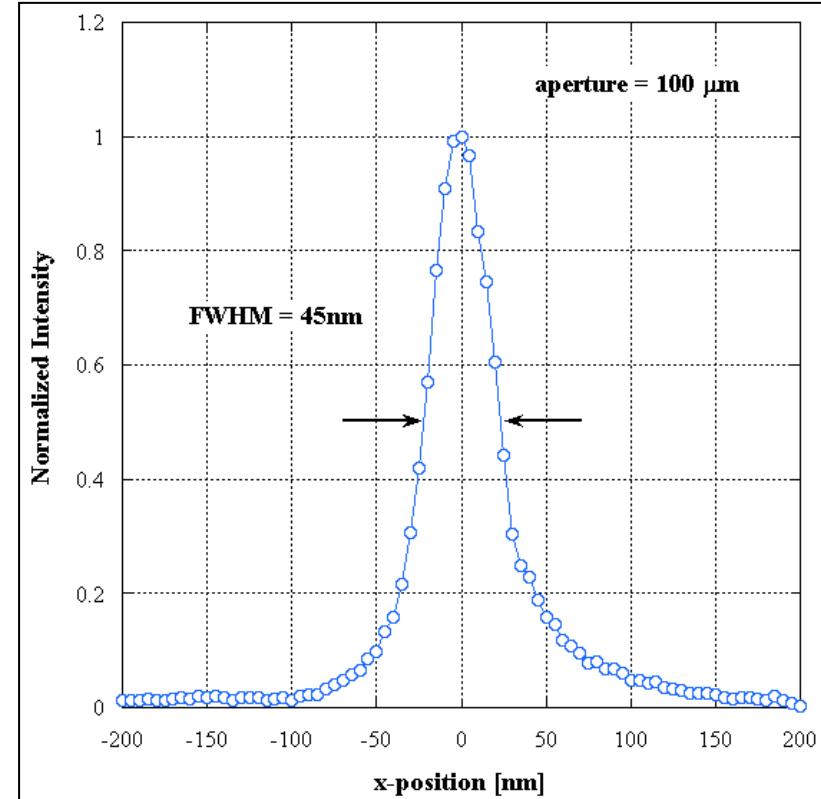
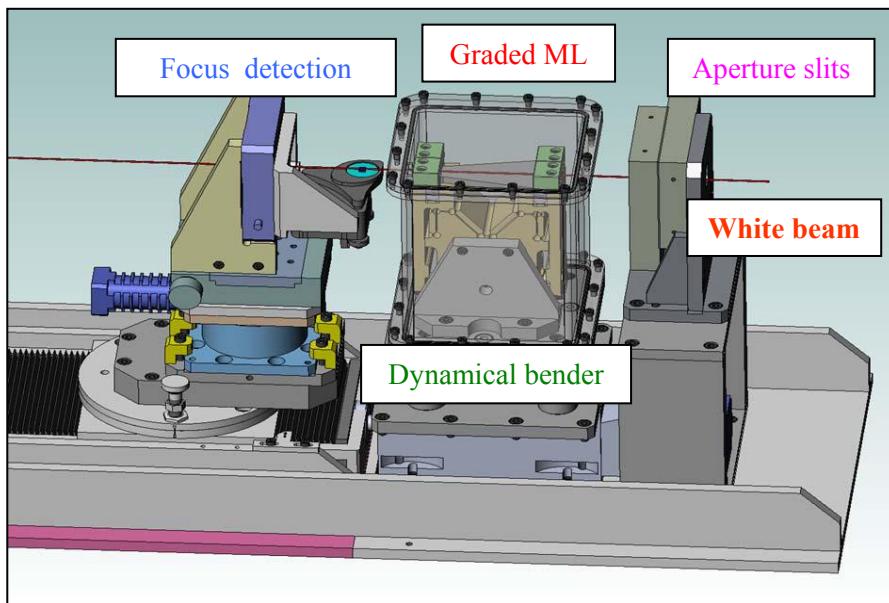
Example:  $[W/B_4C]_{25}$  ML @ 24550 eV



# Experimental progress

## ESRF focusing experiment

- Full undulator spectrum
- $P = 150 \text{ m}$ ,  $Q = 77 \text{ mm}$
- Vertical line focus
- Raw data **45 nm FWHM @ 100 μm aperture**



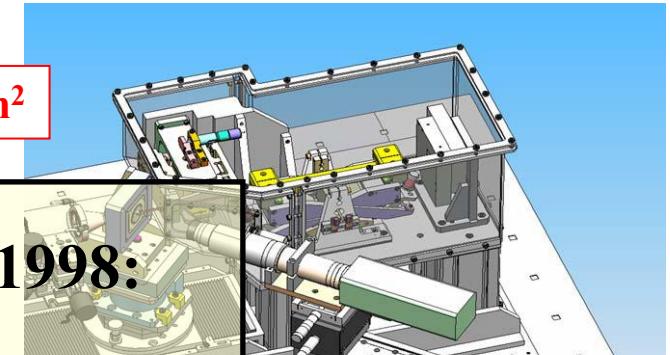
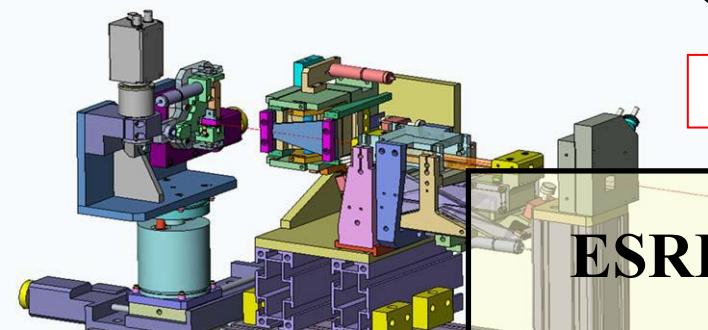
Ch. Morawe et al, Proc. SPIE 6317 (2006)

# Experimental progress

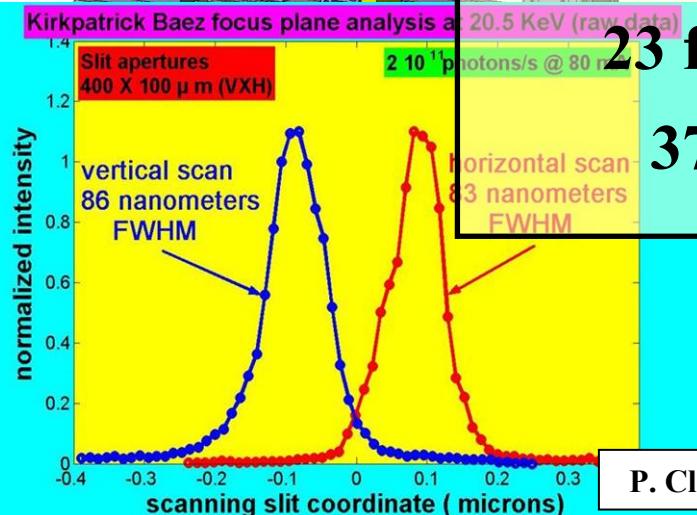
**ID19:** low  $\beta$  @ 150 m, E = 15...24 keV  
 86\*83 nm<sup>2</sup>:  $2 \cdot 10^{11}$  ph/s @ 80mA

**ID22:** high  $\beta$  @ 60 m, slit source, E = 17 keV  
 76\*84 nm<sup>2</sup>:  $10^9$  ph/s @ 200mA  
 150\*100 nm<sup>2</sup>:  $10^{12}$  ph/s @ 200mA

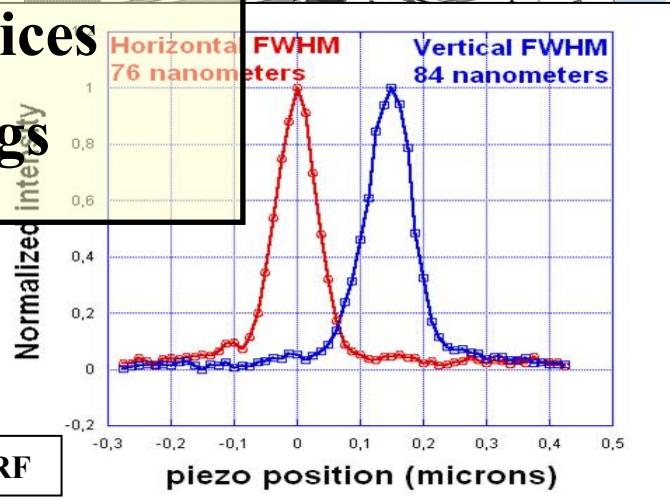
**$3 \cdot 10^5$  ph/s/mA/nm<sup>2</sup>**



**ESRF BLs since 1998:**



**23 focusing devices**  
**37 ML coatings**



# Summary

## ML - KB “Data Sheet”

Energy range	5...100 keV
Peak reflectivity	50...90% (per reflection)
Energy bandpass	0.5...20%
Minimum focal spot size	≈ 5 nm (expected diffraction limit) < 50 nm (proof of feasibility) < 100 nm (routine operation)
Focal distance	50...1000 mm
BL layout	Beam deflection (horizontal + vertical)
Alignment	Pre-alignment + on-line (recommended)
Available technologies	Static (fixed energy) Dynamic (tunable energy)
Principal curved ML developers	ESRF, Univ.Osaka/Spring-8, (APS)
Synchrotron optics (no MLs)	Irelec (France), JTEC (Japan), SESO (France), Xradia (USA), Zeiss (Germany)
Lab optics or coatings only	AXO (Germany), Incoatec (Germany), Osmic/Rigaku (USA), WinlightX (France), Xenocs (France)

# Refractive x-ray lenses for hard x-ray microscopy

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ISG, Research Center Jülich

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Fraunhofer IZM, Chemnitz, Germany



# Hard X-Ray Microscopy & Tomography

## Full-field microscopy:

transmission imaging

contrast generated by attenuation and refraction

large 3D-images of the sample (tomography)

## Scanning microscopy:

scan sample with nanobeam (< 100 nm lateral size)

different contrasts:

fluorescence

absorption (XAS)

diffraction (SAXS, WAXS, CXDI)

...

scanning: relatively slow

tomography: local inner structure of sample



K

# Optics for Hard X-Rays

Full-field microscopy:

- objective lens for imaging free of aberrations
- condensor lens to concentrate x-rays on sample

Scanning microscopy:

- generate an intensive x-ray microbeam

Variety of x-ray optics available today:

- Fresnel zone plates and multilayer Laue lenses

- refractive lenses [Snigrev, et al., Nature **384**, 49 (1996)]**

- curved/bent mirrors and multilayers

- capillaries

- wave guides (mode filter)

- crystal optics

...

# Refraction

$$n = 1 - \delta + i\beta, \quad \delta > 0$$

Vacuum optically denser than matter!

$$\delta = \frac{1}{2\pi} N_A r_0 \lambda^2 \rho \frac{Z + f'}{A}$$

specific refraction:

independent of material  
(away from absorption edges)

very weak

## Absorption

$$n = 1 - \delta + i\beta, \quad \delta > 0$$

Lambert-Beer Law:

$$I(x) = I_0 e^{-\mu x}$$

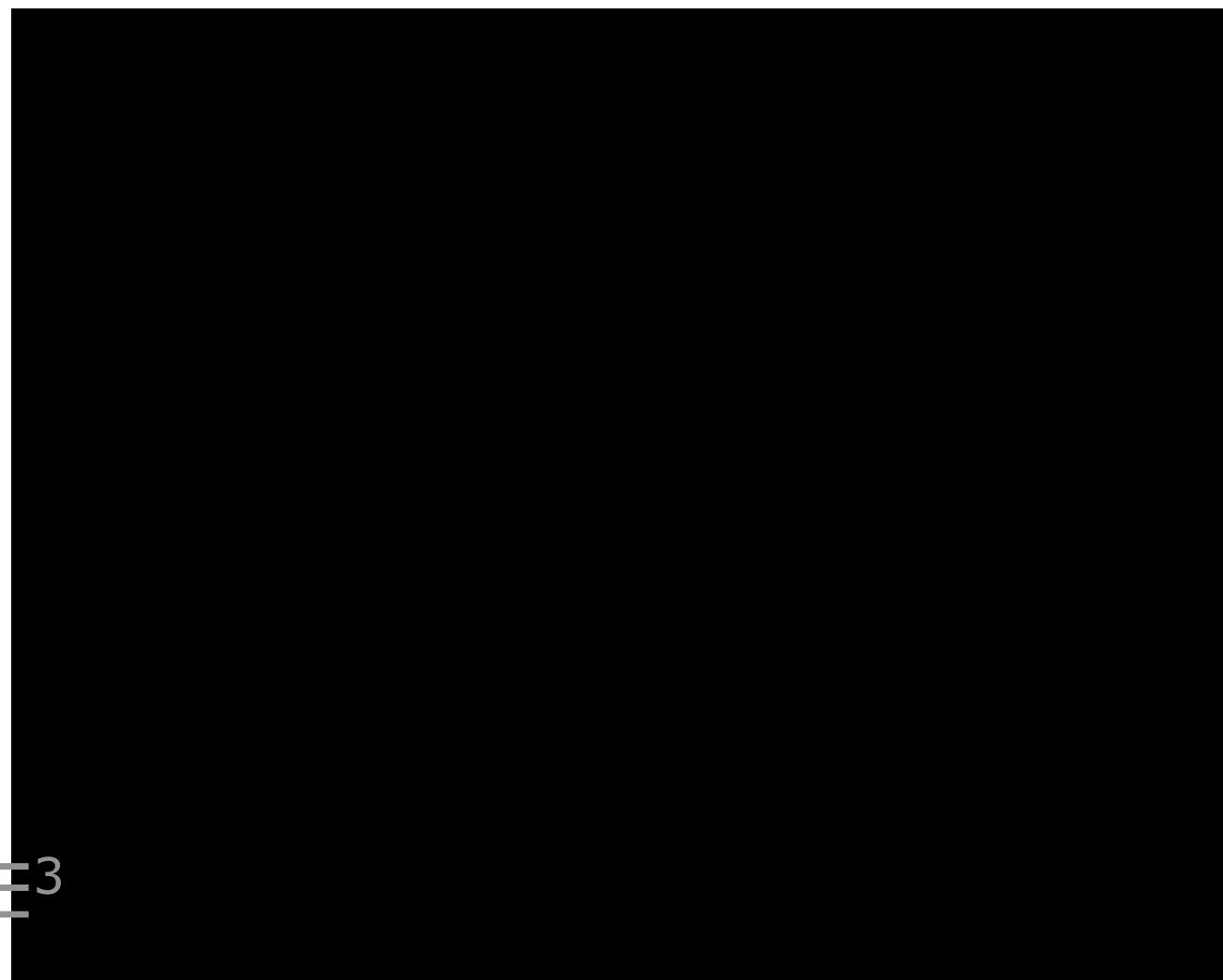
attenuation coefficient  $\mu$ :

$$\mu = \frac{4\pi\beta}{\lambda}$$

2 main contributions:

photo absorption  $\tau \sim Z^3/E^3$

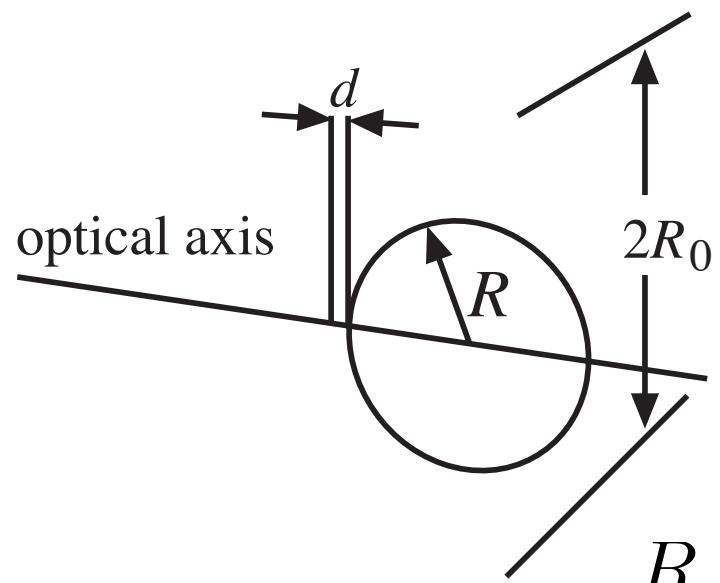
Compton scattering  $\mu_c$



For comparison:  $\mu_{\text{glas}} = 10^{-7} \text{ cm}^{-1}$   
for visible light

# Refractive X-Ray Lenses

single lens



stack of lenses:  
compound refractive lens (CRL)

$$R = 50 \text{ } \mu\text{m} - 1000 \text{ } \mu\text{m}$$

$$d = 10 \text{ } \mu\text{m} - 30 \text{ } \mu\text{m}$$

$$2R_0 = 450 \text{ } \mu\text{m} - 1000 \text{ } \mu\text{m}$$

variable number of lenses:  $N = 10 \dots 300$

parabolic profile: no spherical aberration

→ true imaging optic

---

# Parabolic Refractive X-Ray Lenses

Bruno Lengeler  
RWTH Aachen

# Full-Field Imaging

lenses used as  
objective lens in full  
field microscope

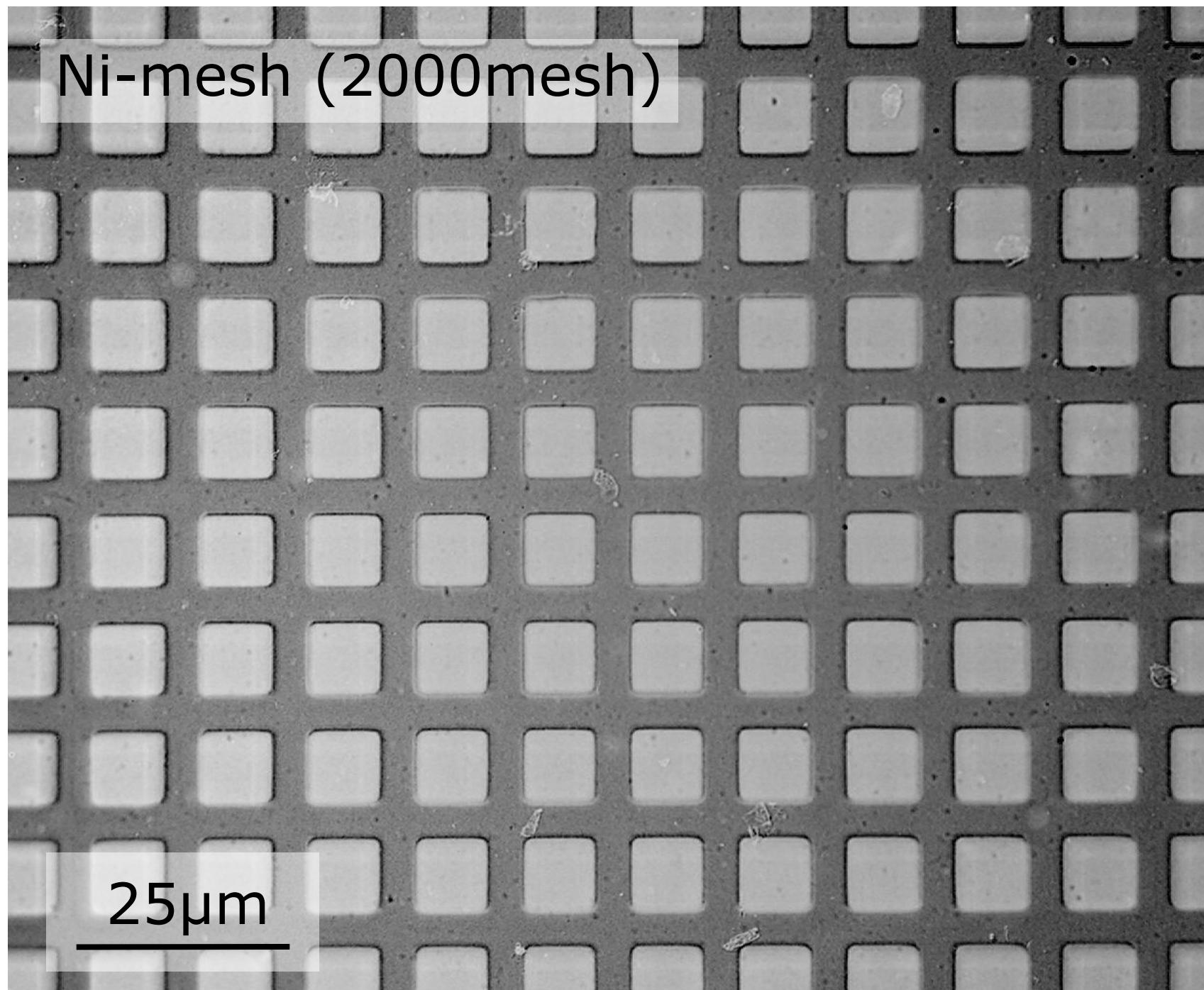
image distance

$$L_2 = \frac{L}{L_1}$$

numerical aperture

$$NA = \frac{D}{2}$$

# Full-Field Imaging



For comparison:  
spherical lens

(simulation)

imaging parameters:

$$E = 12\text{keV}$$

$$N = 91 \text{ (Be)}$$

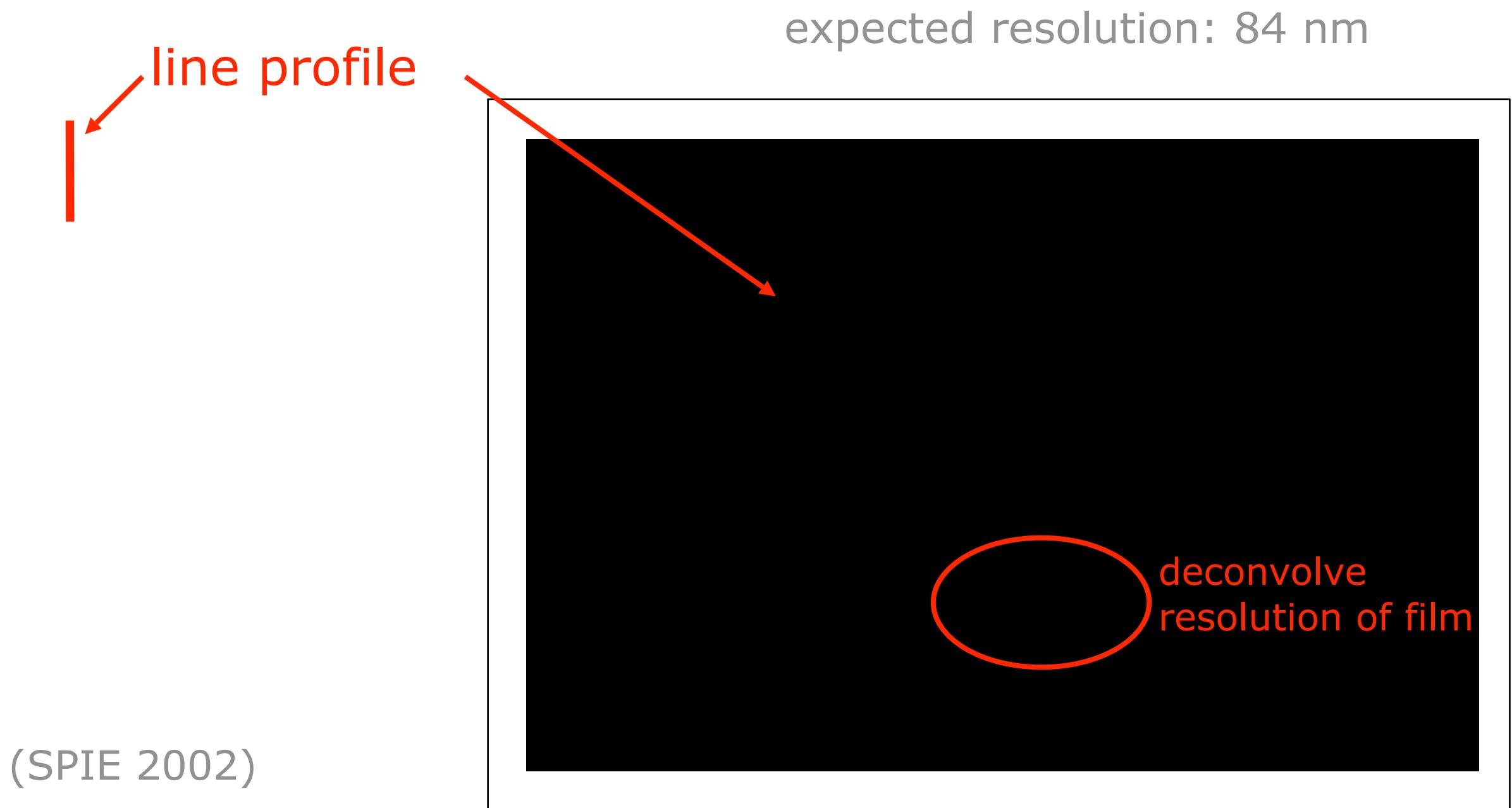
$$f = 495 \text{ mm}$$

$$m = 10x$$

spatial resolution:

$$\sim 100 \text{ nm}$$

## Full-Field Imaging: Spatial Resolution



→ resolution of x-ray optical setup:  $105 \text{ nm} \pm 30 \text{ nm}$

# Hard X-Ray Microbeam

source

Focus size and shape determined by:

source size  
magnification  $L_2/L_1$   
diffraction limit  
aberrations

$L_1$

lens

Flux in focus determined by:

brilliance

source size

focusing cross-section of lens

$$L_2 = \frac{L_1 f}{L_1 - f}$$

microbeam  
on sample

High brilliance:

High flux per phase space  
volume

ERL



Ideal for nanobeams:

small source:

small geometric image  
(diffraction limited focusing)

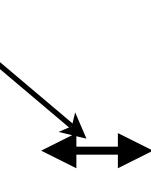
small divergence:

optic captures large fraction  
of emitted radiation

## Be-Lens with $R = 50\mu\text{m}$ : Microbeam

vertical focus

200nm



ESRF ID10

$E = 8 \text{ keV}$

$N = 31$

$L_1 = 60.8 \text{ m}$

$f = 156 \text{ mm}$

gain  $\sim 10^5$

flux:  $3 \cdot 10^{11} \text{ ph/s}$

mono: Si 111

expected focus size: 170 nm

horiz focus:  $1.14 \mu\text{m}$   
(horizontal slits at 0.3mm gap)

**focus source size and stability limited!**

# Rotationally Parabolic Refractive X-Ray Lenses

State-of-art (Be, Al):

$R = 50 \mu\text{m}$  [tested for focusing  $< 200 \text{ nm}$  (source size limited)]

$R = 200 \mu\text{m}$  [tested for full field imaging with  $\sim 100 \text{ nm}$  resolution]

$R = 300 \mu\text{m}, 500\mu\text{m},$  and  $1000\mu\text{m}$  [not tested, yet]

Lenses with  $R = 1500 \mu\text{m}$  under development

Energy range: 5 - 150 keV and higher

Application:

hard x-ray full-field microscope (tomography)

microbeam analysis, e. g., micro-fluorescence, XANES, SAXS  
also in tomography

coherent (micro-)diffraction

beam conditioning (moderate focusing, collimation)  
(white beam compatible)

→ Optics for X-FEL

## Microprobe Example: SAXS-Tomography

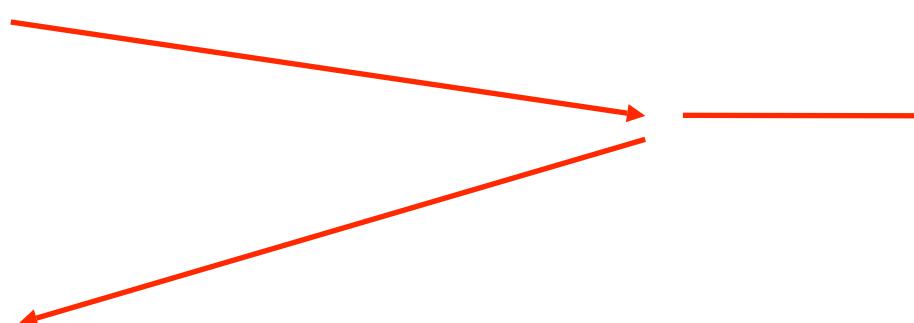
Probe nanoscale structure on a virtual section through  
a sample

Sample:

nondestructive probe of the  
interior of sample

define virtual slice

obtain SAXS cross  
section at each location  
on section



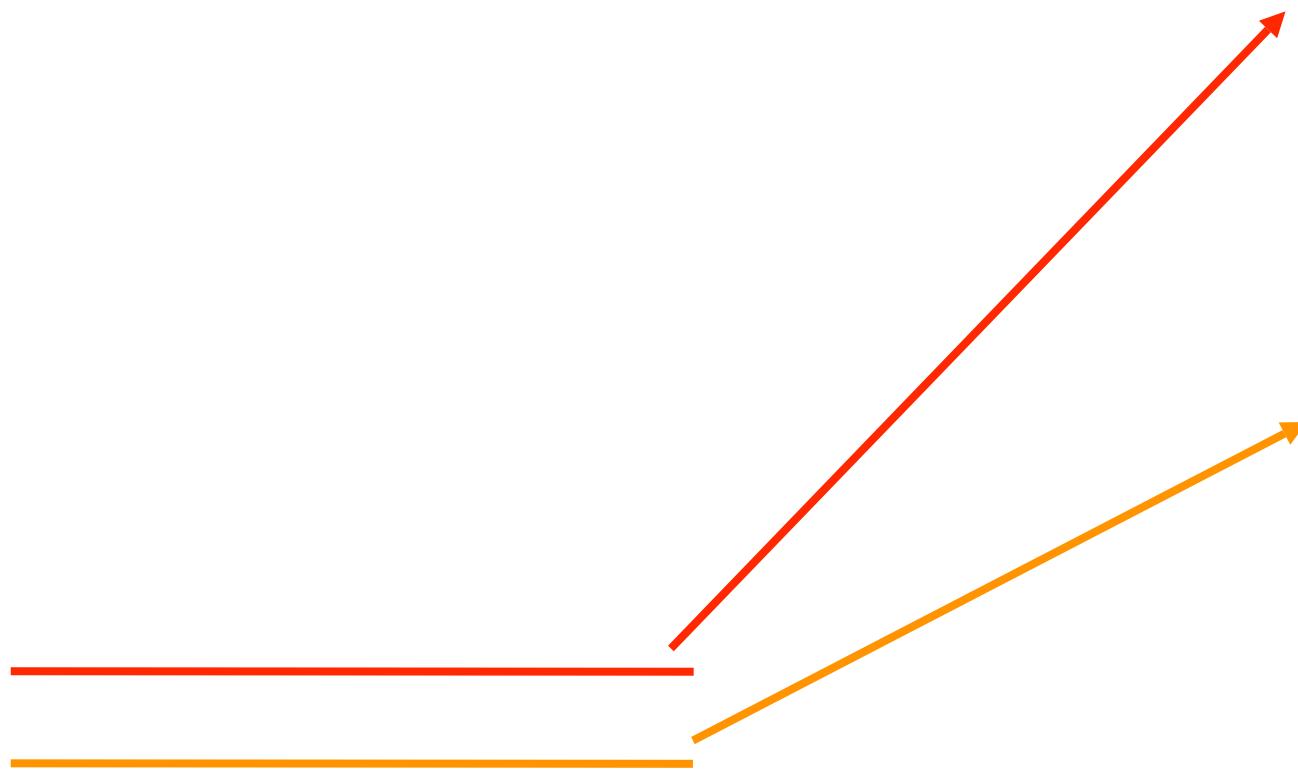
injection molded PE

Collab.: N. Stribeck, Univ. Hamburg

APL **88**, 164102 (2006)

# SAXS-Tomography

$$I_{\vec{q}}(r)$$

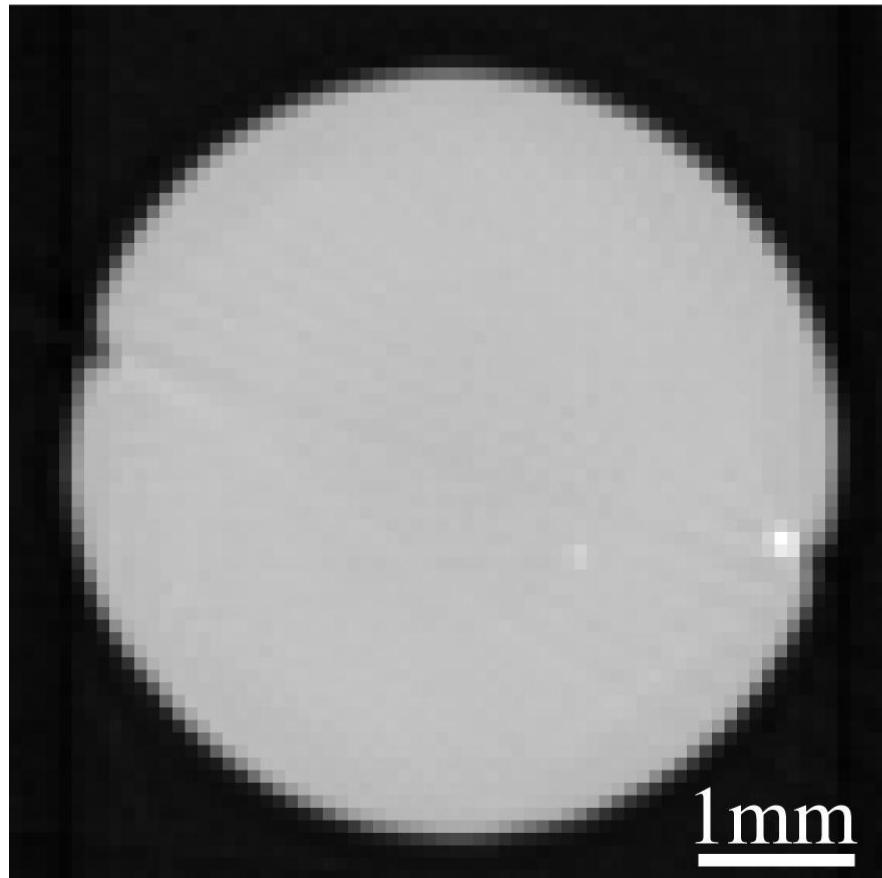


101 projections with  
70 steps each  
80 $\mu$ m step size

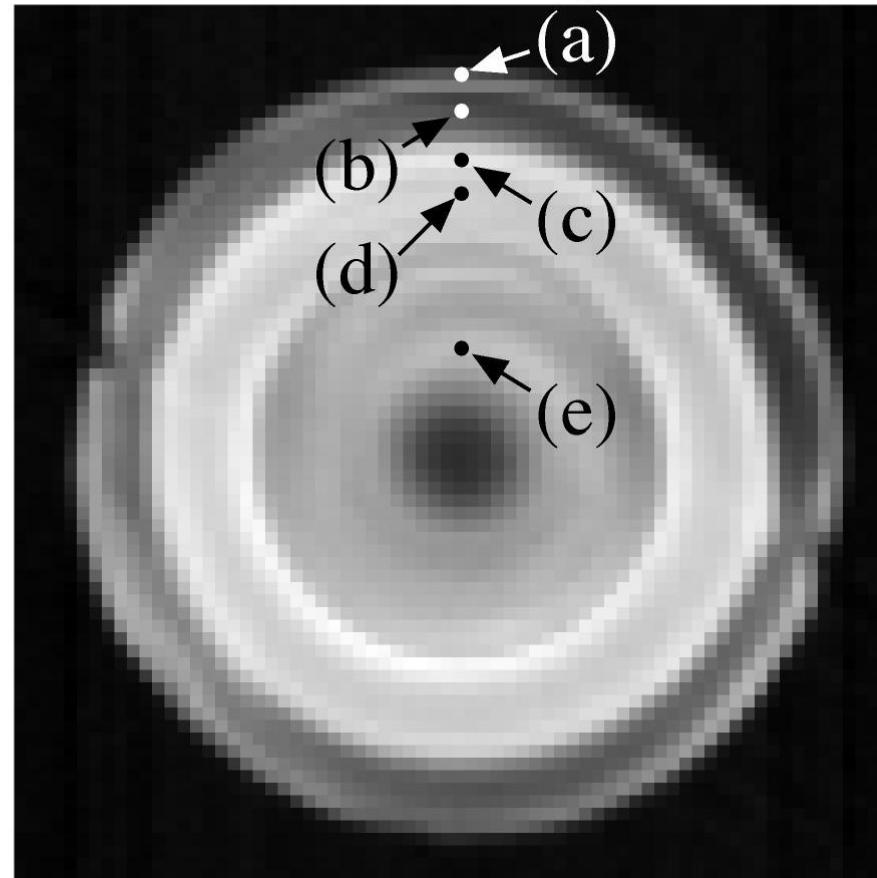
# SAXS-Tomography

Reconstruction:

attenuation

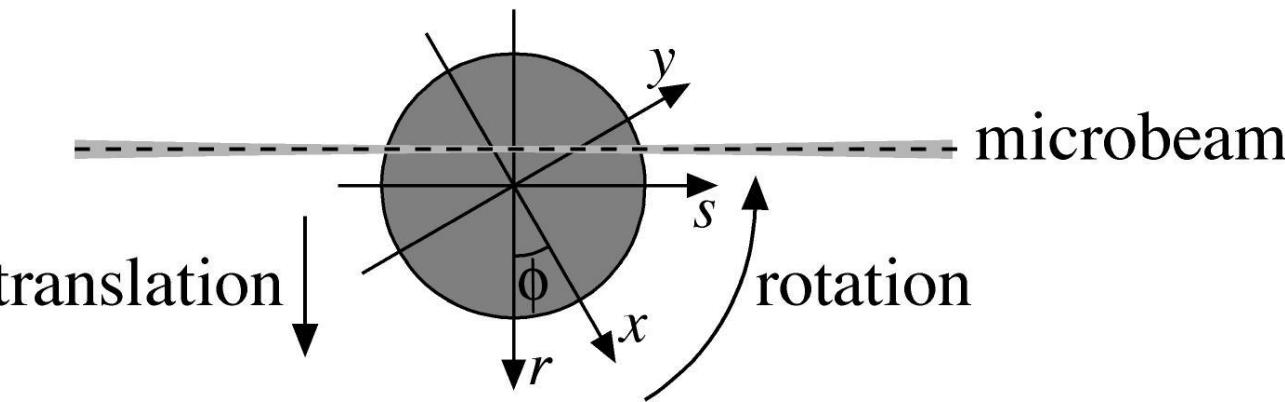


diffraction



integral  
scattering  
along rotation  
axis

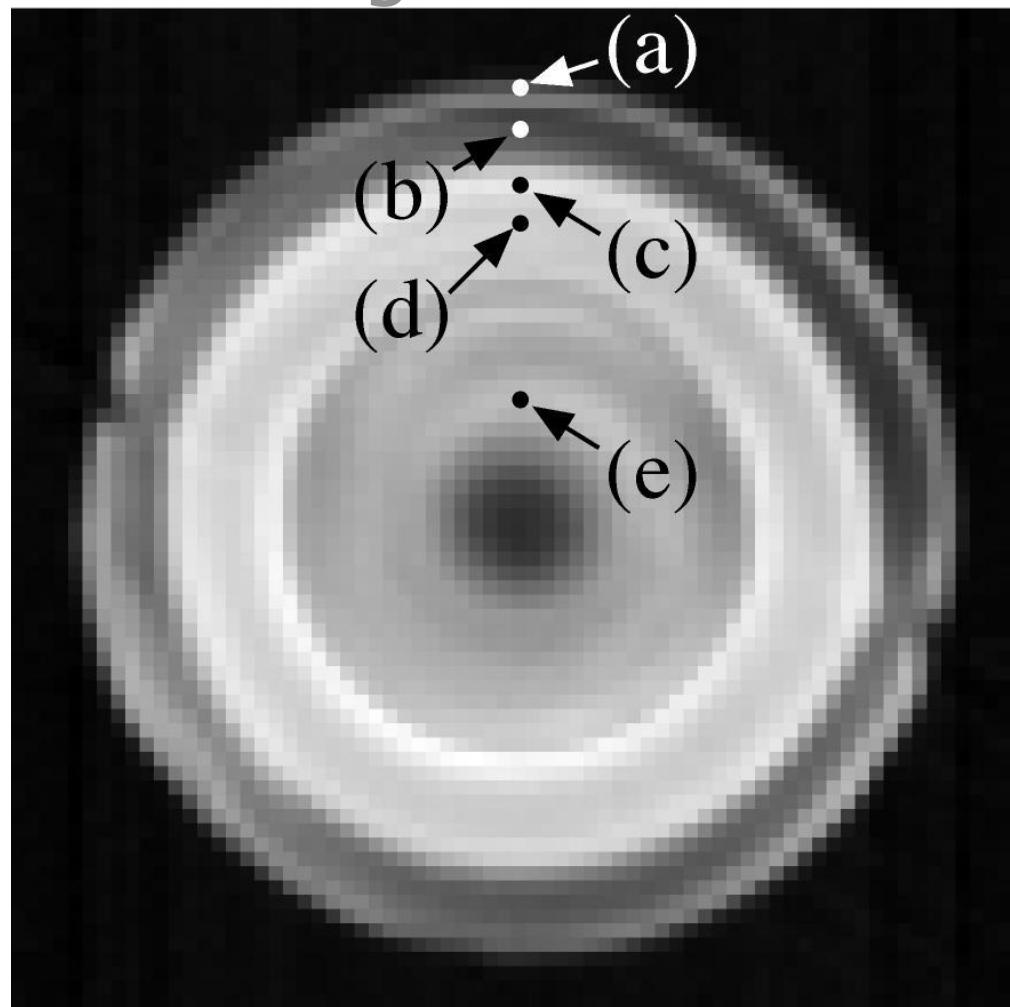
$$q_r = 0$$



# SAXS-Tomography

Sample is fibre textured:

scattering cross section



scattering cross section

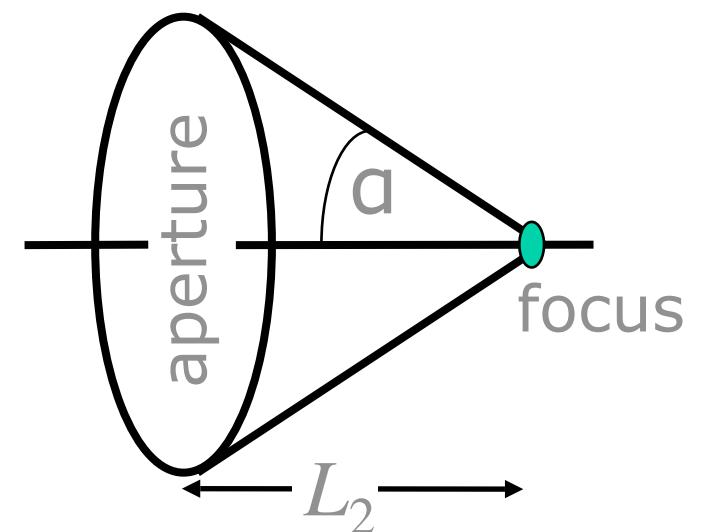
inhomogeneous  
nanostructure

In each pixel:  
full scattering  
cross section  
(rotationally  
symmetric)

interpretation:  
Stribeck, et al.  
Macromol. Chem.  
Phys. 207, 1139 (2006)

# Effective Aperture and Diffraction Limit

Numerical aperture:



$D_{\text{eff}}$  limited by:

geometric aperture  $2R_0$

attenuation inside lens material  
(includes Compton scattering)

→ low  $Z$  lens material

$$NA = \sin \alpha = \frac{D_{\text{eff}}}{2L_2}$$

Diffraction limit:

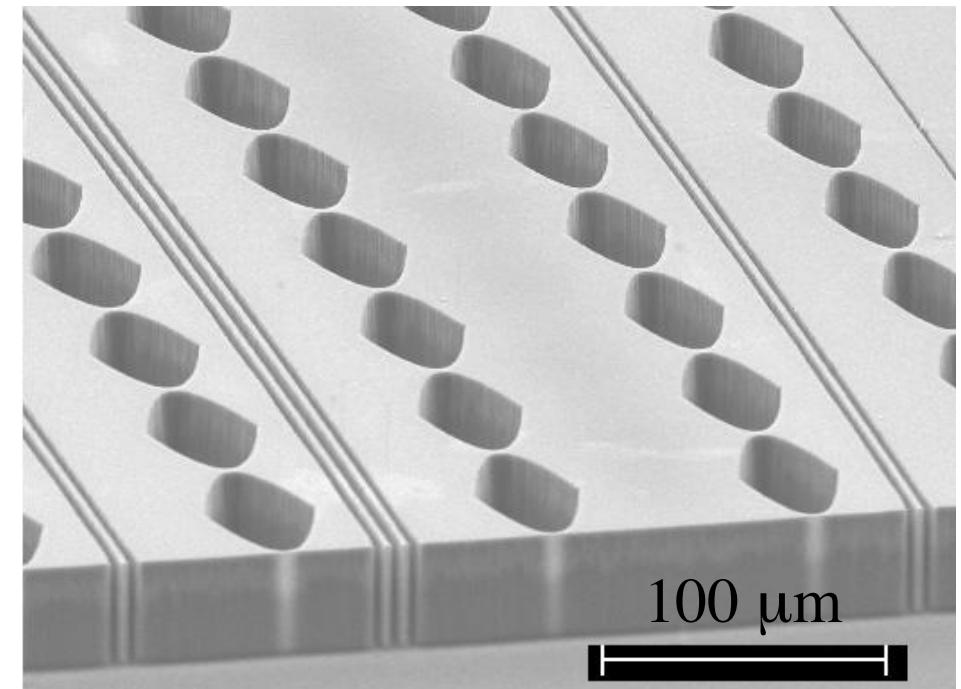
$$d_t = 0.75 \cdot \frac{\lambda}{2NA}$$

## Numerical Aperture

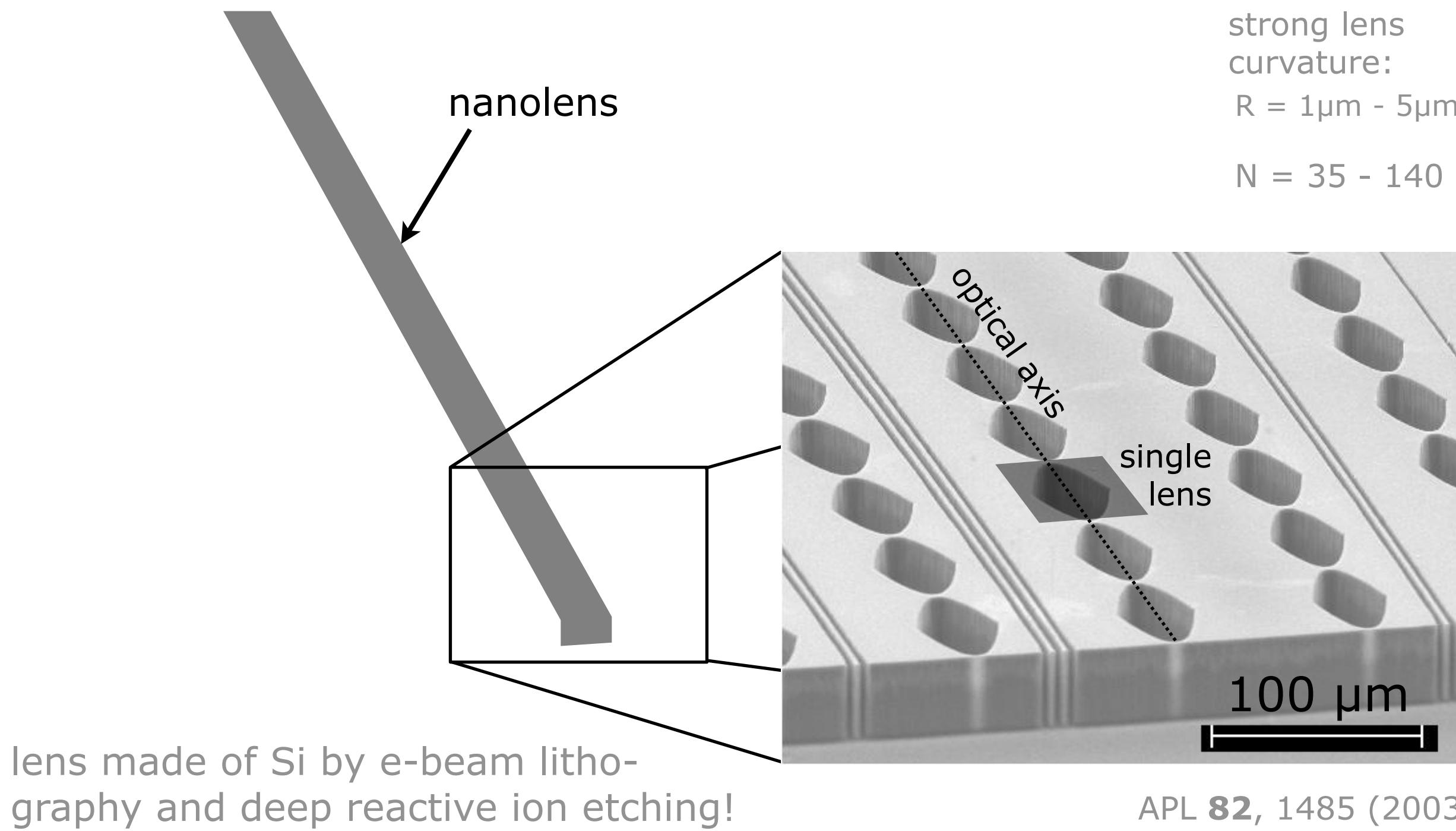
large  $f$ : aperture dominated by attenuation

$$D_{\text{eff}} = 4 \sqrt{\frac{f\delta}{\mu}} \propto \sqrt{f}$$

- reduce  $\mu/\delta$  (low  $Z$  lens material)
- $NA = D_{\text{eff}}/2f \propto 1/\sqrt{f}$ : reduce focal size to minimum

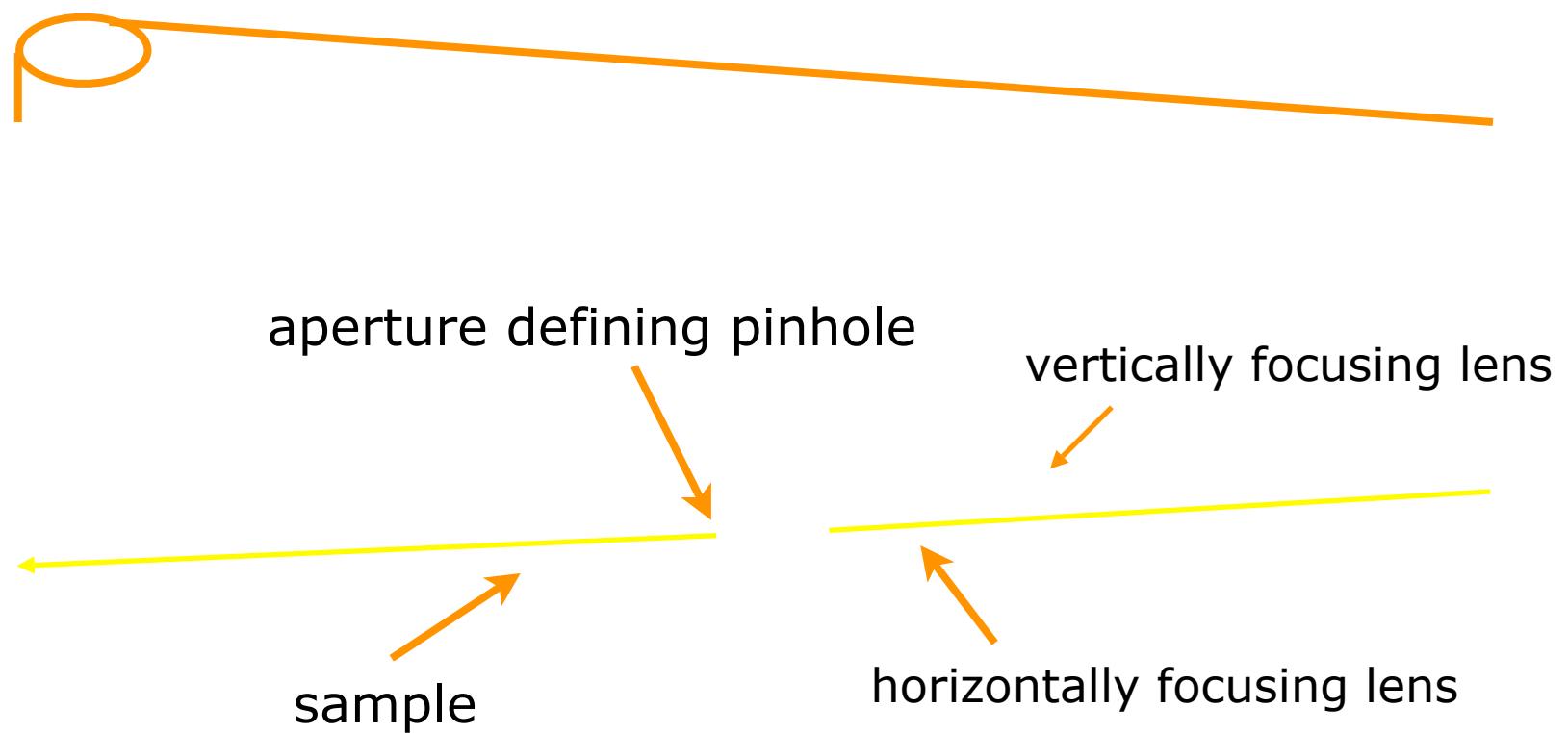


# Nanofocusing Lenses (NFLs)



# Crossed Nanofocusing Lenses

Setup at ID13 of ESRF



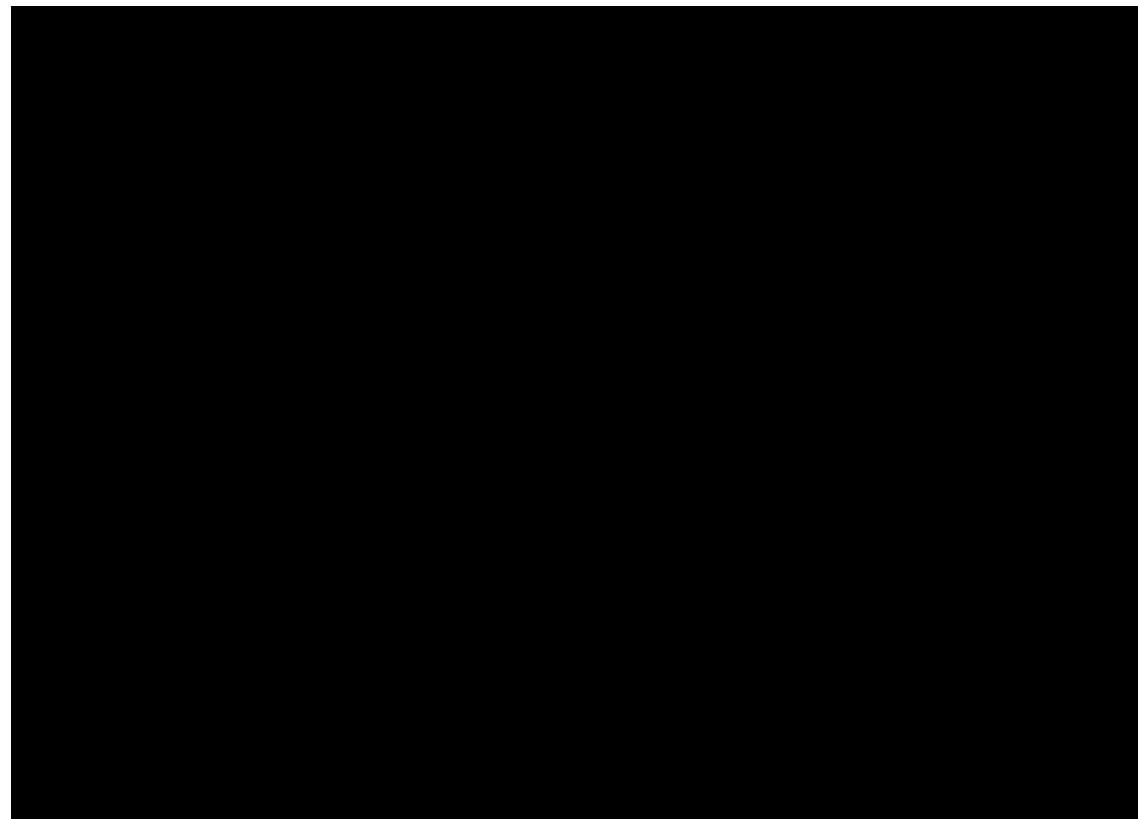
# Focusing with NFLs

Si lens:  $E = 21\text{keV}$ ,  $L_1 = 47\text{m}$

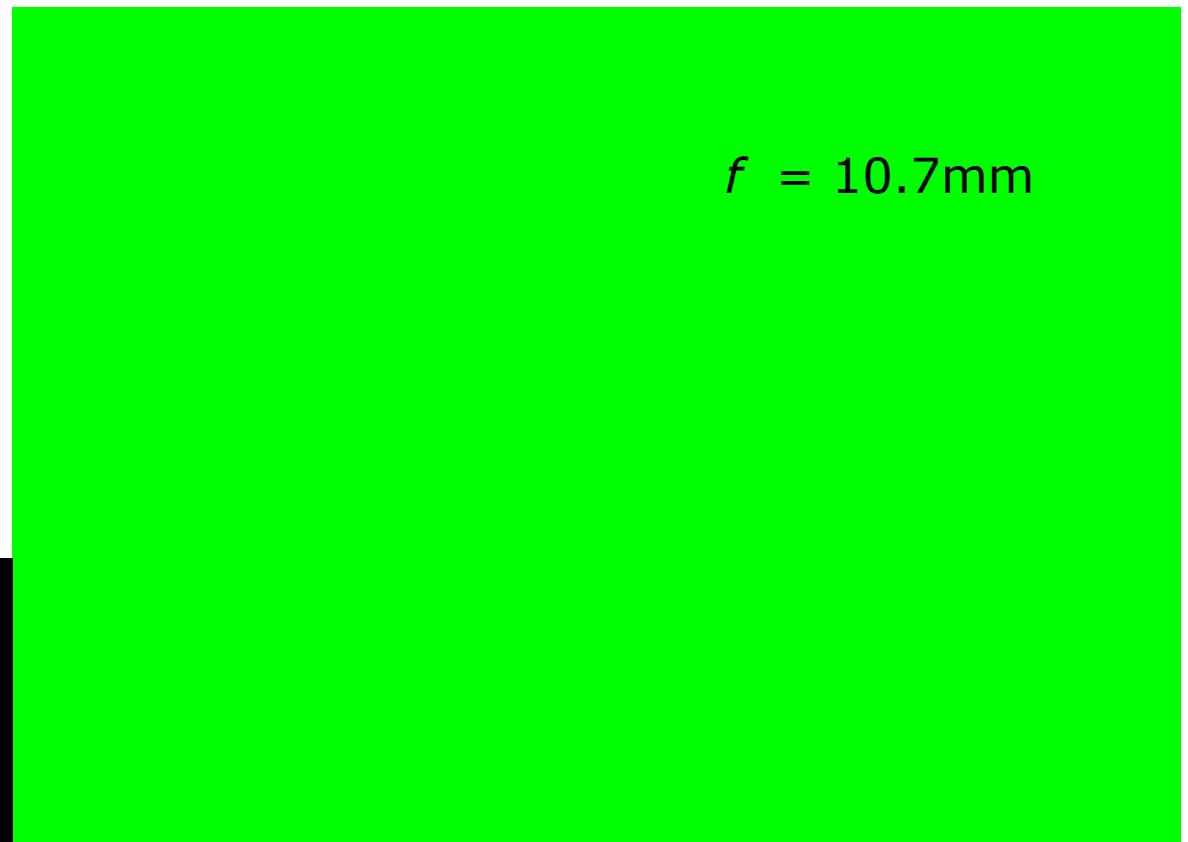
source:  
ID13 low- $\beta$  invac. undulator

source size:  $150 \times 60\mu\text{m}^2$

vertical focus: 55nm



horizontal focus: 47nm



demagnification:  
 $\sim 2400 \times 4400$

flux:  $1.7 \cdot 10^8\text{ph/s}$

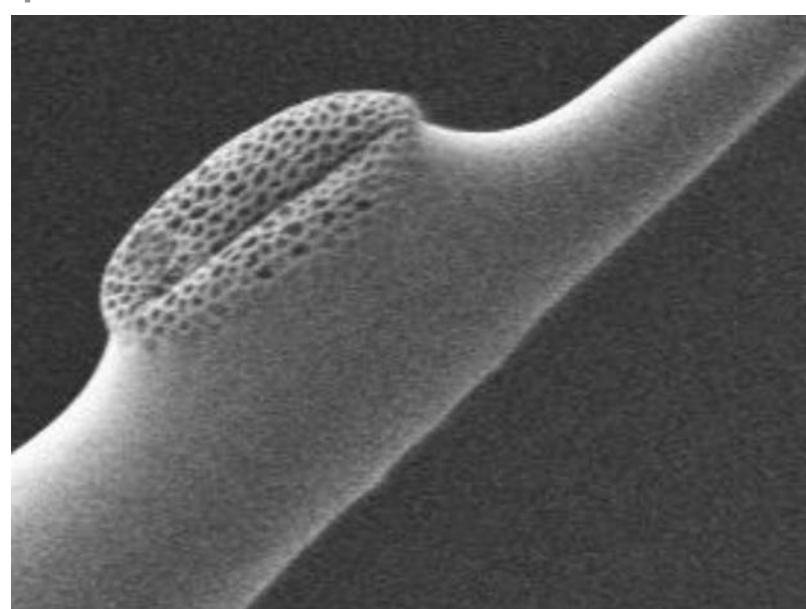
APL **87**, 124103 (2005)

## 2D Scanning Mode: X-Ray Fluorescence

*Arabidopsis thaliana*

Fluorescence map

pollen



~ 100 nm resolution  
 $E = 15.25 \text{ keV}$

# High-Resolution Fluorescence Microtomography

*Arabidopsis thaliana*

trichome (leaf hair)



200µm

tip of trichome  
(freeze dried)

Energy:  
24.3keV

focus size:  
80nm x 120nm

pixel size:  
100nm

# Nano-Diffraction

User experiment at ID13 carried out with prototype (Feb 2008)

M. Hanke, et al., APL **92**, 193109 (2008)

Scan single SiGe/Si(001)-islands

- (a) Ge fluorescence
- (b) light micrograph

Beam parameters:

$E = 15.25 \text{ keV}$

beam size:  $200 \times 200 \text{ nm}^2$

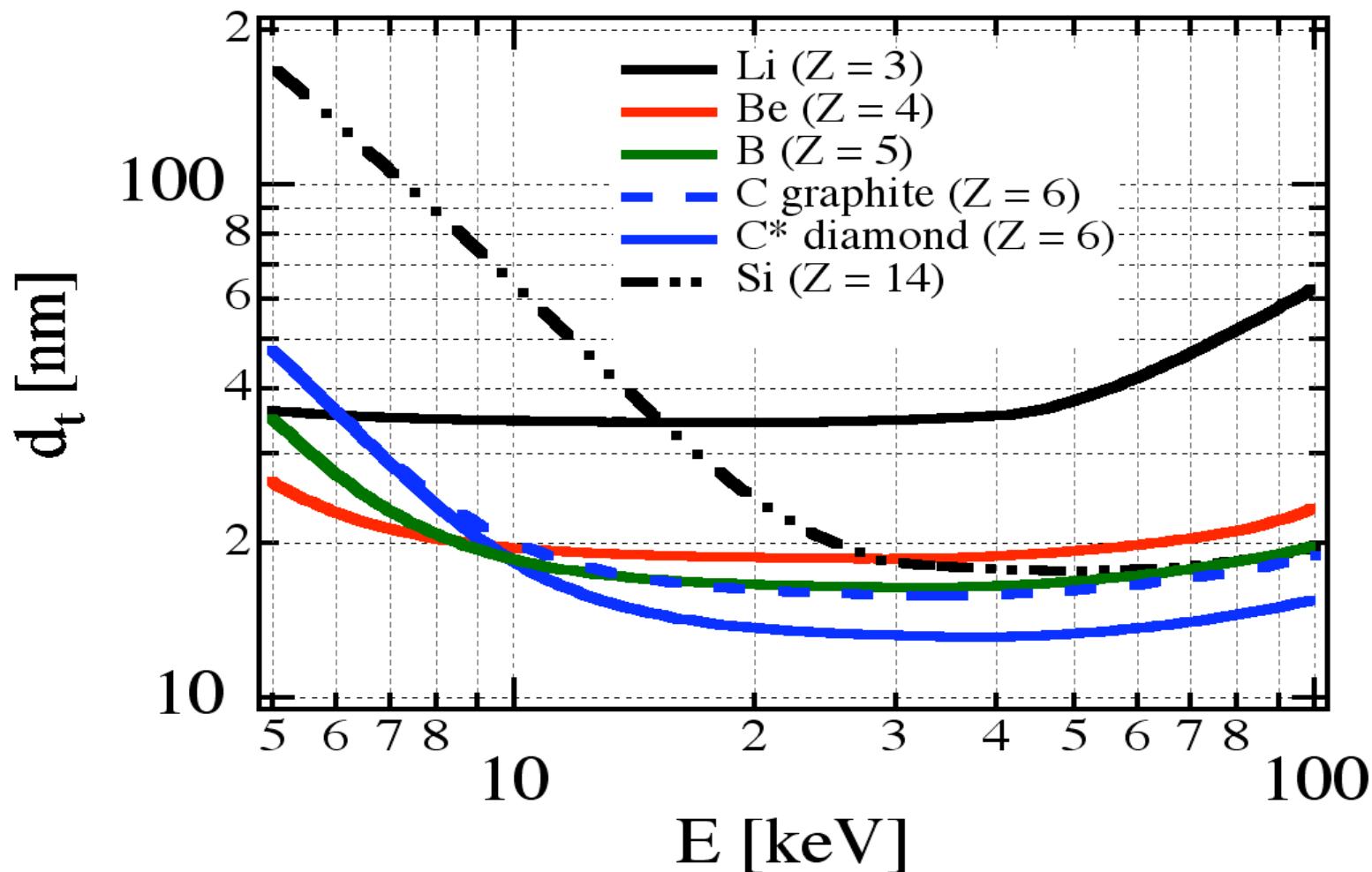
flux:  $> 10^9 \text{ ph/s}$

**facet-rods**

Map of diffuse scattering around  
Si(004)-reflection

# Limits of Focusing with NFLs

Diffraction limit:



$$\begin{aligned}N &= 100 \\I &\geq 0.084 \\R &= 0.5 - 50 \mu\text{m}\end{aligned}$$

NA limited by

$$\sqrt{2\delta}$$

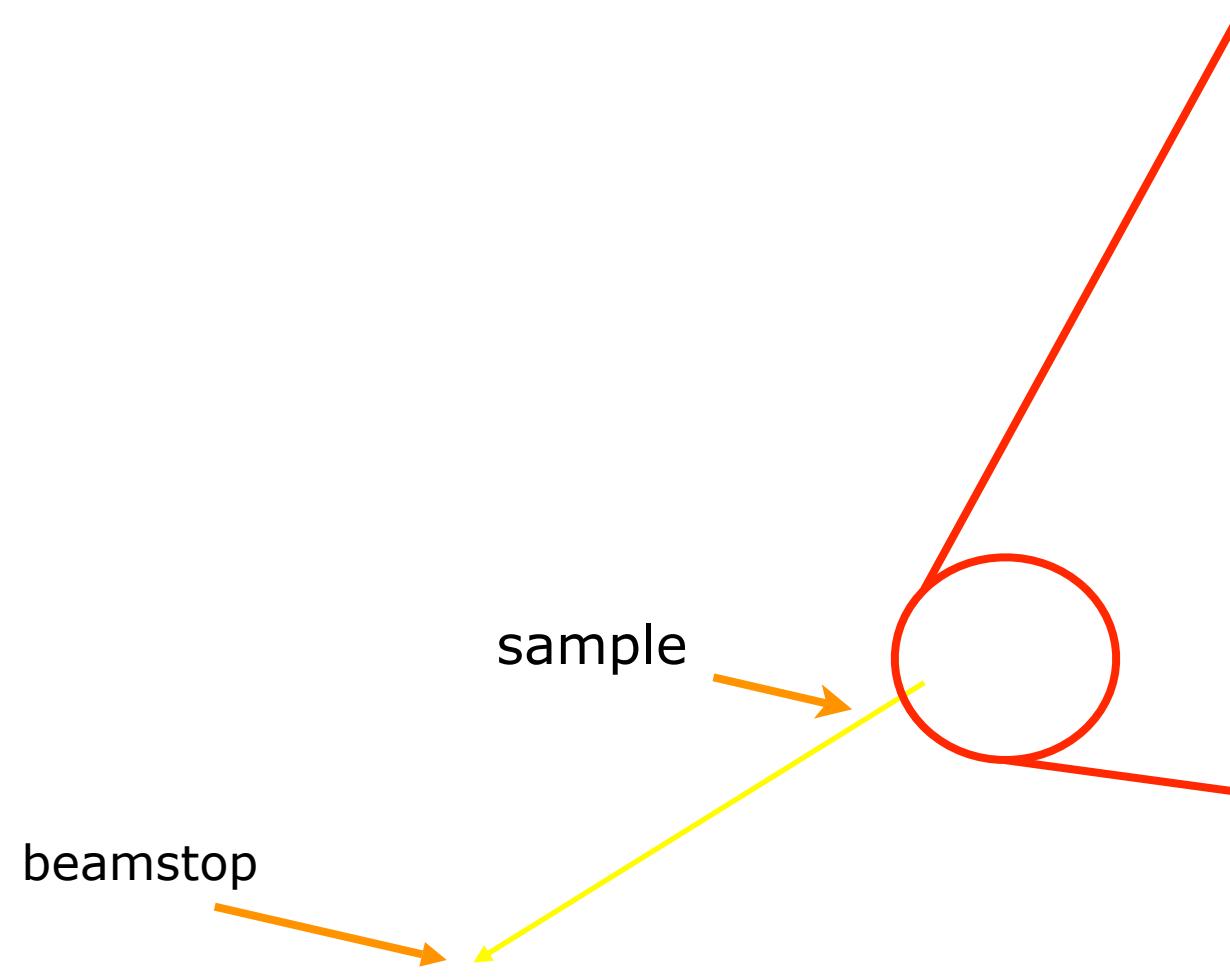
adapt aperture to  
converging beam (AFLs):

focus < 5 nm

[PRL 94, 054802 (2005)]

Further improvement of focus size with diffractive optics (e. g., MML).

# Nanoprobe: Coherent Nanodiffraction



$E = 15.25 \text{ keV}$   
 $\lambda = 0.813 \text{ \AA}$

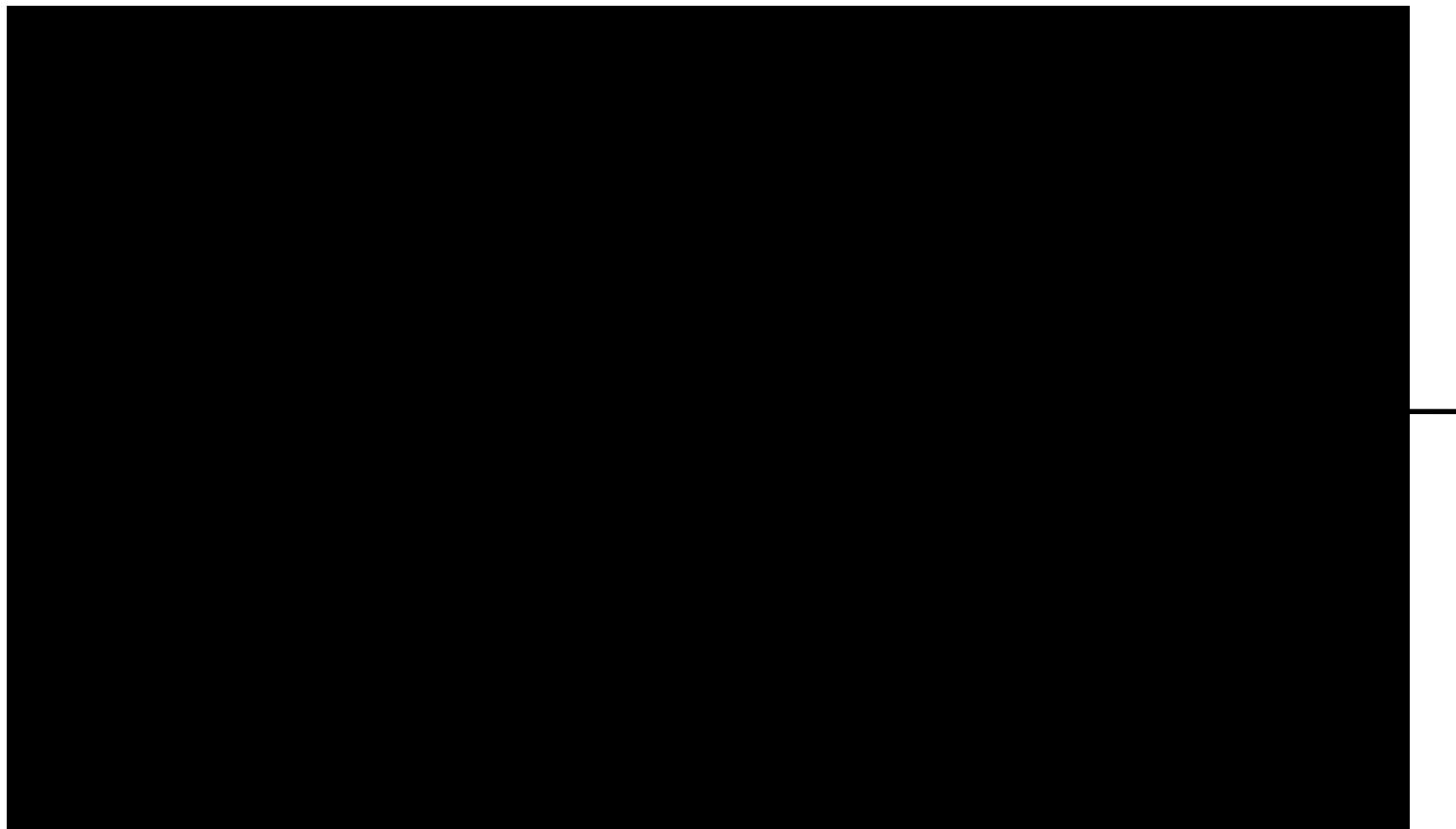
beam size:  
 $< 150 \times 150 \text{ nm}$   
(amplitude)

## Wave Front in Diffraction Limited Focus

divergence angle:  
numerical aperture

$$d_t = \frac{2\sqrt{2\ln 2}}{\pi} \frac{\lambda}{2NA} \approx 0.75 \frac{\lambda}{2NA}$$

Gaussian limited plane wave



CXDI  
XPCS, XFCS

## Coherence in Focus

Focus size (amplitude):

$$b_{\text{ampl}} = \sqrt{2b_{\text{geo}}^2 + 2d_t^2}$$

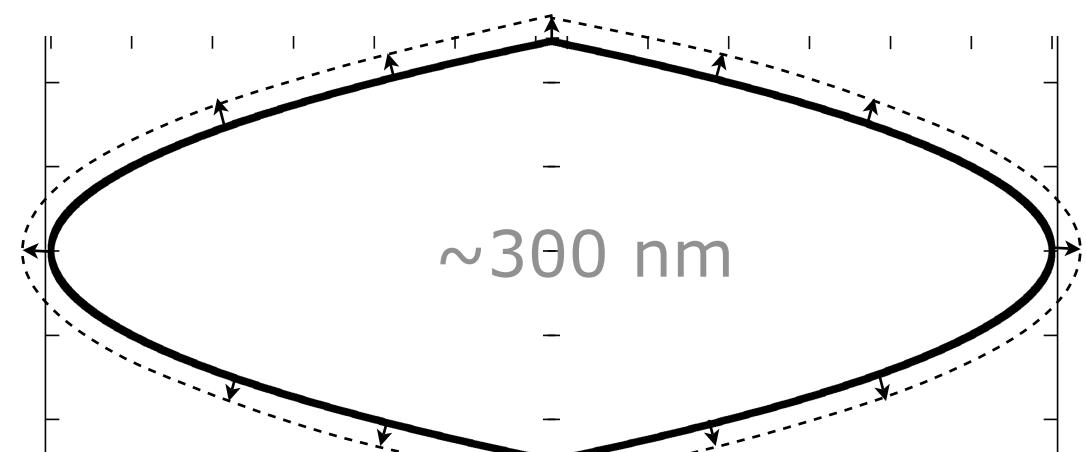
lateral coherence length:

$$l_t = 2d_t \sqrt{1 + \frac{d_t^2}{b_{\text{geo}}^2}}$$

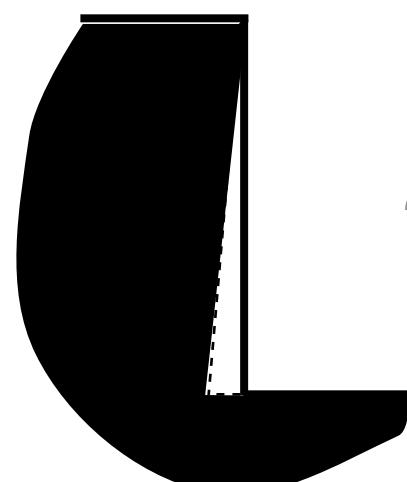
## So Far: No Ideal Lens...

Shape errors:

Underetching & proximity effect:



Roughness:



$\sim 10 \text{ mrad}$

tilted side wall

## Shape of Wave Front in Focus

Main result:

beam flat in central  
speckle

In general:

Speckle size in focal  
plane can not be finer  
than diffraction limit!

---

# Test Object: Gold Particle on Si<sub>3</sub>N<sub>4</sub>-Membrane

size < 100 nm

# Diffraction Pattern of Gold Nanoparticle

sample-detector distance:

1250 mm (in air)

detector:

FReLoN 4K

50 $\mu$ m pixel size

exposure time:

10 x 60 s

intensity on sample:

3300 ph/s/nm<sup>2</sup>

integral dose in beam:

10<sup>11</sup> ph > 2 month in fl  
coherent beam

compared to 10<sup>12</sup> ph/pulse  
at XFEL

# Reconstruction

reconstruction by HIO

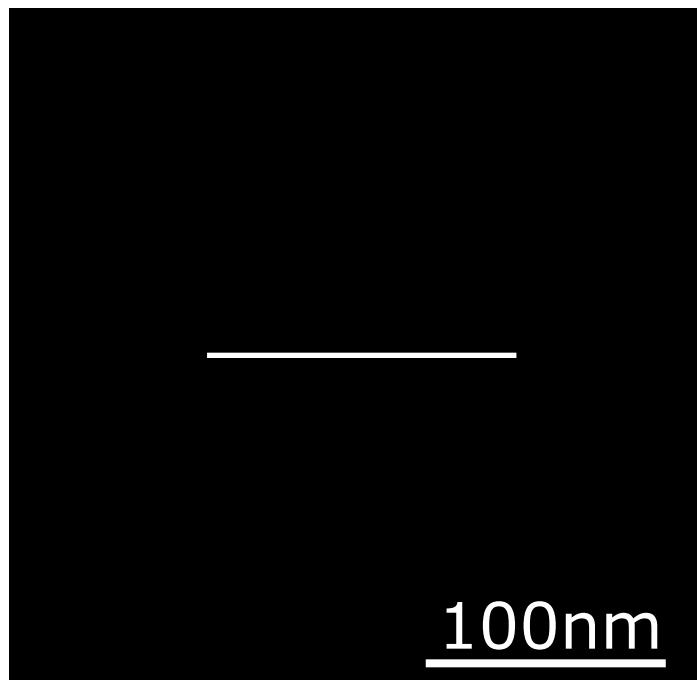
shrink-wrap

phase left free to evolve

200 reconstructions

(9 converged to wrong solutions)

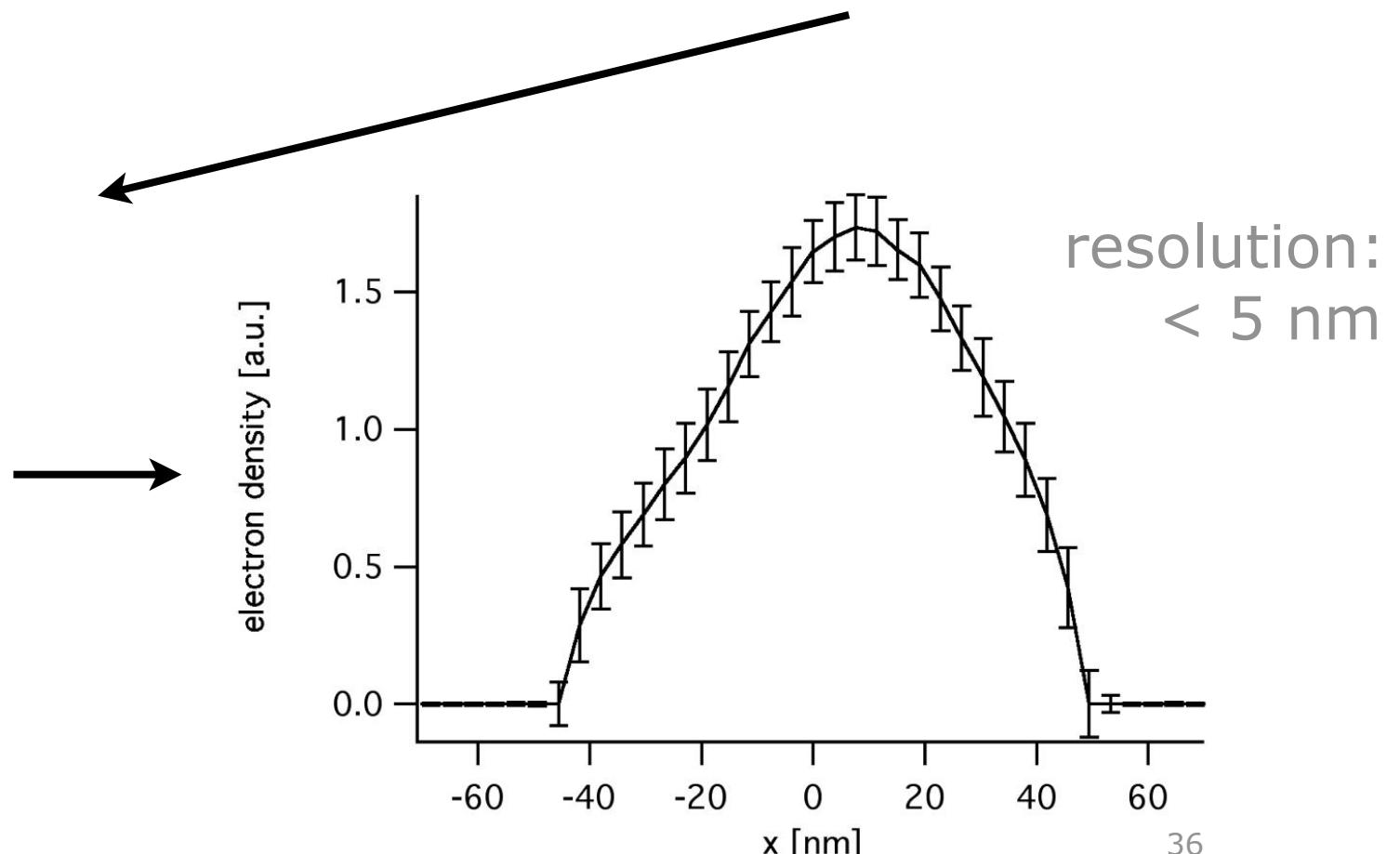
averaged solution:



reconstructions:

left-handed

right-handed



# Conclusion

Refractive x-ray lenses:

- high resolution imaging optics

- small numerical apertures ( $\sim$  mrad): aspherical lens is parabolic

- spatial resolution  $\sim$ 100 nm and below for different designs

- diffraction limits (theoretical):

  - < 20 nm for regular design (all lenses same size)

  - $\sim$  5 nm for adiabatically focusing lenses

  - (lens size adapted to converging beam)

- diffraction limited focusing: high degree of coherence in focus

Applications:

- full-field microscopy

- scanning microscopy (fluorescence, diffraction, absorption)

- coherent diffraction imaging

- combine scanning microscopy with coherent diffraction imaging:

  - ptychography [Thibault, et al., Science **321**, 379-382 (2008)]

# Kinoform x-ray lens arrays

Werner Jark

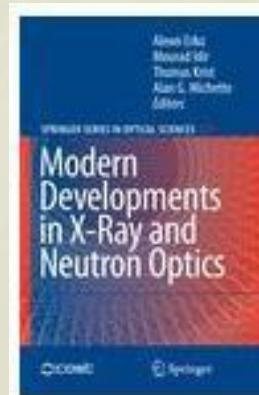
Sincrotrone Trieste  
Basovizza (TS), Italy

[werner.jark@elettra.trieste.it](mailto:werner.jark@elettra.trieste.it)



[www.elettra.trieste.it/experiments/  
beamlines/microfluo/index.html](http://www.elettra.trieste.it/experiments/beamlines/microfluo/index.html)

[www.elettra.trieste.it/organisation/  
experiments/laboratories/  
multilayer\\_technology/index.html](http://www.elettra.trieste.it/organisation/experiments/laboratories/multilayer_technology/index.html)

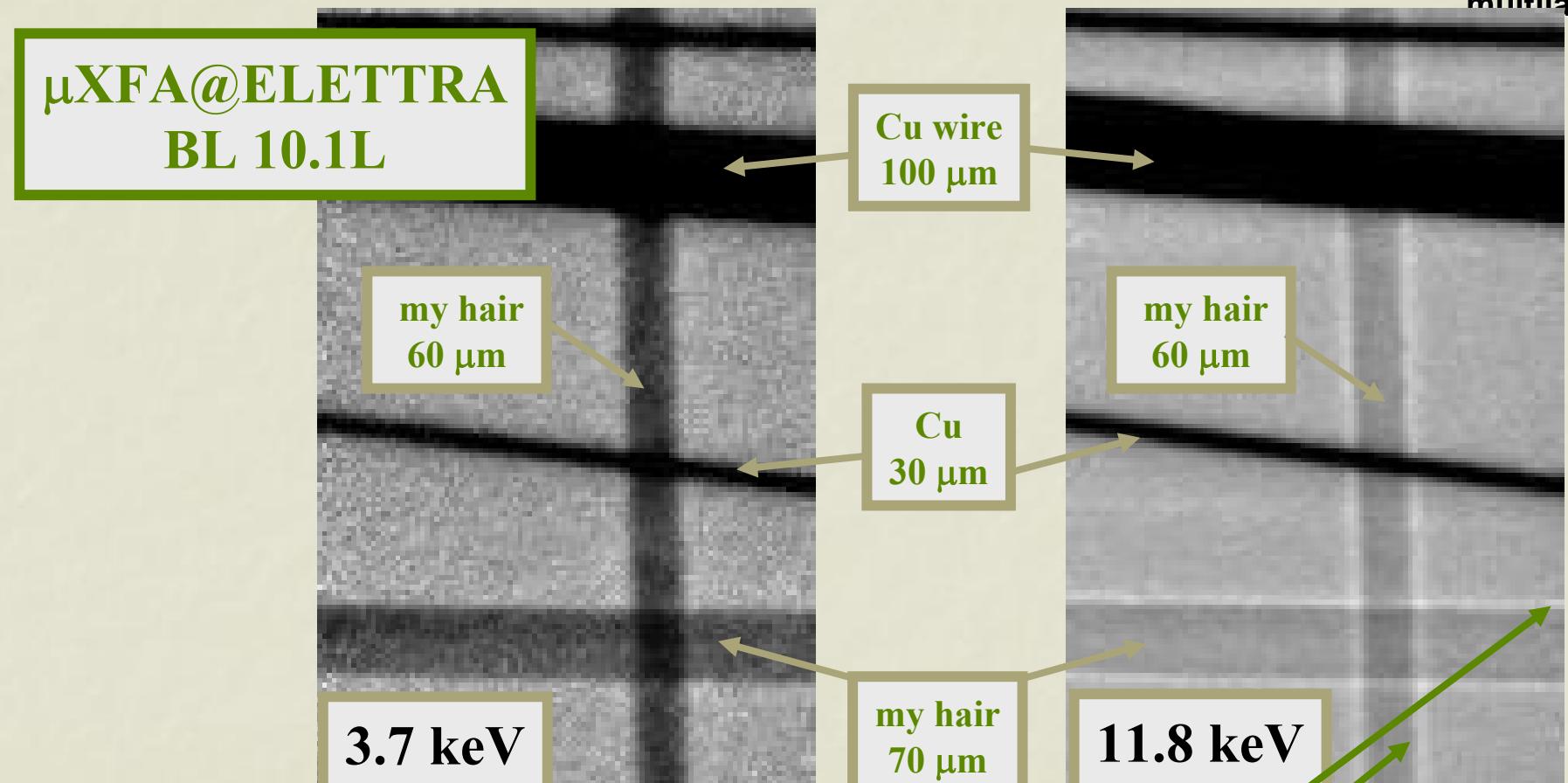


Modern Developments in X-Ray and Neutron Optics  
Series: Springer Series in Optical Sciences , Vol. 137  
Erko, A.; Idir, M.; Krist, Th.; Michette, A.G. (Eds.)  
2008, XXIII, 533 p. 299 illus., 5 in color.  
With series ad on (virtual) p. 535, 536., Hardcover

ISBN: 978-3-540-74560-0

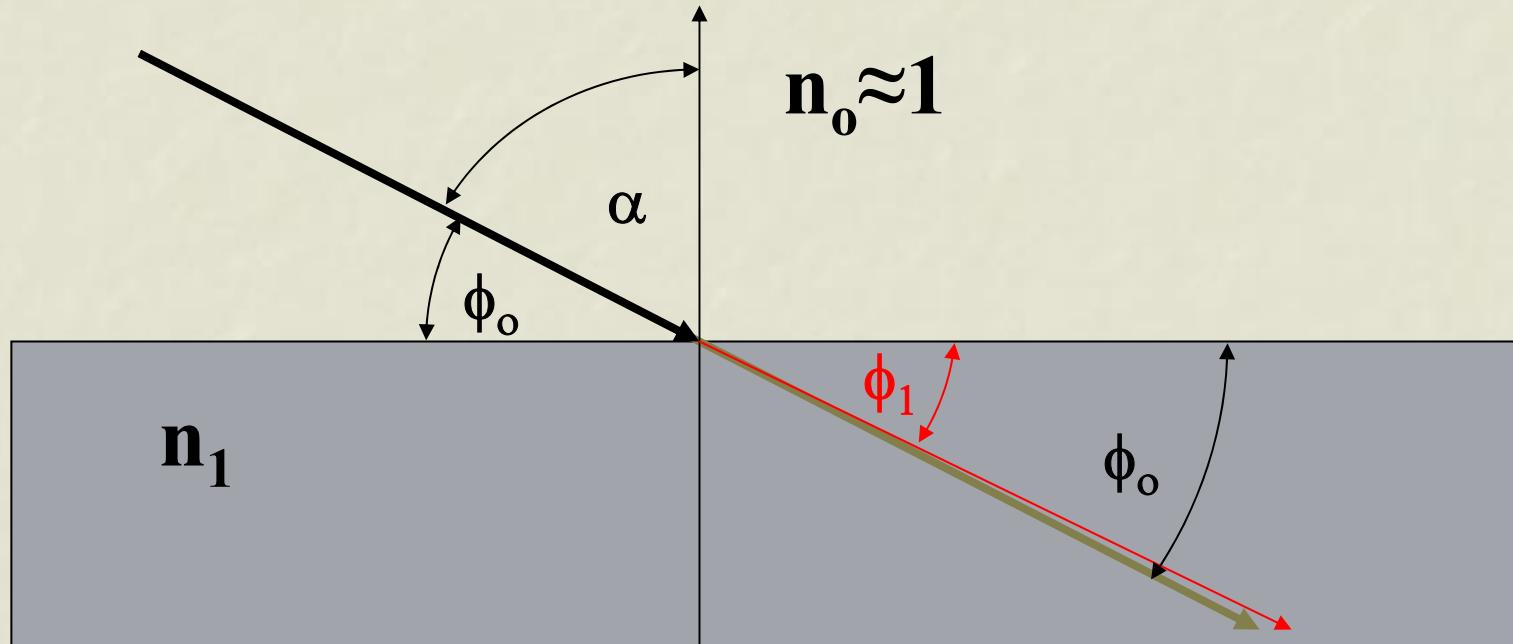
Read on CLESSIDRA kinoform lenses  
on pages 331-351

# What happens here?



transparent hairs can deviate (i.e. refract) x-rays

# Refraction and reflection: x-rays

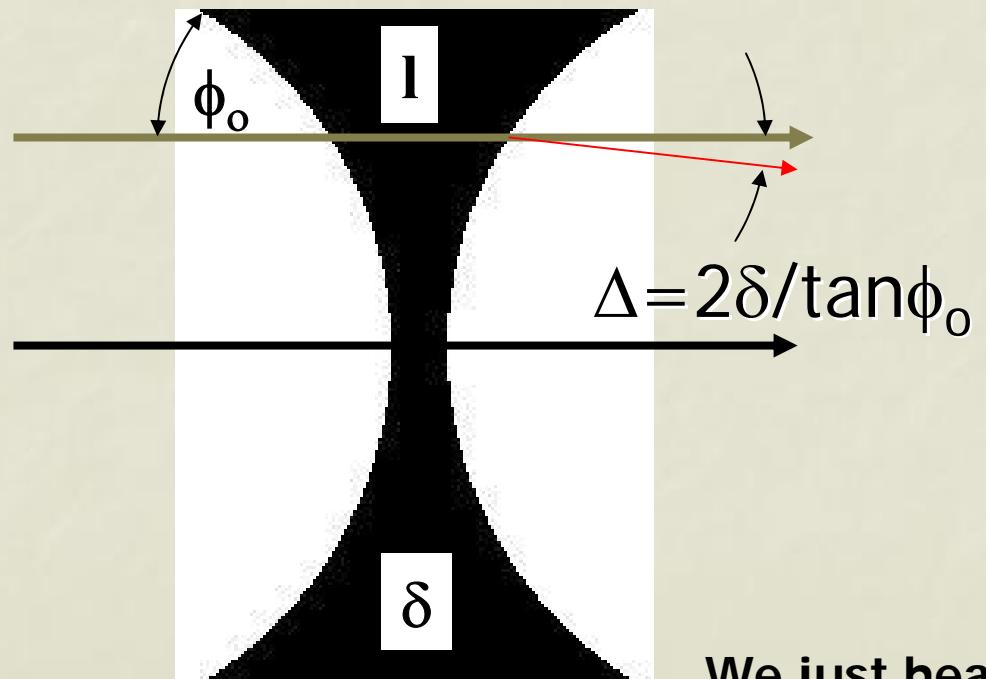
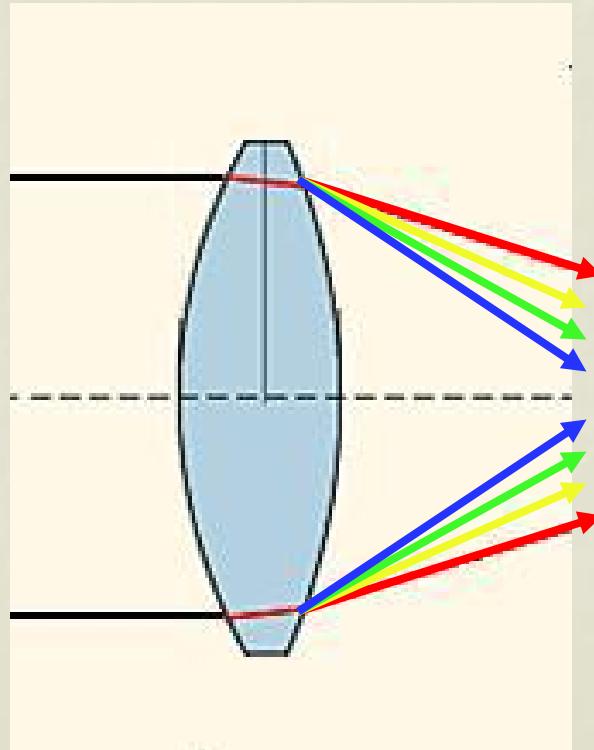


- Snell's law:  $n \sin\alpha = \text{const}$        $\cos\phi_o = (1-\delta) \cos\phi_1$
- Beam deviation at one interface:       $\Delta = \phi_o - \phi_1$
- with  $\cos\Delta = 1$ ,  $\sin\Delta = \Delta$ :  $\cos\phi_1 = \cos\phi_o + \Delta \sin\phi_o$  then  $\Delta = \delta / \tan\phi_o$

# Refraction in transmitted x-rays

$n > 1.0$ : convex  
lens focuses

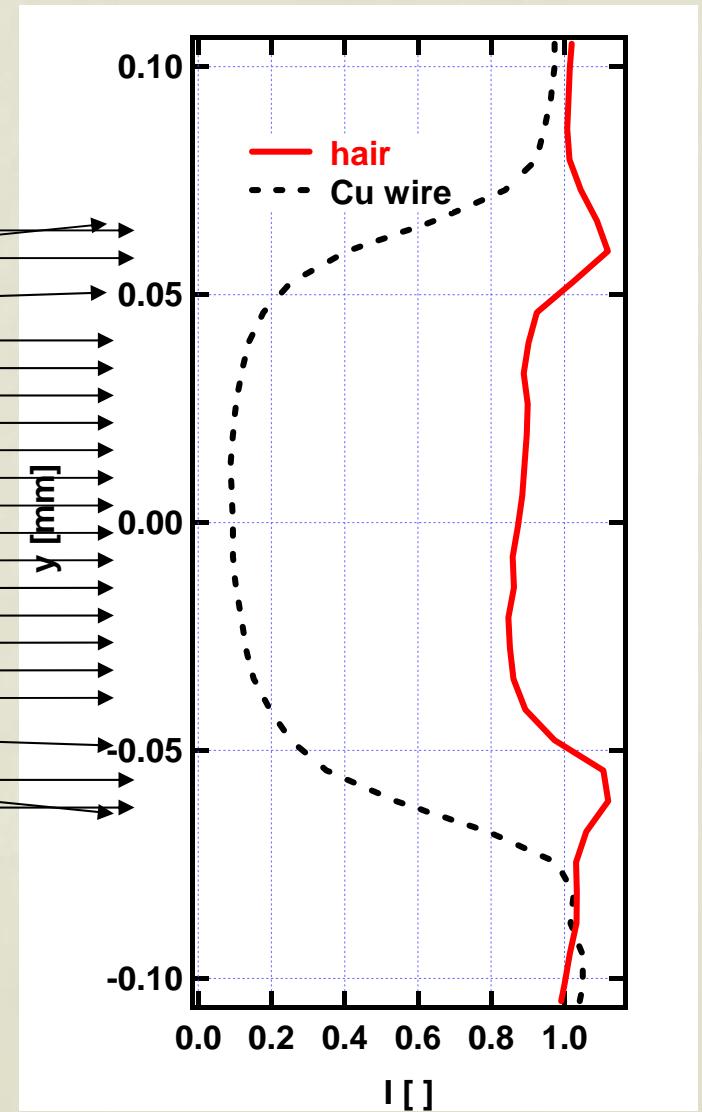
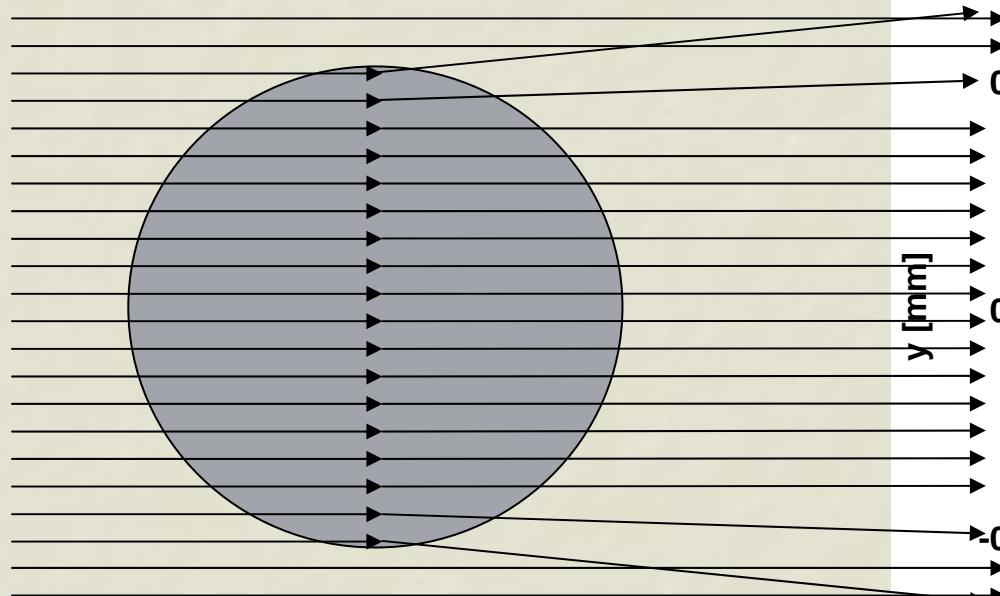
$n < 1.0$ : concave  
lens focuses



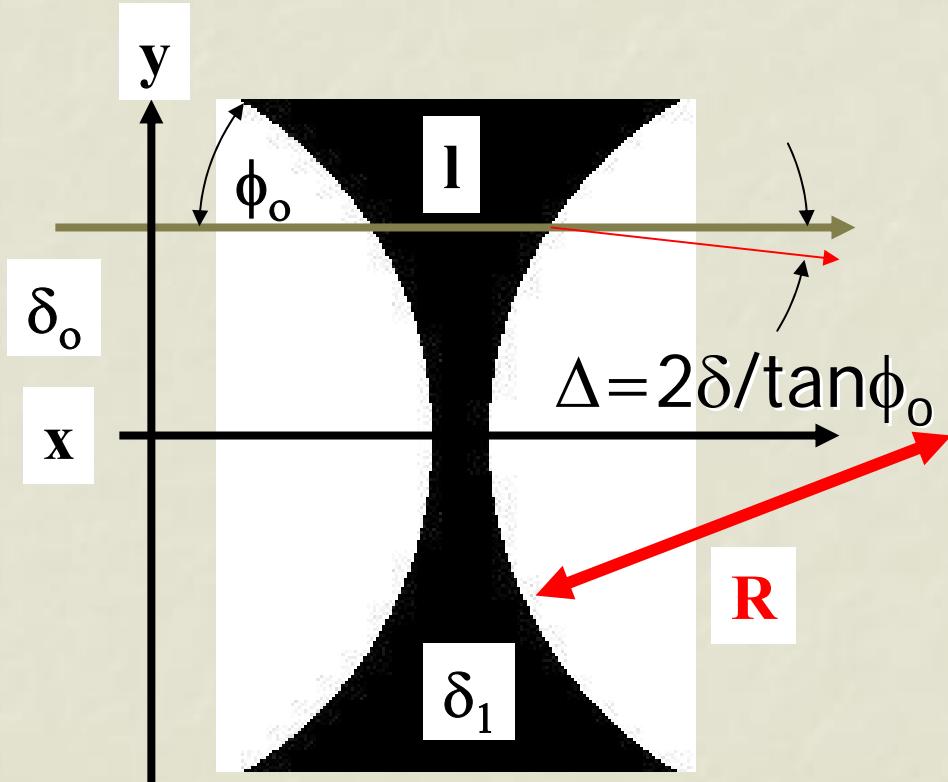
We just heard it!

# Refraction in transmitted x-rays

Back to hair and Cu wire



# Refraction in transmitted x-rays



Equation for parabola

$$2R(x-x_0)=y^2$$

focal length

$$f=R/(2\delta)$$

Parabolic material increase

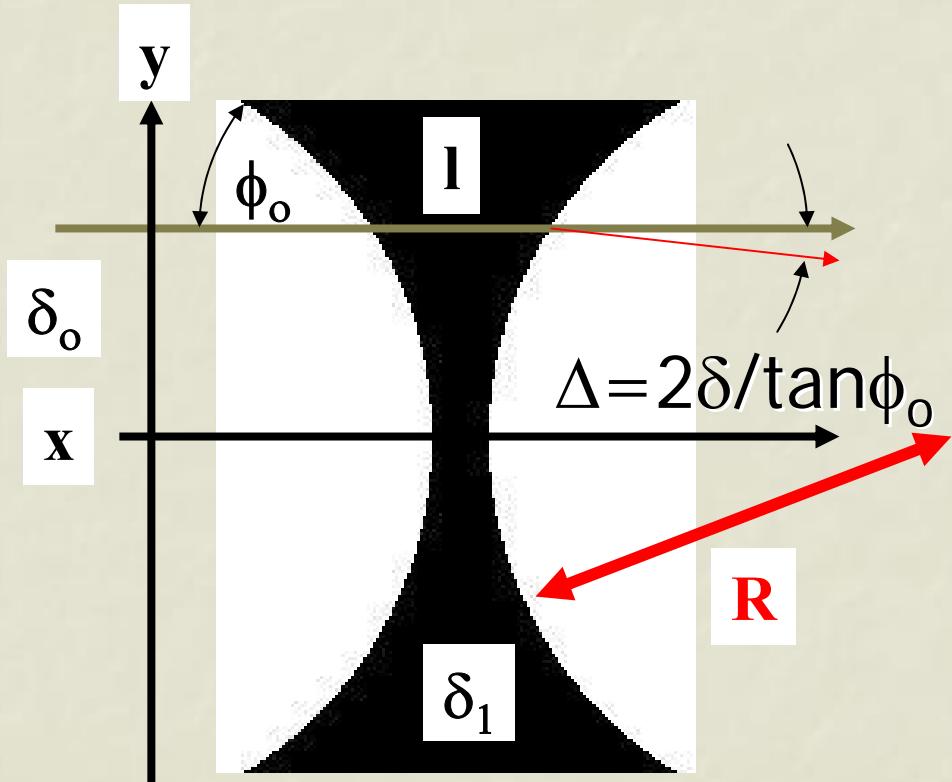
$\rightarrow$

Gaussian transmission function

$$T=\exp(-y^2/(2\delta f L))$$

with  $L$ =attenuation length

# Refraction in transmitted x-rays



$$T = \exp(-y^2/(2\delta f L))$$

Optimum aperture

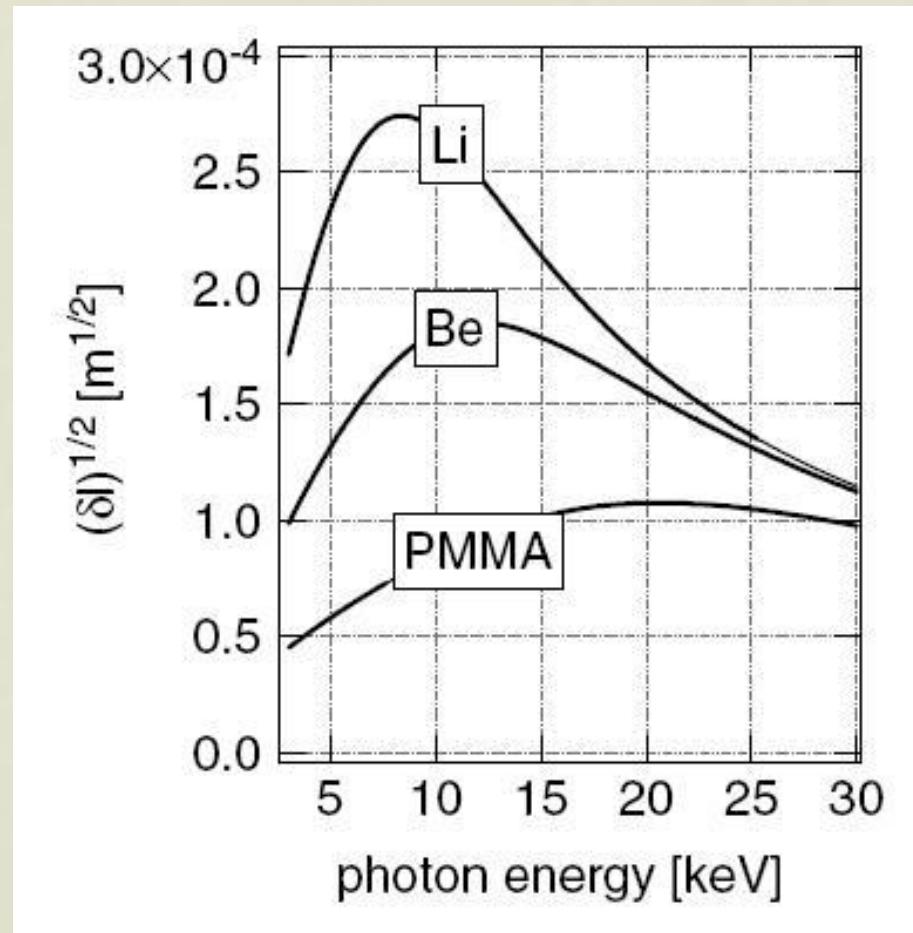
$$A = 2\sqrt{2\delta f L}$$

Average T is 75%

Figure of merit  
of materials  
 $\sqrt{\delta L}$

# Refraction in transmitted x-rays

Figure of merit  $\text{sqrt}(\delta L)$



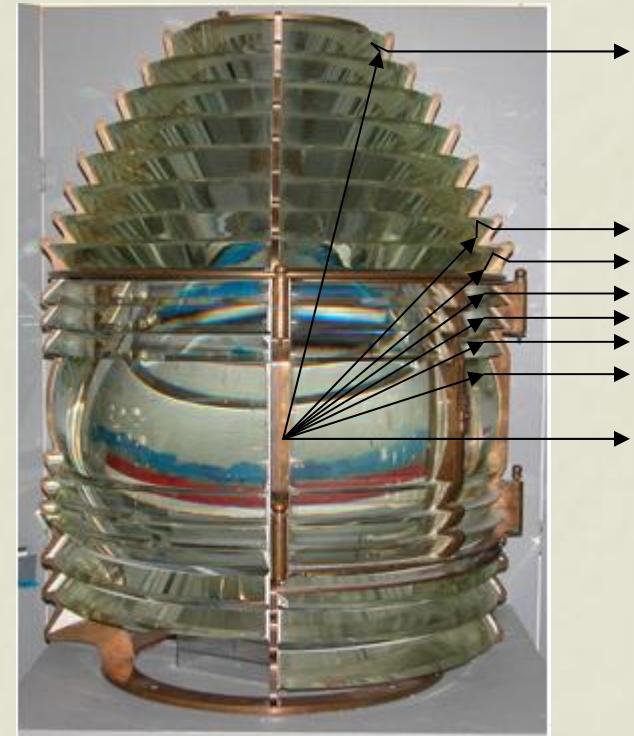
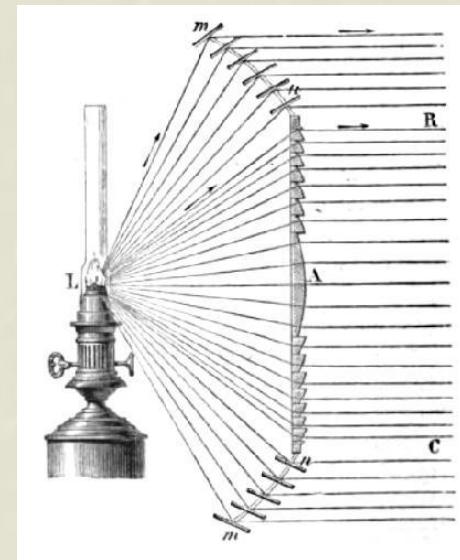
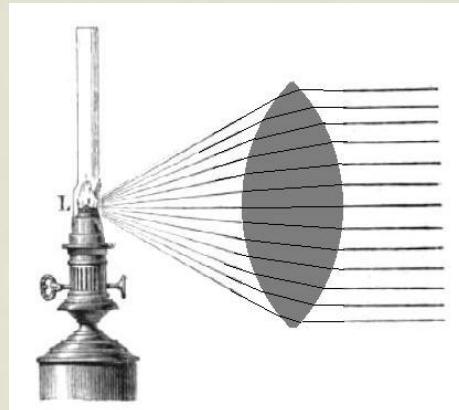
Difficult Li, very interesting  
Be, but also plexiglass  
(pmma)

Compton scattering  
dominates at higher  
energies (>30 keV):  
all materials have similar  
figure of merit

# Can we “lighten” the lens?

A.J. Fresnel made the CONVEX lenses for the Cordouan lighthouse in 1822 lighter

Strategy: Refraction only on transmission through inclined surfaces



remove “useless” rectangular blocks

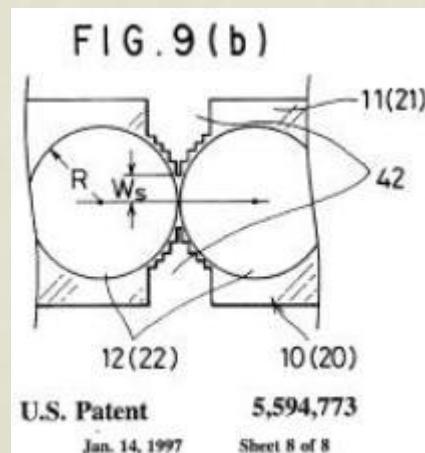
increase angles by refraction – reflection – refraction in prisms

# To “lighten” a CONCAVE lens

**History:**  
**Prior to introduction of compound refractive lenses (CRL)!**

Suehiro et al, Nature 352, 385 (1991): proposal in letter without picture (lathe)  
 Michette, Nature 353, 510 (1991): critically comments the idea  
 Yang, NIM A328, 578 (1993): more detailed elaboration

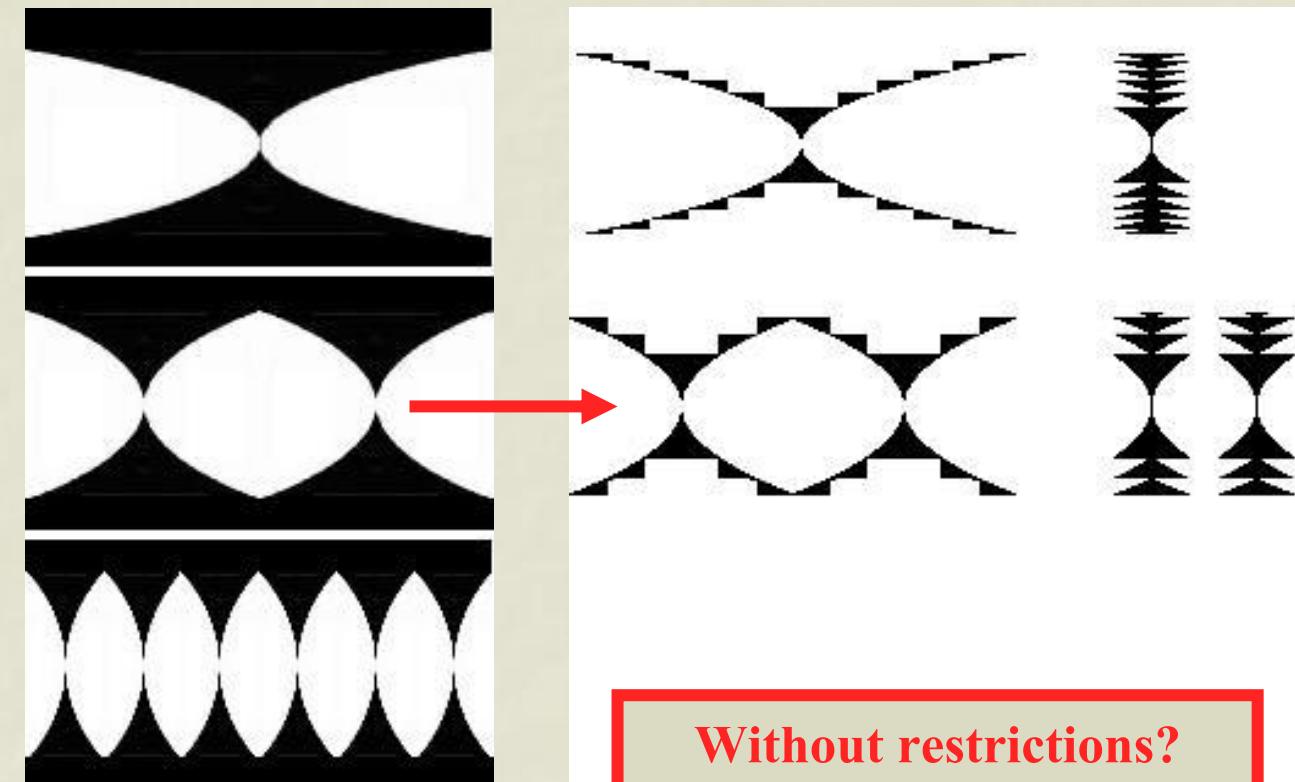
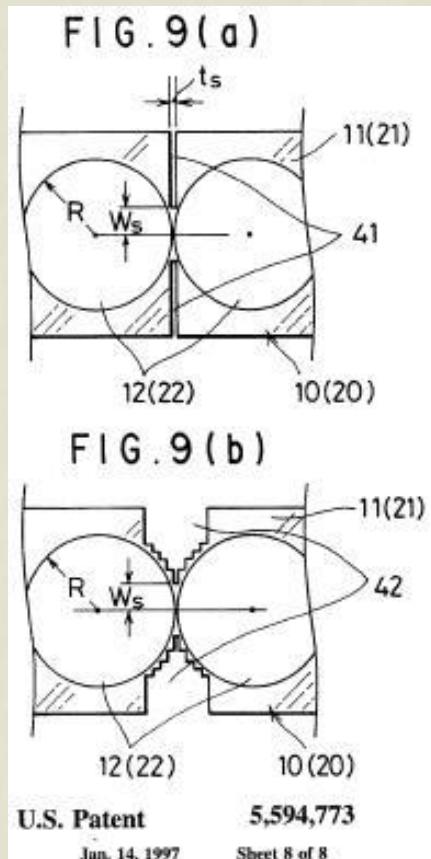
T. Tomie, “X-ray lens”,  
 Japanese patent 6-045288  
 (18 Febr 1994)  
 Covering compound  
 refractive lenses and  
 “lightened” lenses



Never made this way

First realisation:  
 Aristov et al, APL 77,  
 4058 (2000)

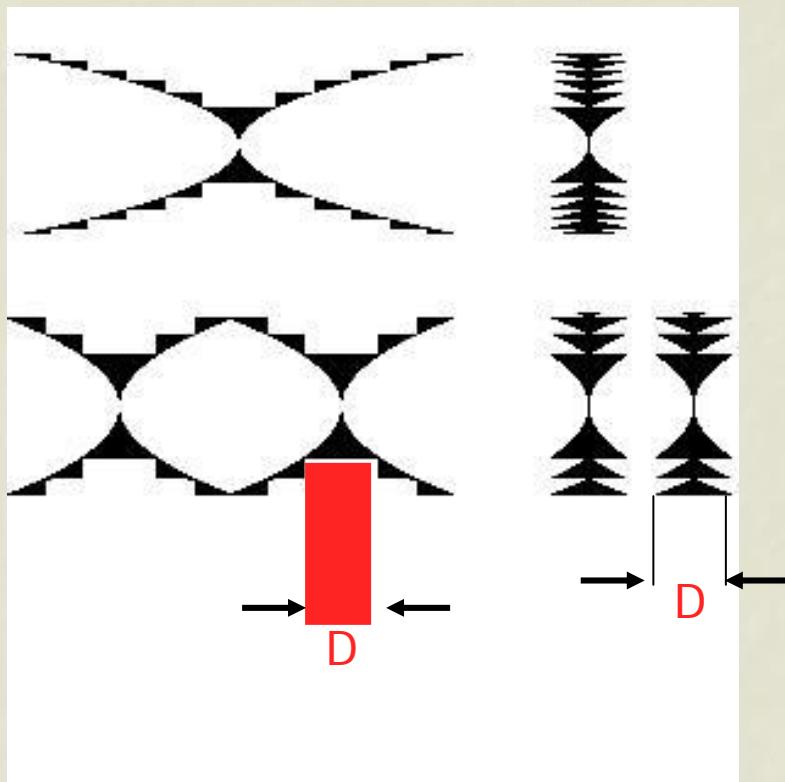
# To “lighten” a CONCAVE lens



Without restrictions?

Tomie 1994

# Restrictions



Do not distort the passing wave  
Keep planes of equal phase continuous

Make use of longitudinal field periodicity:

Remove blocks, which shift phase by  
integer multiple of  $2\pi$ !

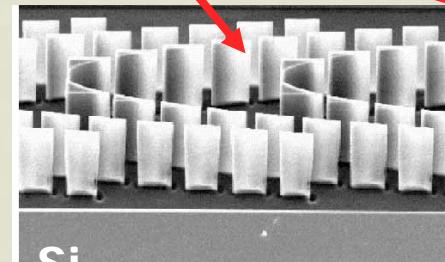
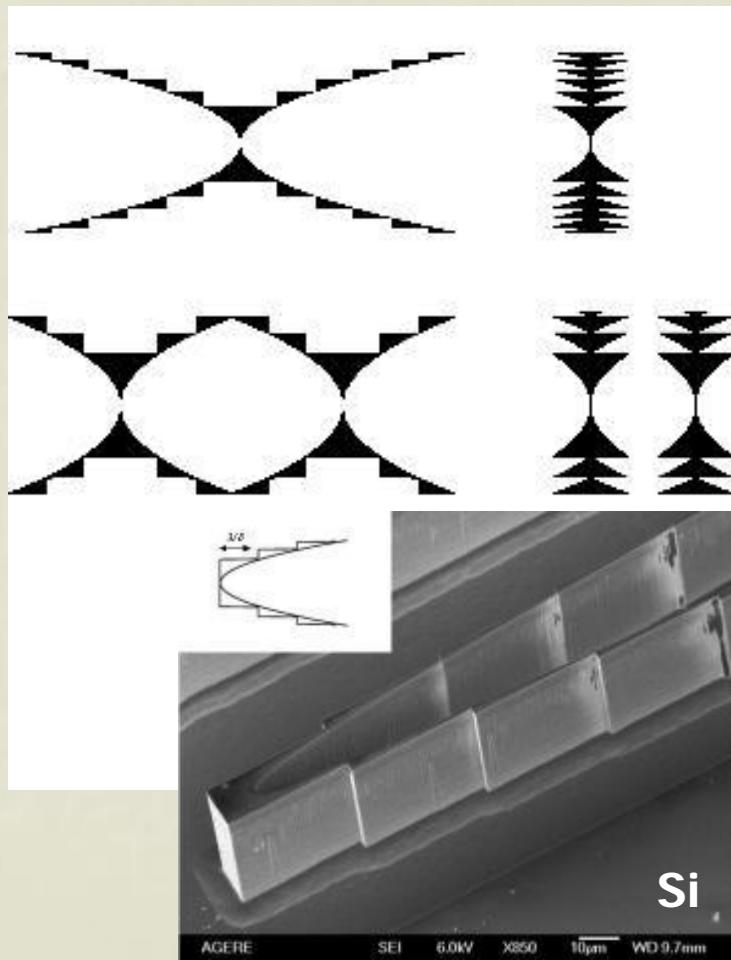
$$D = m\lambda/\delta$$

$m$  = integer multiple  
 $\lambda$  = wavelength  
 $\delta$  = refractive index

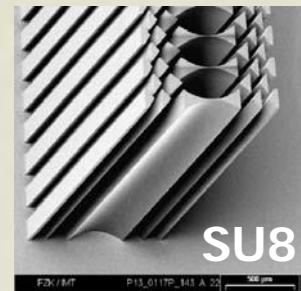
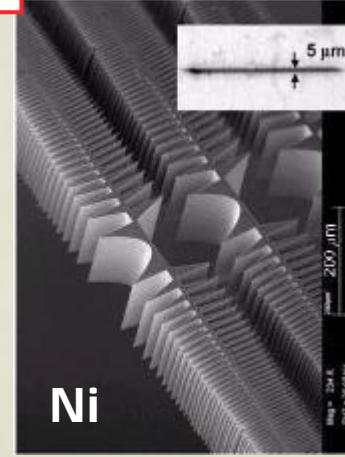
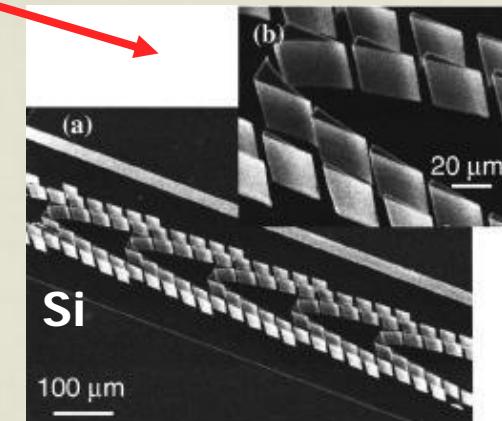
# Reduced material!!!

First prototype: Aristov et al, APL 77, 4058 (2000)

These are kinoform lenses produced by lithography



$D=m\lambda/\delta \approx 40 \mu\text{m}$   
For Si@12 keV



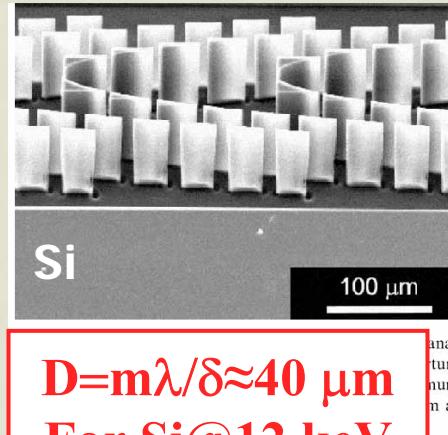
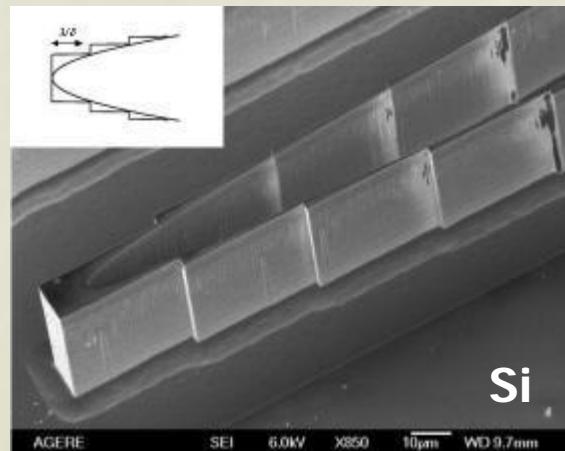
later: Evans-Lutterodt et al, Opt. Express 11, 919 (2003), Nöhammer et al, JSR 10, 168 (2003), Nazmov et al, NIM B217, 409 (2004), Alianelli et al, SPIE Proc. 6705, art. no. 670507 (2007) (single in Si)

# Reduced material!!!

Dimensions: make very good use of chip mass production techniques

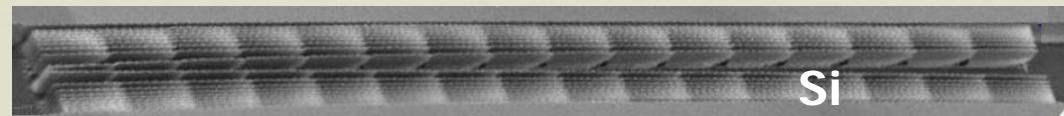
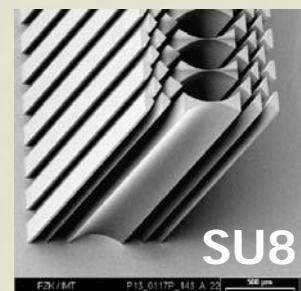
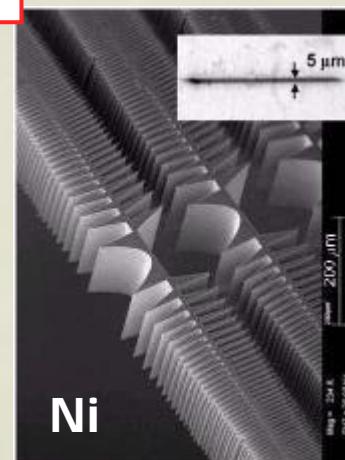
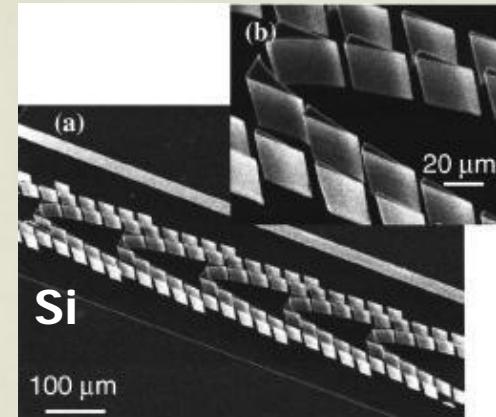
BUT lithography can only shape linear structures

Need crossed lens pair for bi-dimensional focusing:  
match height and aperture!!



$$D = m\lambda/\delta \approx 40 \text{ } \mu\text{m}$$

For Si@12 keV



Still room for other shapes

# Looks good!!

But: More flux than center segment could provide?  
Better spot size than diffraction limit of center segment?

- YES, both

- More flux,  
large focus

- NO, both

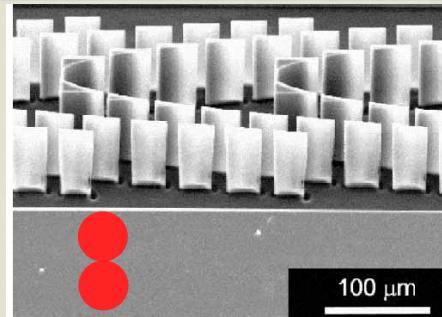
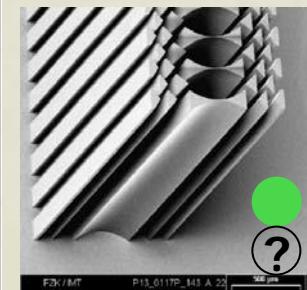
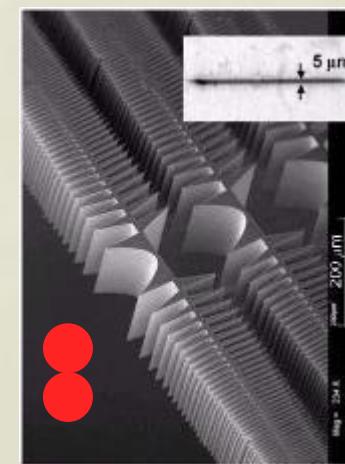
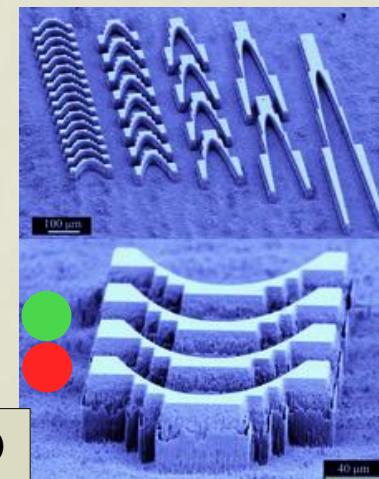
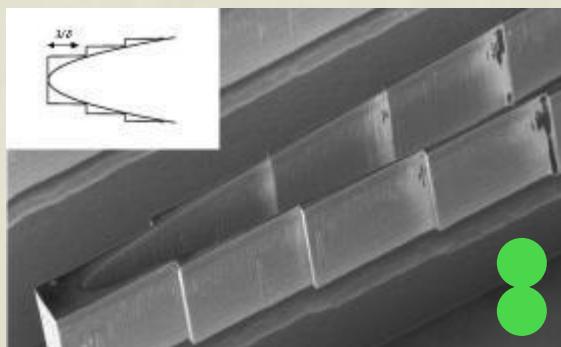
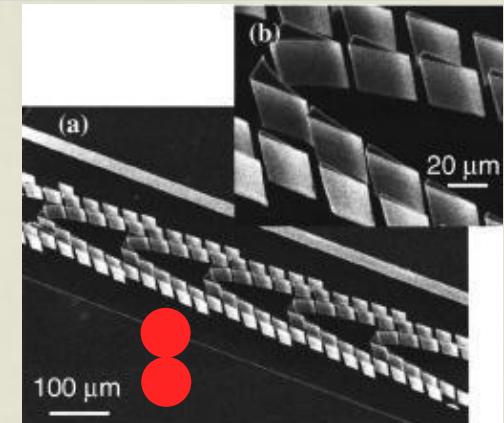


Fig. 1. An SEM micrograph of a 100  $\mu\text{m}$ -deep silicon planar parabolic lens with minimized absorption. The lens aperture  $A = 150 \mu\text{m}$ , the number of unit lenses  $p = 5$ , the maximum phase variation number  $M = 2$ , the focal length  $F = 80 \text{ cm}$  at the design wavelength  $\lambda_0 = 0.071 \text{ nm}$  ( $E_0 = 17.48 \text{ keV}$ ).

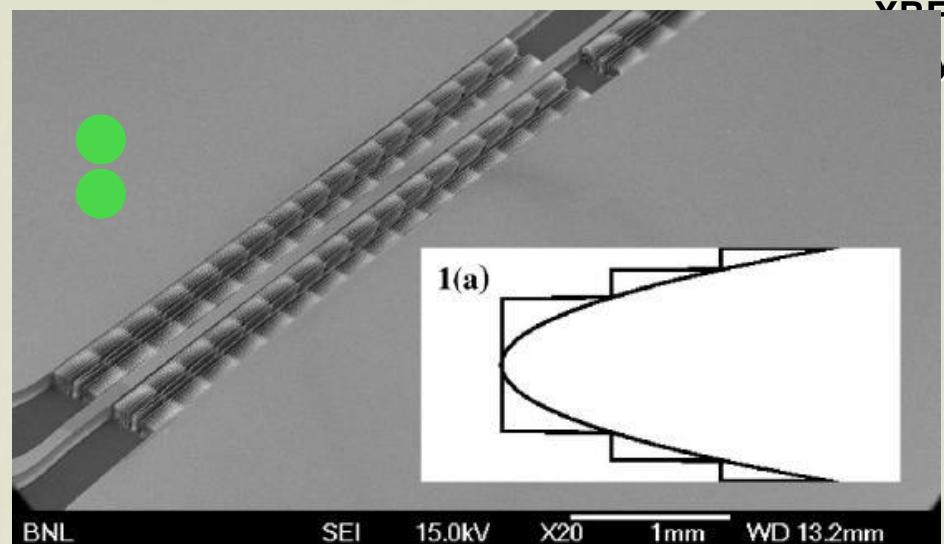
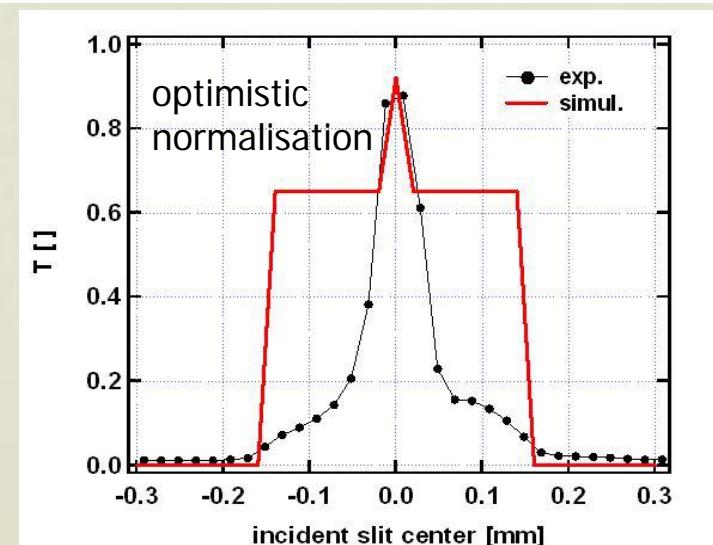
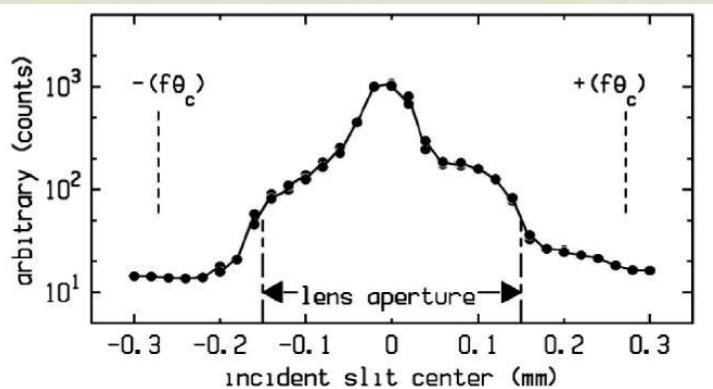


Evans-Lutterodt et al, Opt. Express 11 (2003)  
Alianelli et al, SPIE Proc. 6705 (2007)

IMT@FZK

# Problem: small outer zones

Evans-Lutterodt et al, PRL 99  
(13), 134801 (2007)



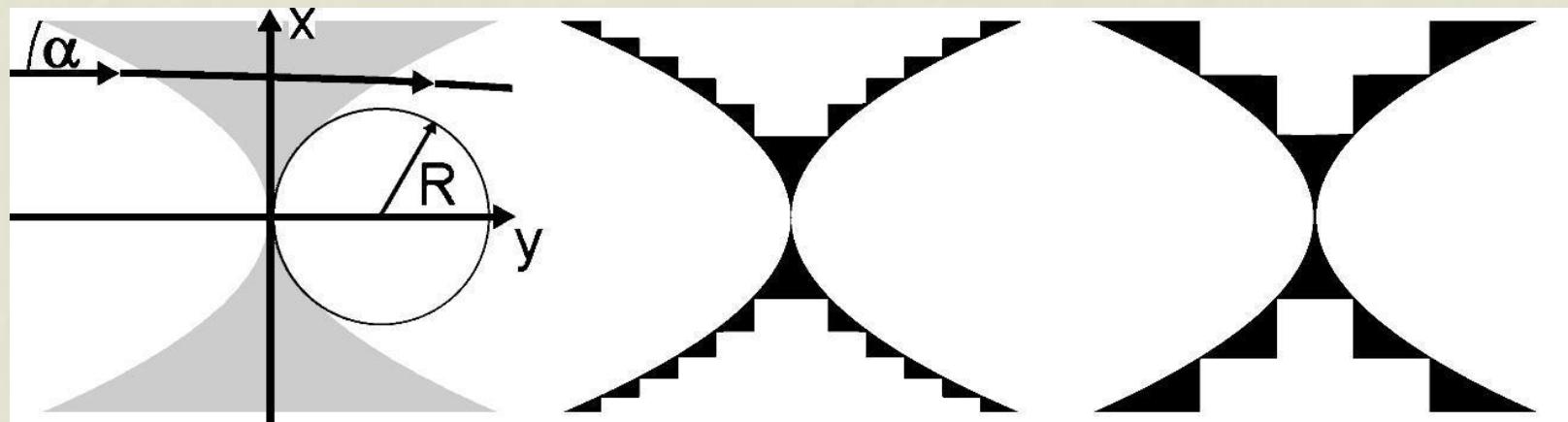
Transmission: integrated  $\leq 30\%$   
i.e.  $\leq 45\%$  of expectation  
Drops off when segment height  $< 2 \mu\text{m}$

Nevertheless in single lens  
smallest focus  $\approx 320 \text{ nm fwhm}$   
(Stein et al, JVST B26, 122 (2008))  
private communication Evans-Lutterodt:  
more recently  $\ll 320 \text{ nm}$

# Alternative "lightening"

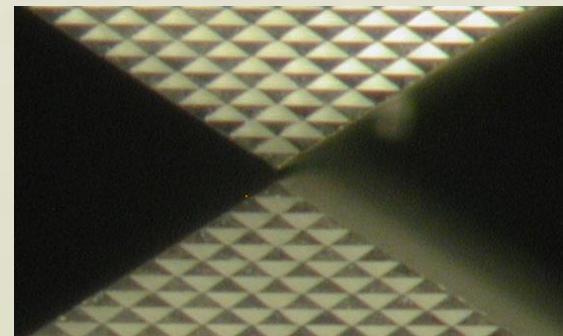
How to keep segment HEIGHT large?

Keep it constant!

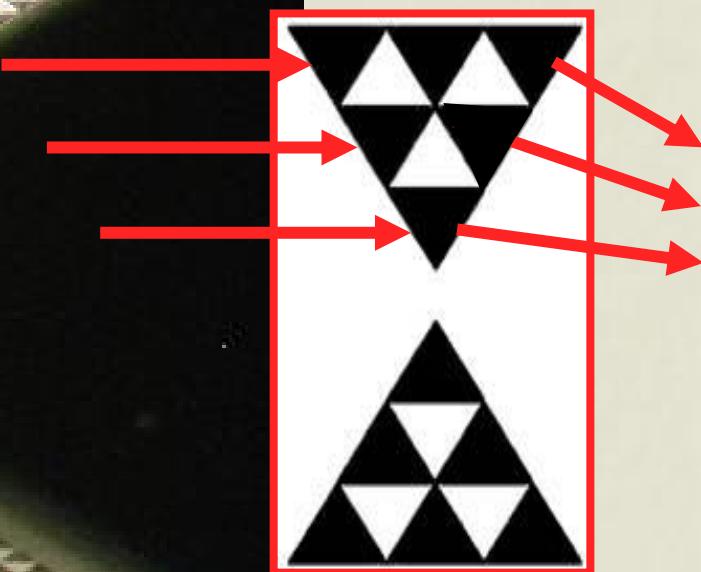
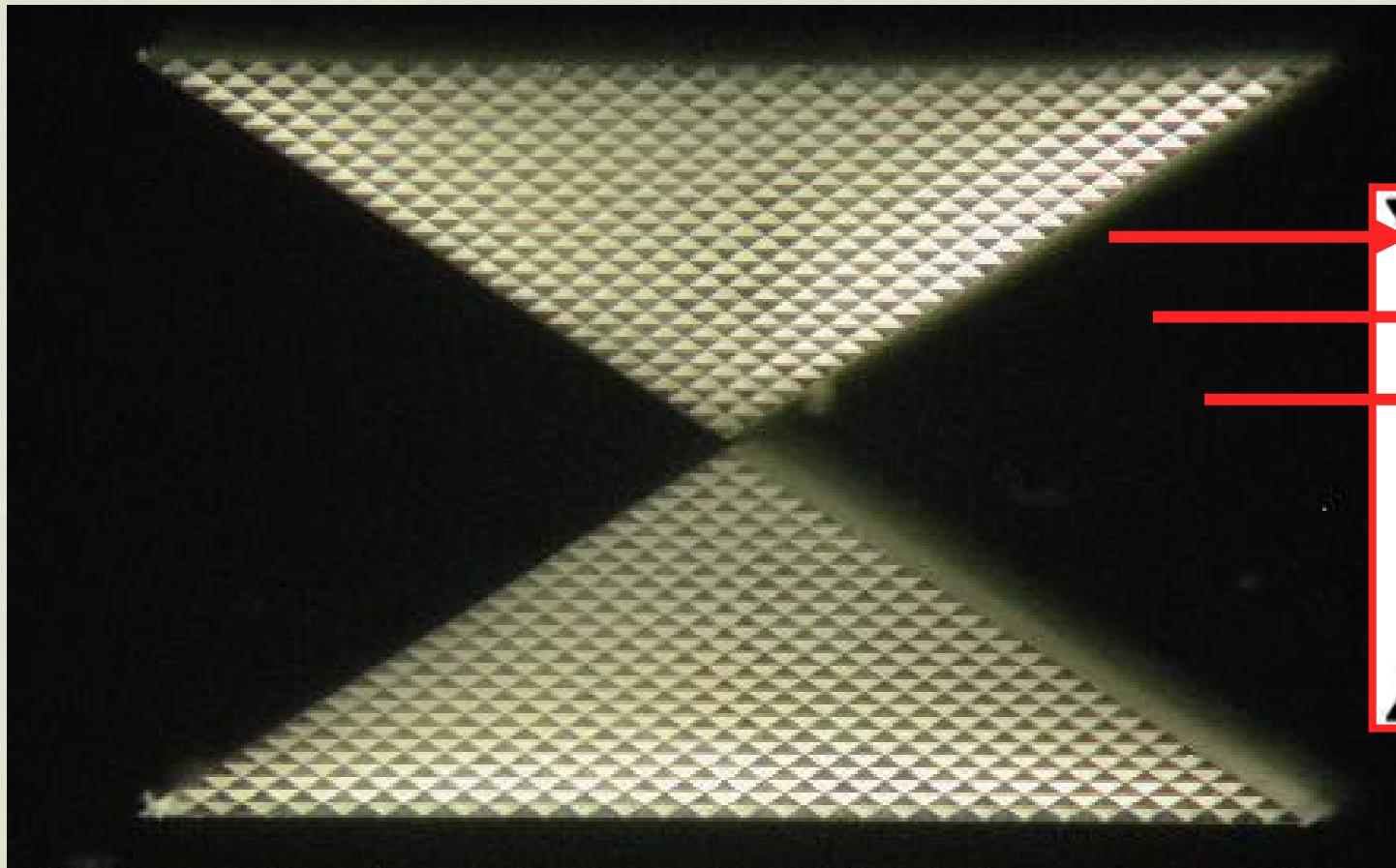


Then simplify and compact the lens

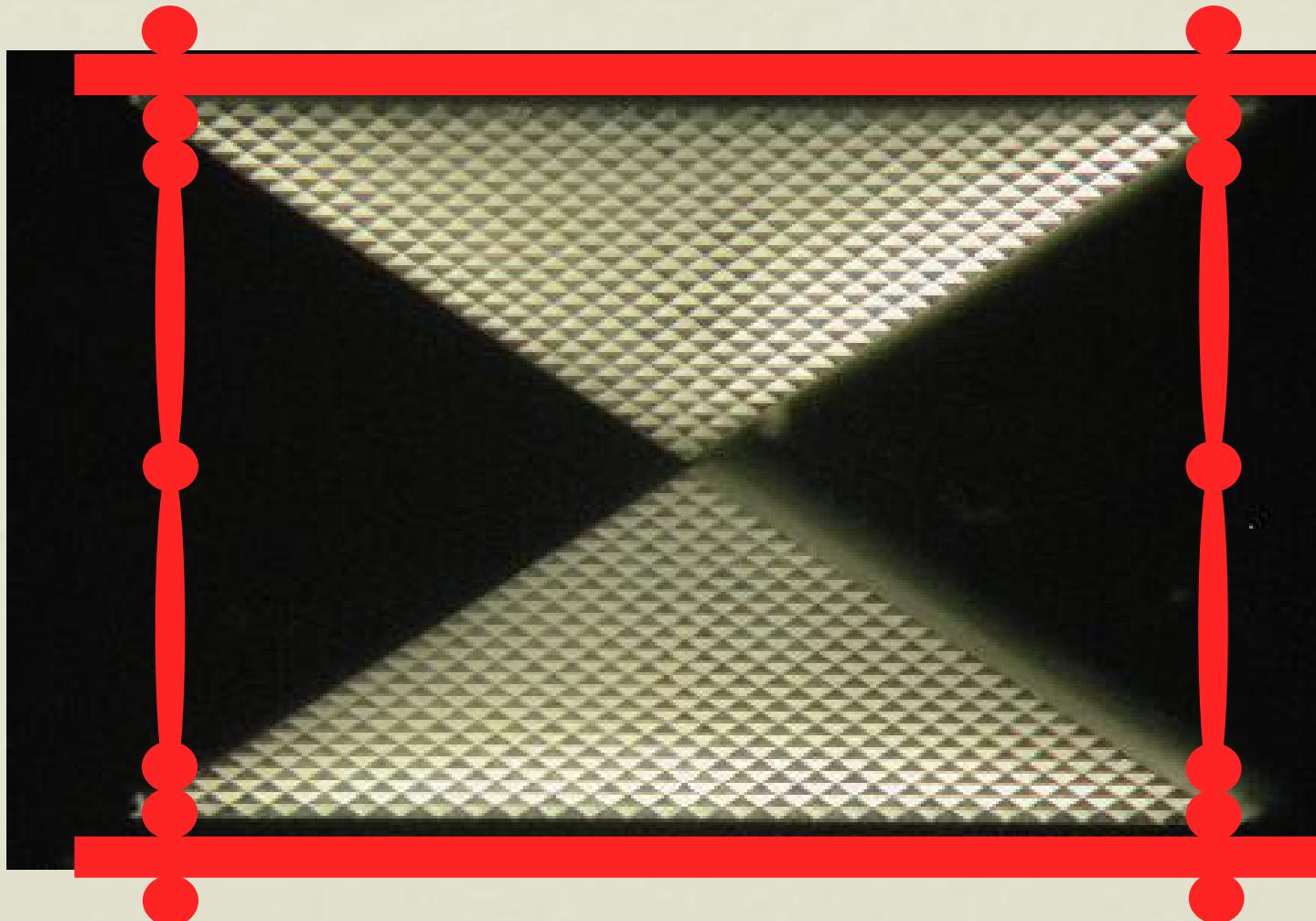
and make it



# It needs a name



# Looks good: CLESSIDRA



Jark et al,  
JSR 11,  
248 (2004)

Jark et al,  
JSR 13,  
239 (2006)

As before  
 $D \approx 40 \mu\text{m}$

for  
 $\text{SU8}@8 \text{ keV}$   
 $\text{Si}@12 \text{ keV}$

ISSN 0909-0495

Volume 13

Part 3

May 2006

May  
2006

Beamlines and optics

Detectors

Electronics and data acquisition

Sample chambers and environment

Diffraction

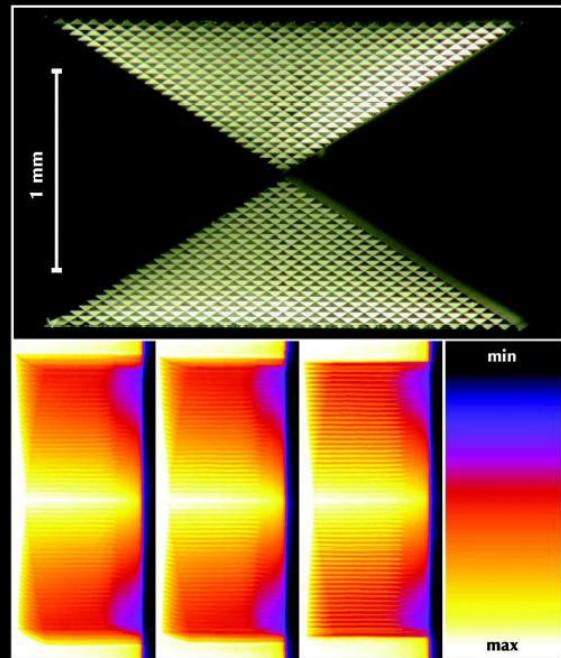
Spectroscopy

Imaging



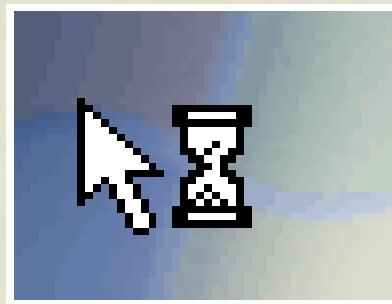
# Journal of Synchrotron Radiation

Editors: Å. Kvick, D. M. Mills and T. Ohta



journals.iucr.org  
International Union of Crystallography  
Blackwell Munksgaard

# CLESSIDRA

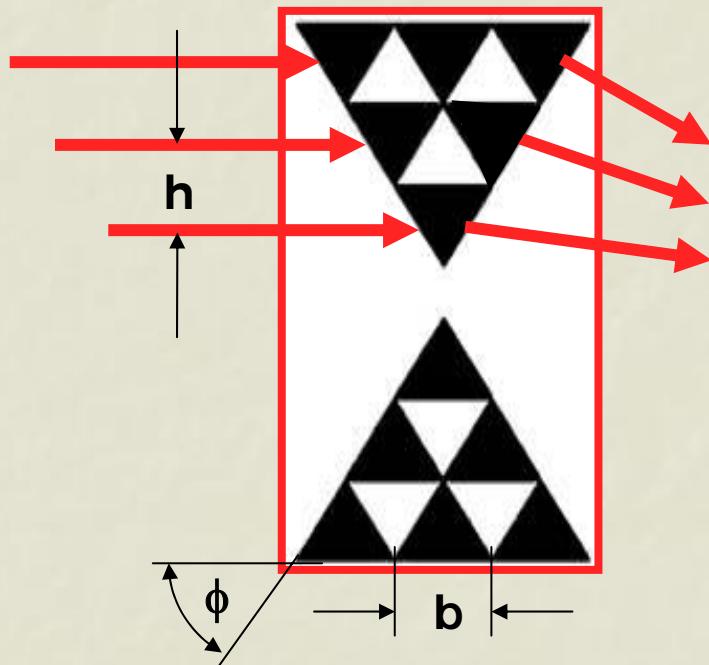


Obviously would be a linear transmission grating

in sufficiently spatially  
coherent incident beam

# Spatially incoherent incident beam

CLESSIDRA is an array of tiny refracting prisms



Deflection angle in prism

$$\Delta = \frac{2\delta}{\tan \phi} = \delta \frac{b}{h}$$

Distance to refractive focus

$$\Delta f = h$$

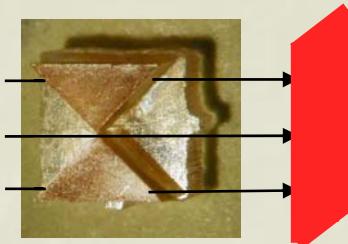
$$f_{ref} = \frac{h}{\Delta} = \frac{h \tan \phi}{2\delta} = \frac{h^2}{\delta b}$$

Can focus size be  $< h$ ? NO!

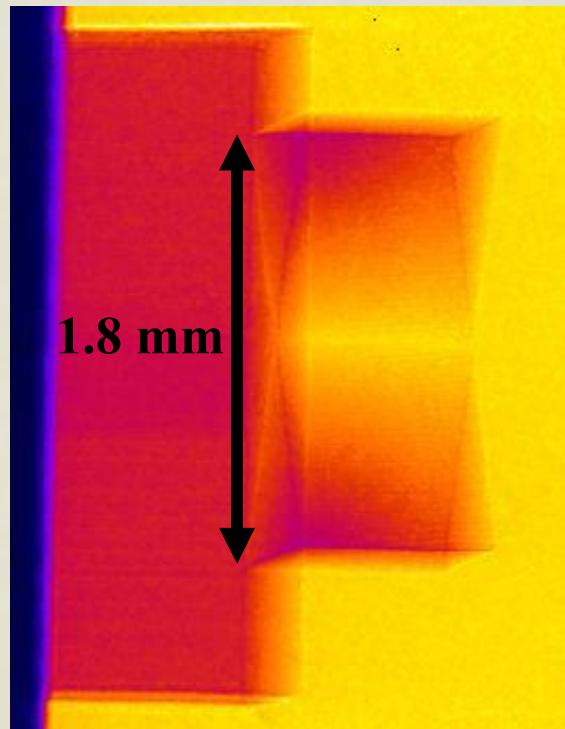
We can use perfect prisms!

# Rapidly alignable x-ray optics

Put it



Radiography



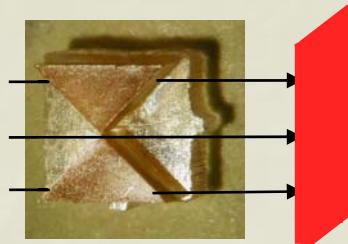
You see the  
clessidra shape



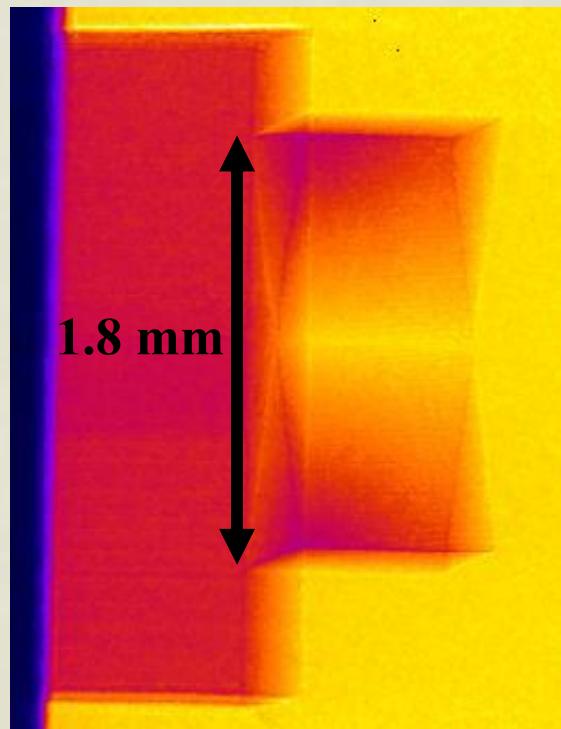
Adjust  
tilt, yaw, roll  
for sharp  
shadow

SYRMEP beamline, 12 keV photon energy, CCD camera 9  $\mu$ m pixel

# Rapidly alignable x-ray optics

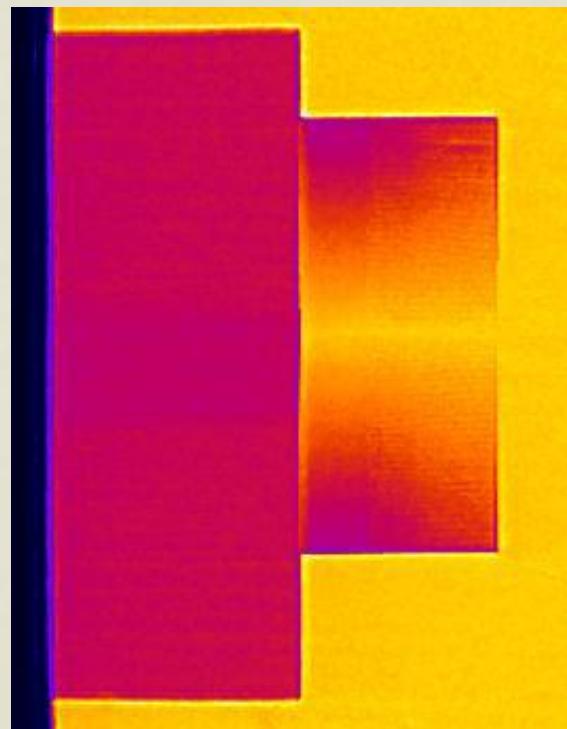


Radiography



You are done.

Now you can go  
to refractive  
focus position.

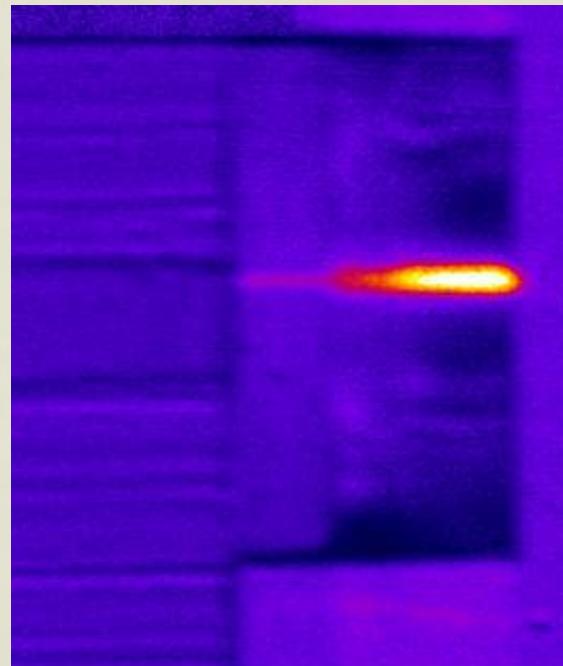
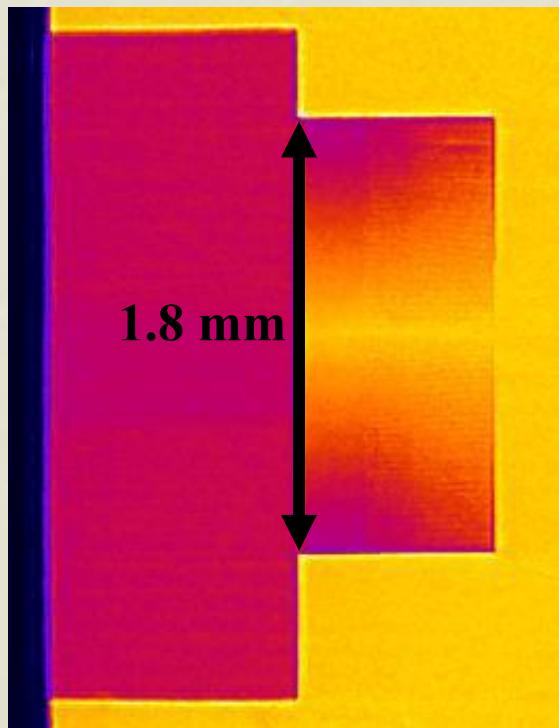


SYRMEP beamline, 12 keV photon energy, CCD camera 9  $\mu$ m pixel

# Rapidly alignable x-ray optics

10 m downstream  
from lens  
with  $h=12.83 \mu\text{m}$

Gain in focus is 6x  
Size is  $110 \mu\text{m}$  ( $\approx$  hair)  
lens efficiency = 25%



Same performance with  
120 mm long mirror  
with slope error <0.5”!



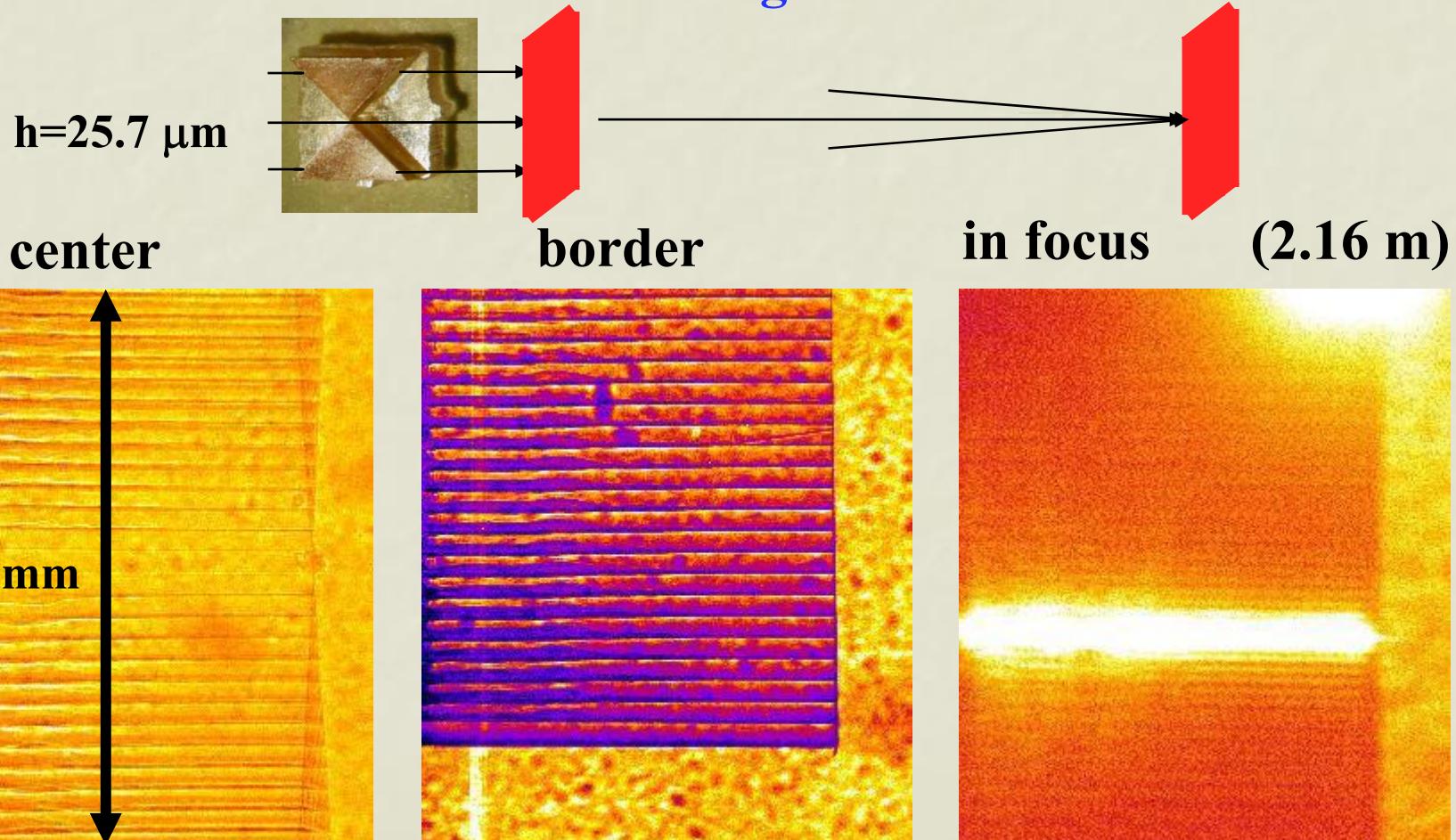
hair

See also Jark et al,  
JSR 15, 411 (2008)

SYRMEP beamline, 19.5 keV photon energy, CCD camera  $9 \mu\text{m}$  pixel

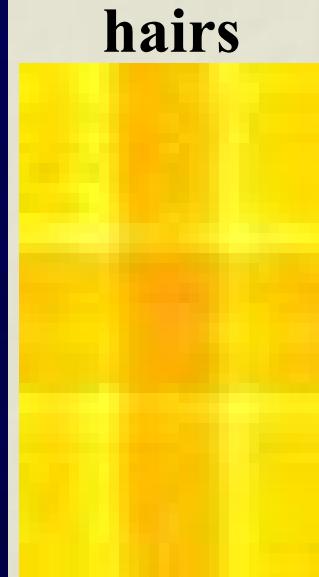
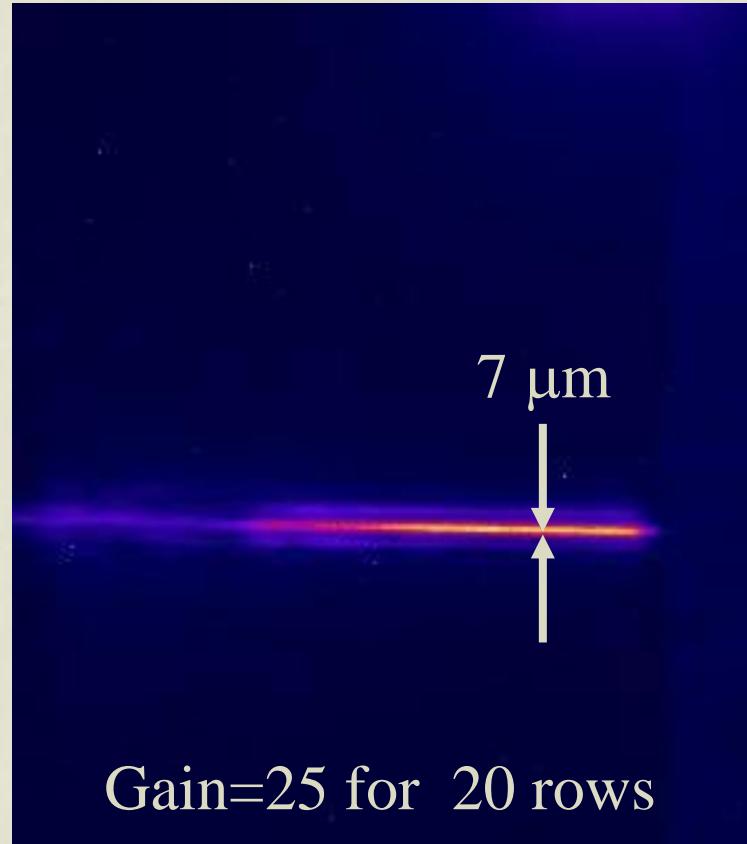
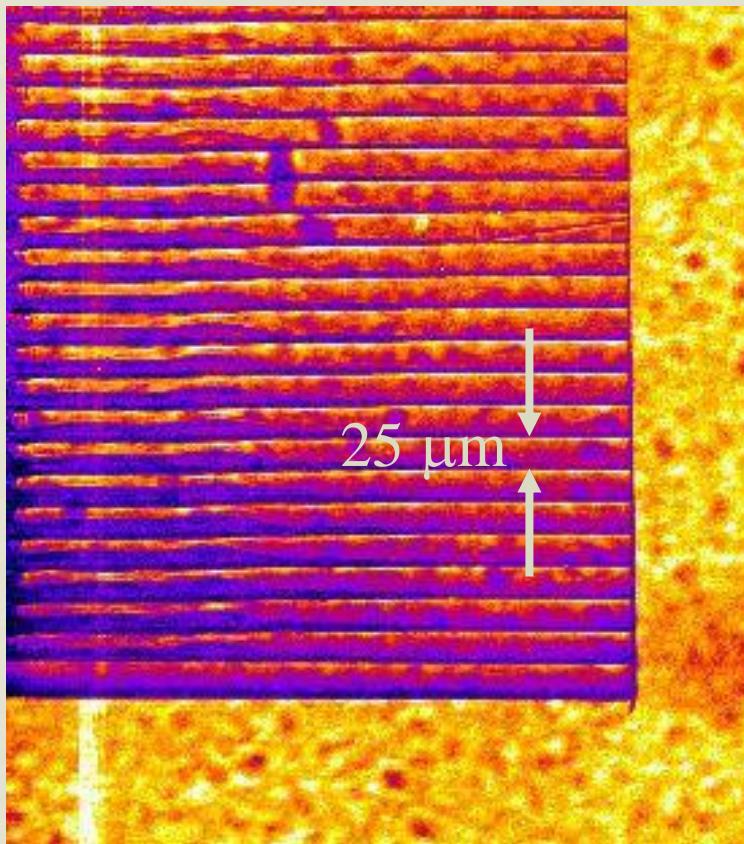
# Rapidly alignable x-ray optics

with better beam coherence and high resolution CCD



BM05(MOTB)@ESRF, 8 keV photon energy, CCD 0.65  $\mu\text{m}$  pixel

# Rapidly alignable x-ray optics

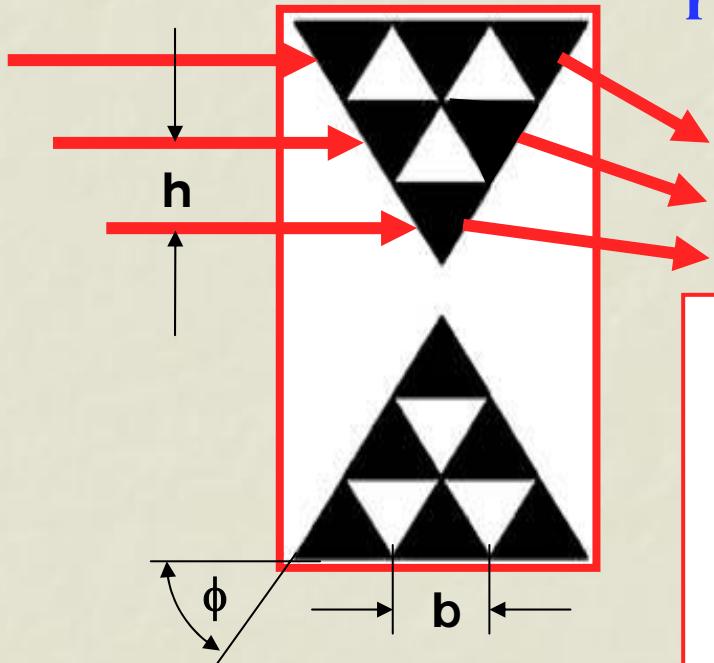


Is the focus size not correlated with prism height  $h$ ??

# Spatially COHERENT incident beam

In near field or Fresnel regime an object with periodic transmission function is re-imaged at the Talbot distances

$$D_{Tal,k/l} = \frac{kh^2}{l\lambda} \quad k, l \text{ integers, } \\ 1/l \text{ demagnification factor}$$



Now phase continuity required

$$b = D = \frac{m\lambda}{\delta}$$

fixing the refractive focal length to

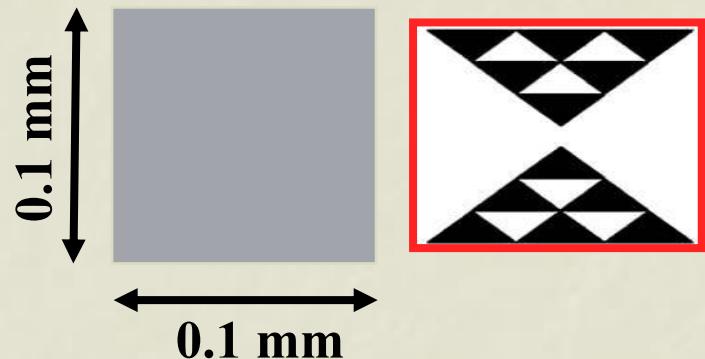
$$f = \frac{h^2}{\delta b} = \frac{h^2}{m\lambda} = D_{Tal,k=1/l=m}$$

Operation restricted to discrete wavelengths

# Some numbers

**f=1 m@ 8 keV  
 $(\lambda=0.155 \text{ nm})$**

$$f = \frac{h^2}{m\lambda}$$

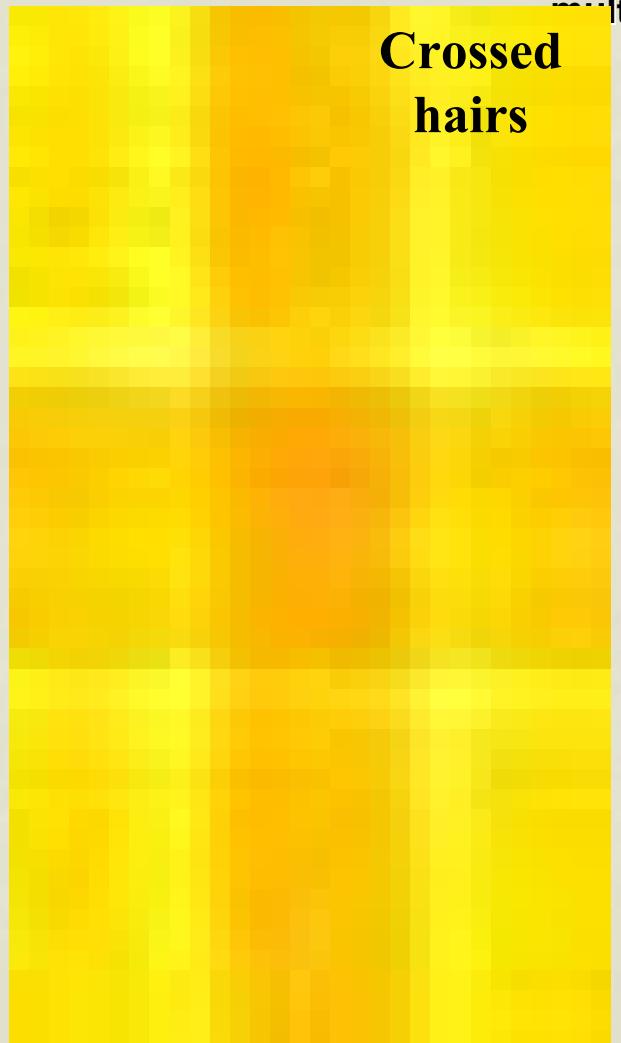


$m=1$

**h independent of material:  $h= 12.45 \mu\text{m}$**

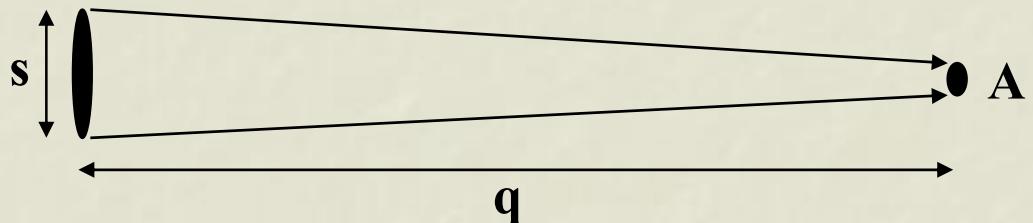
Needs lithography (we have one of few beamlines for deep x-ray lithography (DXRL) at ELETTRA)

in resists (pmma or SU8)       $b=36.7 \mu\text{m}$



# Some numbers

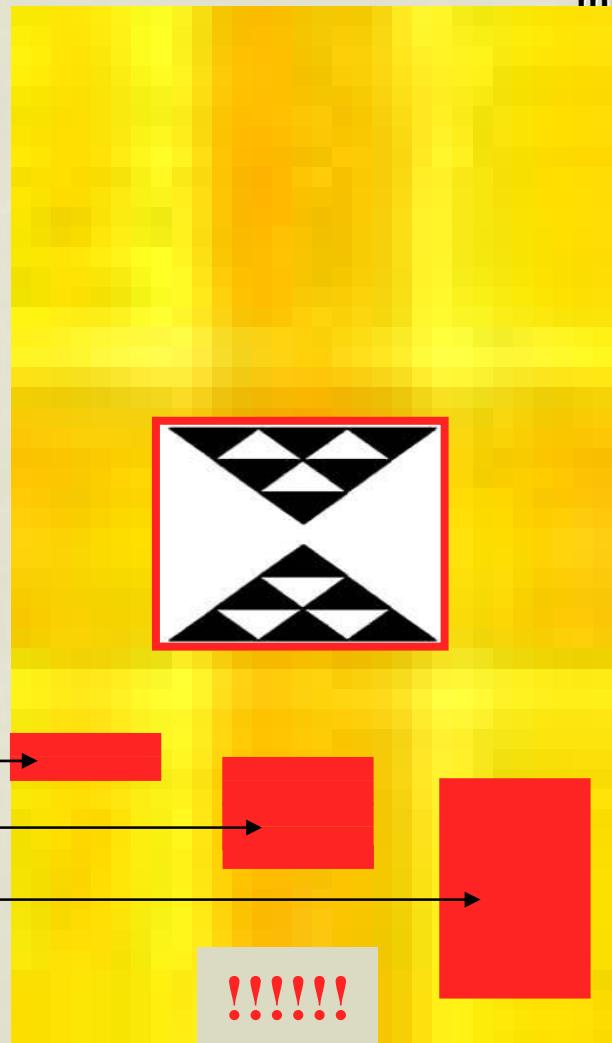
Spatially coherently  
illuminated area:  
 $A=0.44\lambda q/s$



8 keV or  $\lambda=0.155$  nm

SYRMEP (q=23 m, s=90 $\mu\text{m}$ ):	$A=17 \mu\text{m}$
BM05 (q=53 m, s=85 $\mu\text{m}$ ):	$A=42 \mu\text{m}$
ID22 (q=40 m, s=30 $\mu\text{m}$ ):	$A=91 \mu\text{m}$

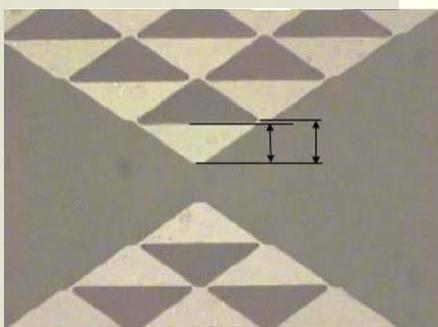
$q=100\text{m}, s=23 \mu\text{m}:$        $A=300 \mu\text{m}$



# Quality control: transmission

**filling: 50%**

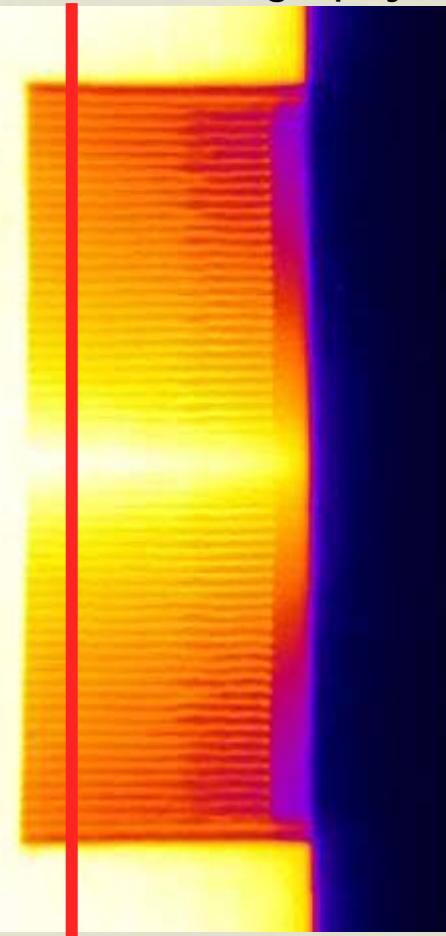
pmma  
 $h=25.7 \mu\text{m}$   
 $m=2, N=29$



$L_{\text{exp}} = 1.612 \text{ mm}$   
at 8.5 keV

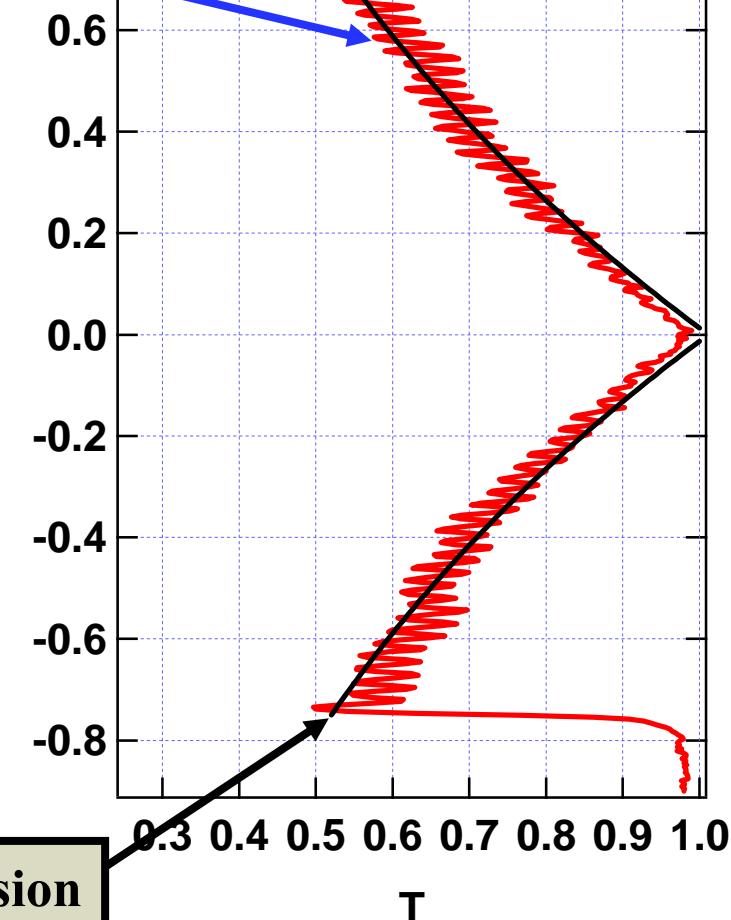
T variation in  
last row  
0.25 ---- 1.0

Contact radiography



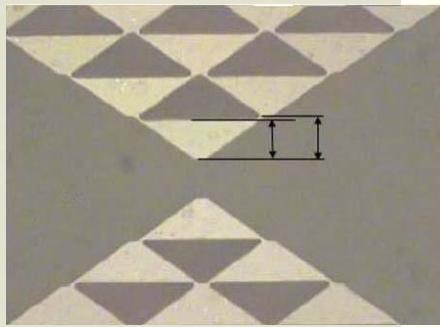
expected average transmission

**damping:  
CCD cross talk**



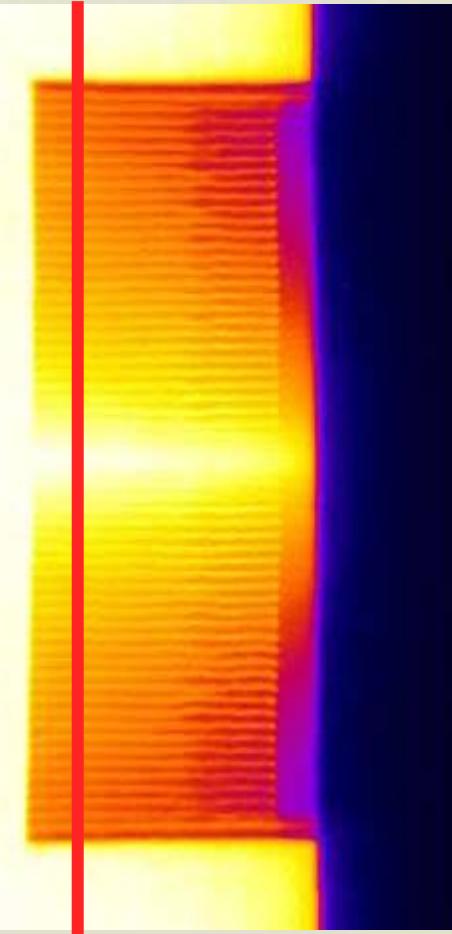
# Quality control: refraction efficiency

Slit scan (0.1 mm):  
Flux integrated over  
50 μm in focus

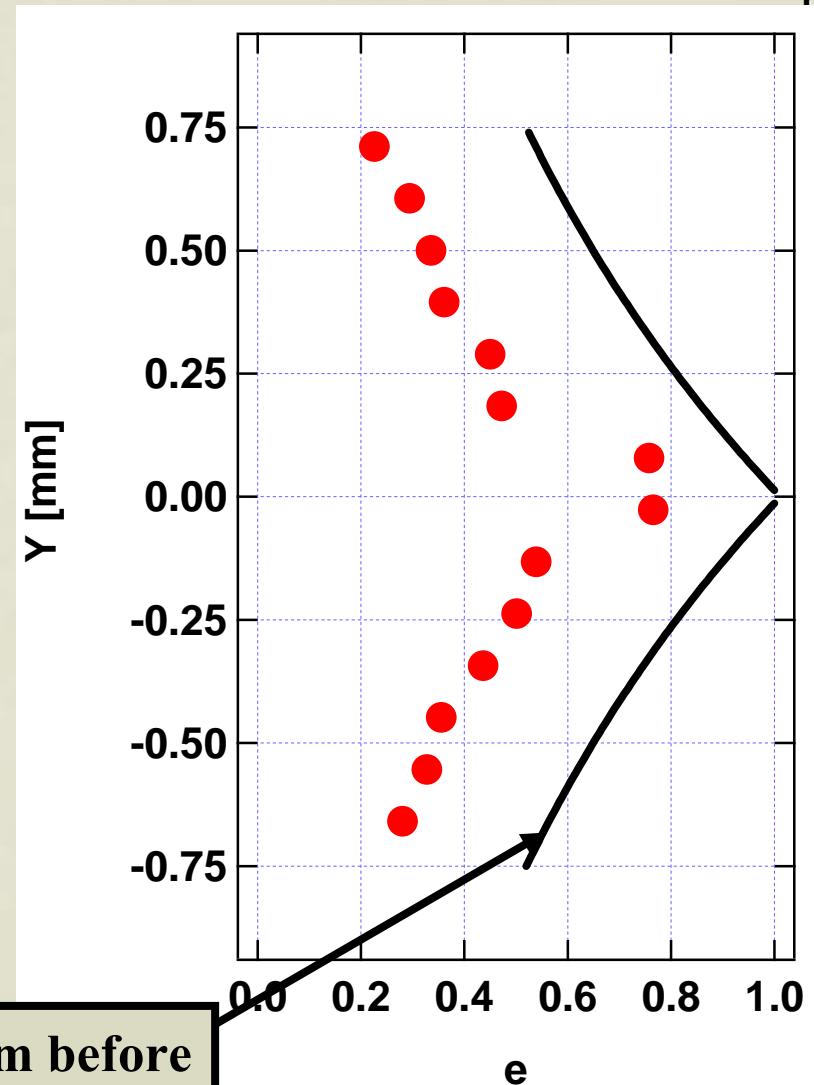


**Relative efficiency**  
**>50%**  
**out to border**

Rounding in  
connected  
prism tips



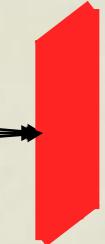
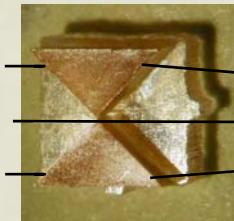
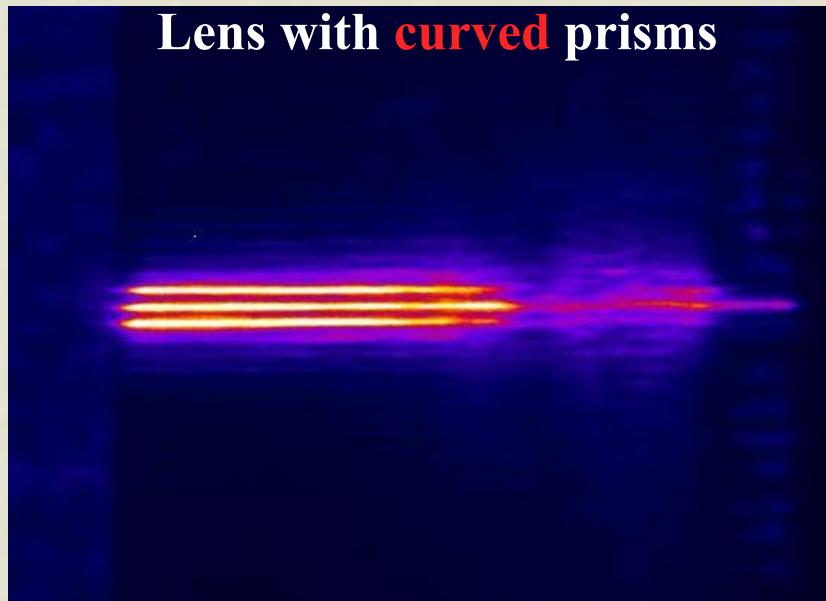
average transmission from before



# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows



Peak width 4.0  $\mu\text{m}$

**“Coherent”  
illumination**

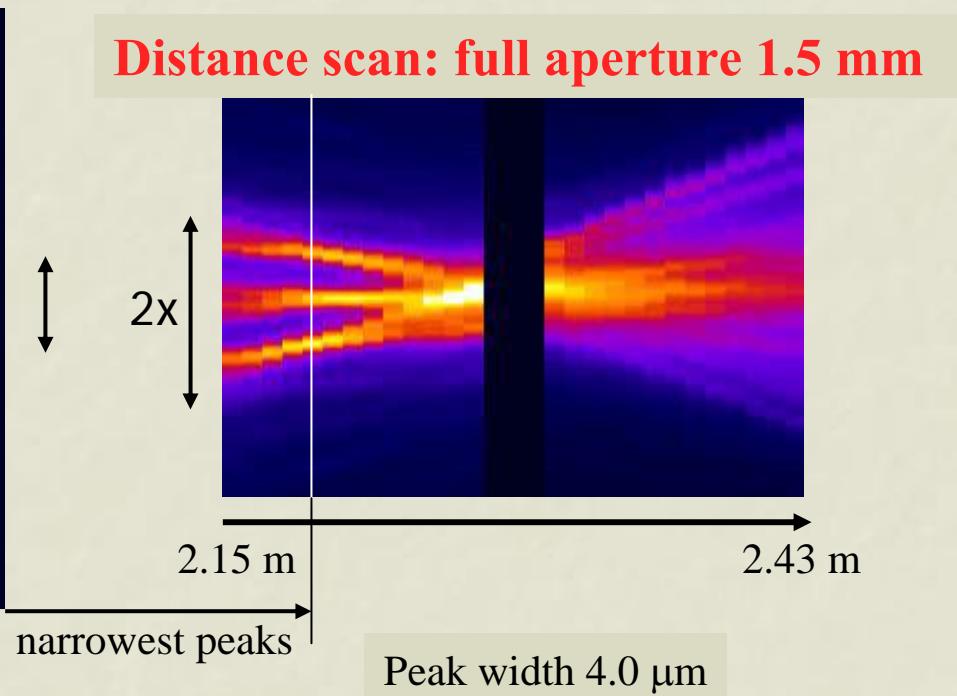
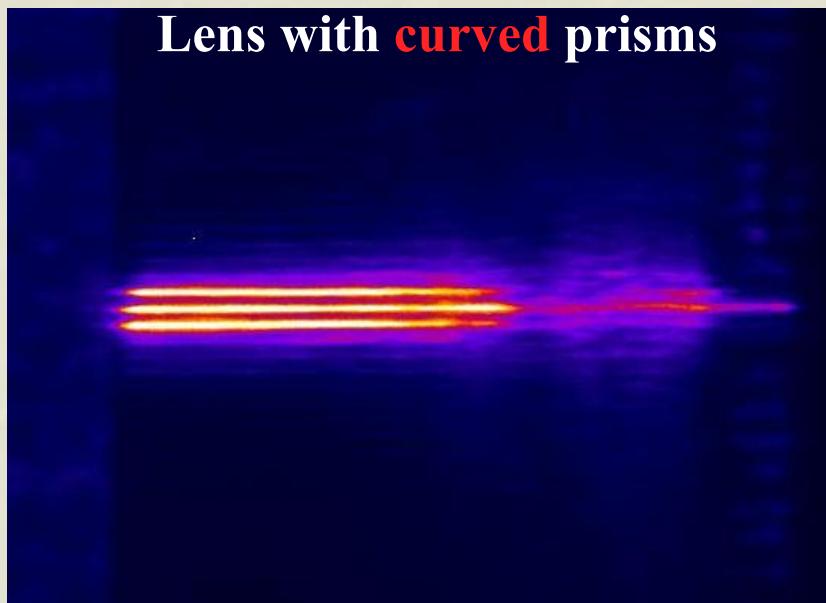
**8.0 keV  
detuned**

**MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel**

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows



**“Coherent”  
illumination**

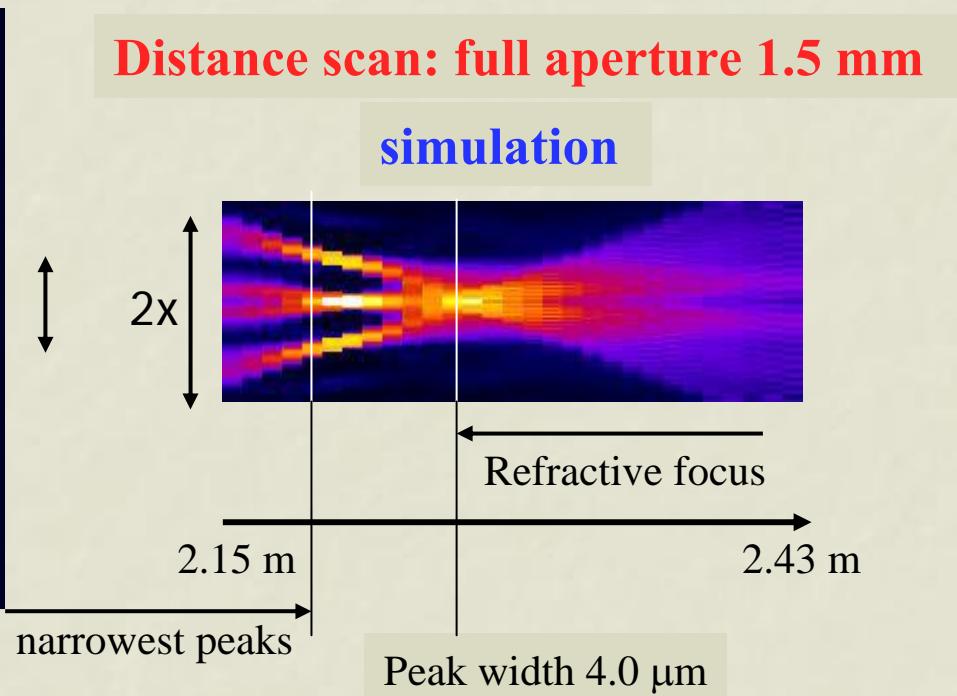
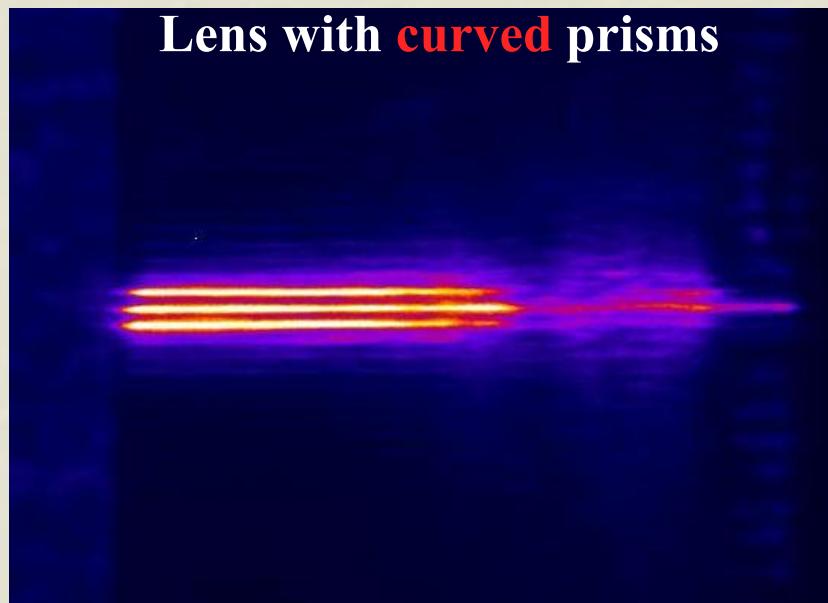
8.0 keV  
detuned

MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows



**“Coherent” illumination**

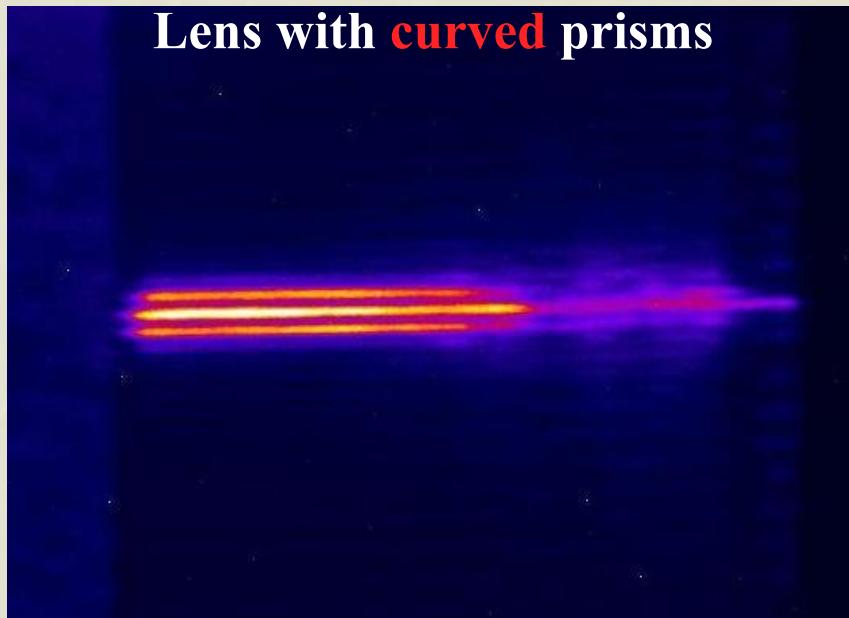
8.0 keV  
detuned

MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows



Lens with **curved** prisms

Another run (1 year later):  
**New monochromator**  
**New E calibration**

**Vibrations:**  
**Larger virtual source**  
→Wider peaks (expect 6.5  $\mu\text{m}$ )  
→reduced spatial coherence  
(from 42  $\mu\text{m}$  to 21  $\mu\text{m} < h$ )

Peak width 7.3  $\mu\text{m}$

**“Coherent”**  
illumination

**8.0 keV**  
**detuned**

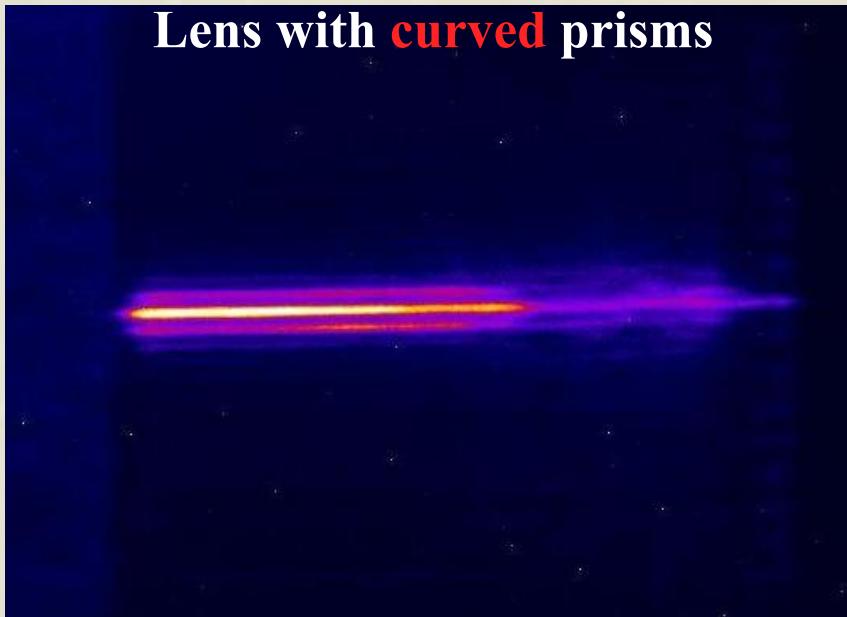
**MOTB@ESRF (BM05-beamline)**  
**CCD with 0.645  $\mu\text{m}$  equivalent pixel**

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows

Lens with **curved** prisms



Peak width 6.6  $\mu\text{m}$

**“Coherent”  
illumination**

**7.9 keV  
better  
tuned**

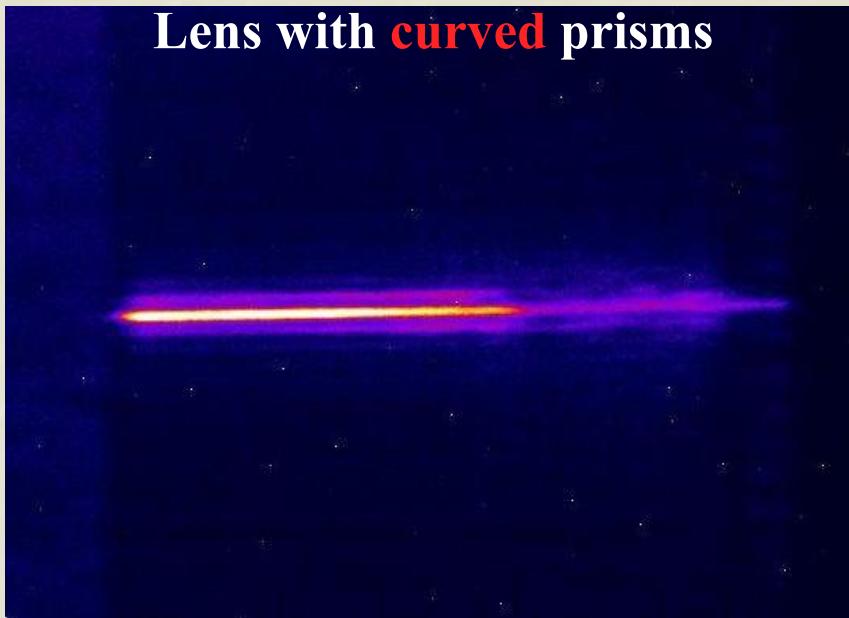
**MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel**

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows

Lens with **curved** prisms



Peak width 5.7  $\mu\text{m}$

**“Coherent”  
illumination**

7.7 keV  
best  
tune

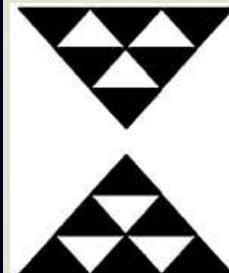
MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel

# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows

Lens with **perfect** prisms



Peak width 6.5  $\mu\text{m}$

**“Coherent”  
illumination**

**7.9 keV  
best  
tune**

**MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu\text{m}$  equivalent pixel**

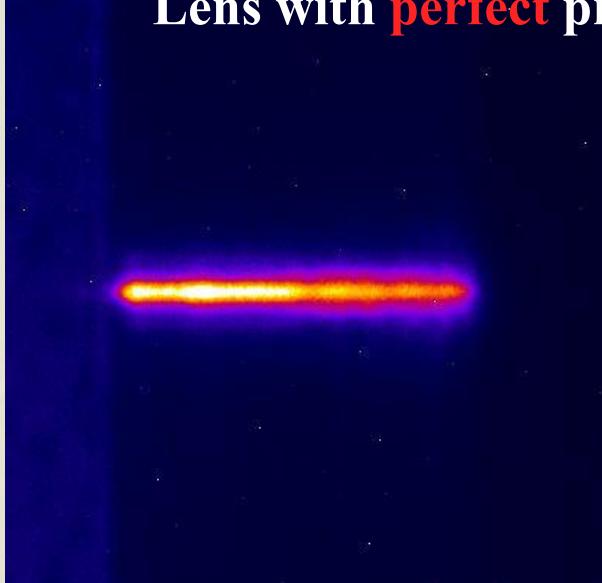
# Optimising the wavelength

pmma,  $m=2$   
 $h=25.7 \mu\text{m}$

illuminating 1.0 mm centered: 40 rows

Focusing horizontal source size

Lens with perfect prisms



reduced spatial coherence  
(from  $21 \mu\text{m}$  to  $13 \mu\text{m} < h$ )

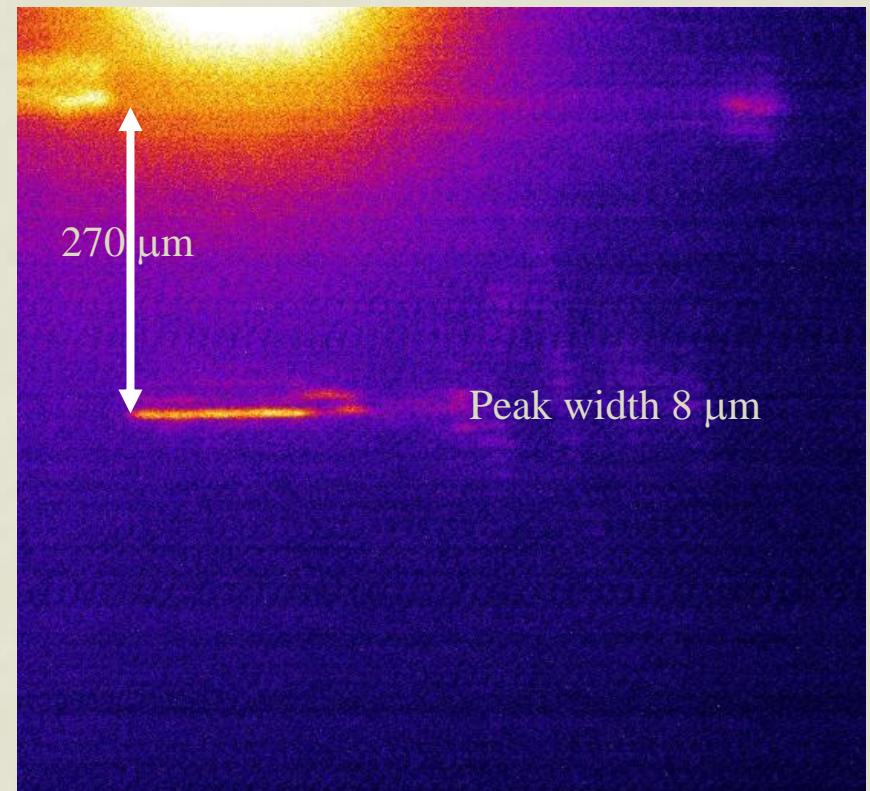
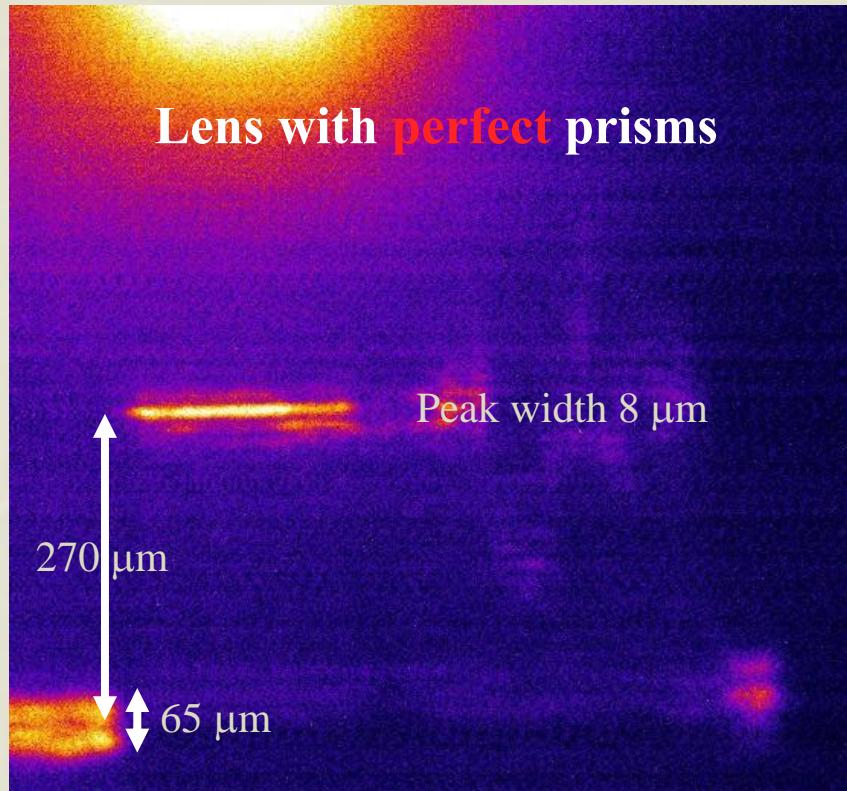
Focus size is  $12.5 \mu\text{m}$  =  
expected demagnified source image  
But also  $h/2$

7.9 keV  
best  
tune

MOTB@ESRF (BM05-beamline)  
CCD with  $0.645 \mu\text{m}$  equivalent pixel

# Refraction efficiency

vertical focusing: illuminating 65  $\mu$ m (3 rows) at 270  $\mu$ m off-axis



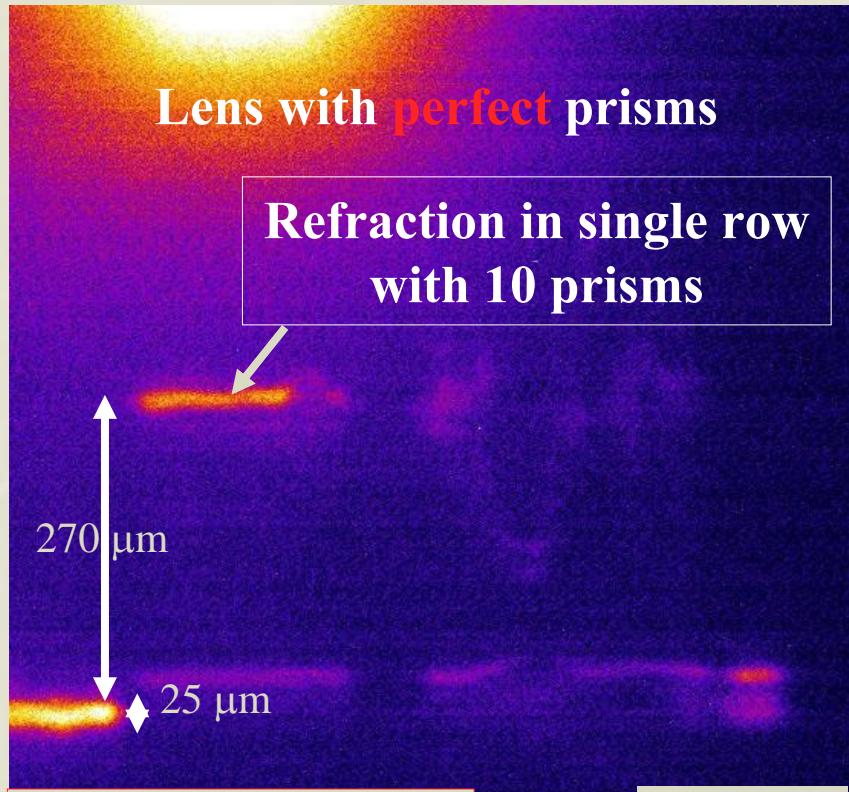
“Coherent”  
illumination

7.9 keV  
best  
tune

MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu$ m equivalent pixel

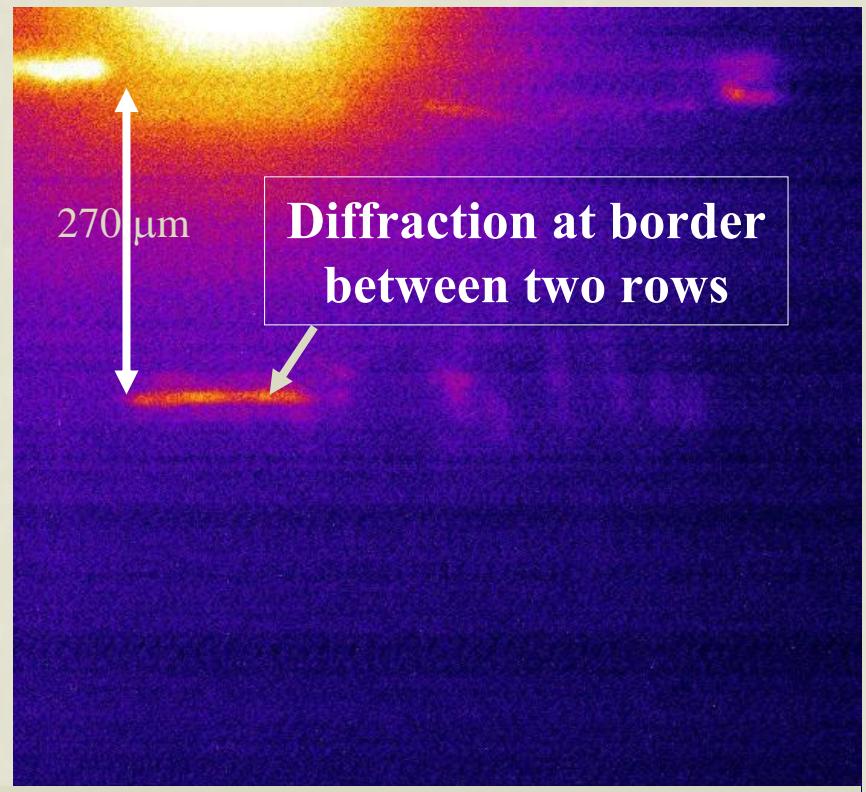
# Refraction efficiency

vertical focusing: illuminating 25  $\mu$ m (1 row) at 270  $\mu$ m off-axis



**“Coherent” illumination**

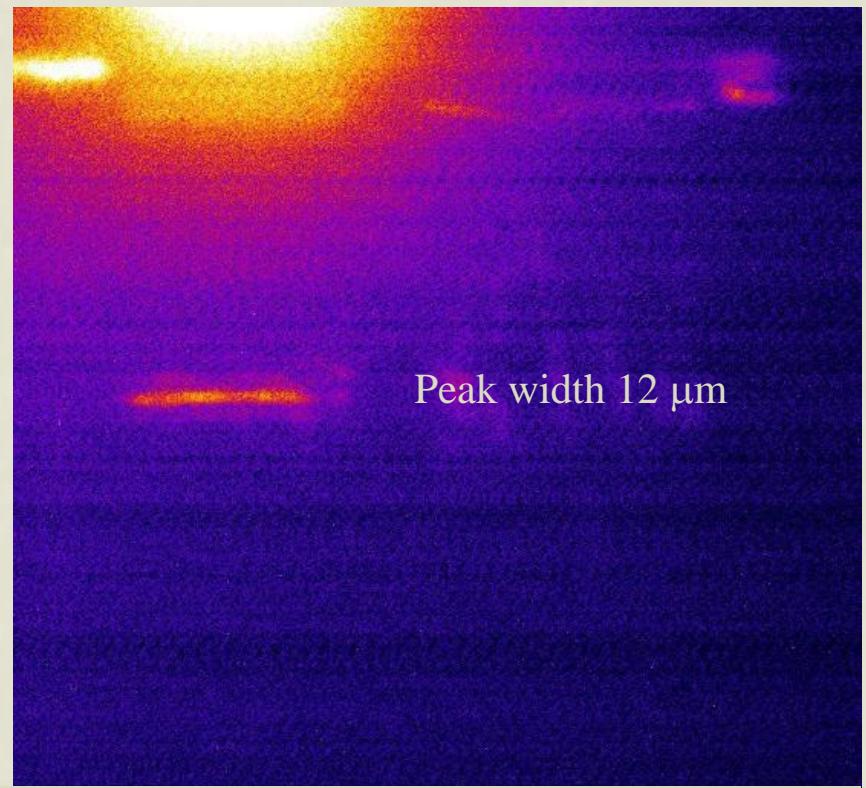
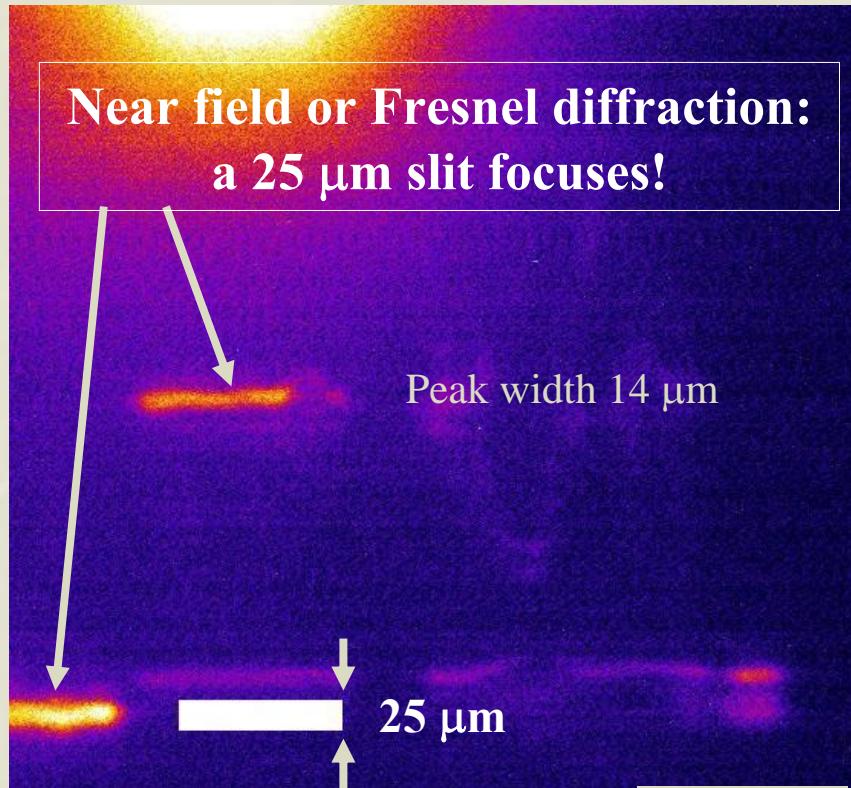
7.9 keV  
best tune



MOTB@ESRF (BM05-beamline)  
CCD with 0.645  $\mu$ m equivalent pixel

# Refraction efficiency

vertical focusing: illuminating 25  $\mu$ m (1 row) at 270  $\mu$ m off-axis



**“Coherent”  
illumination**

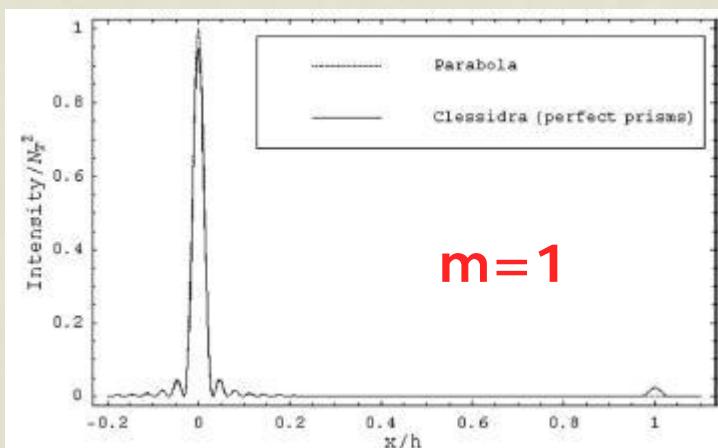
7.9 keV  
best  
tune

# Outlook

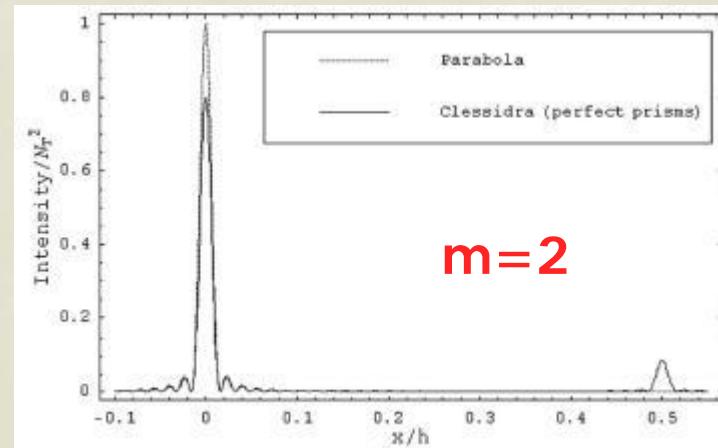
De Caro and Jark, JSR 15, 176 (2008):

Found an analytical solution for the intensity distribution in focal plane for completely spatially coherent illumination!

Diffraction limited focus size identical for CLESSIDRA and concave parabolic lenses of same aperture: for aberrations corrected prisms  
AND for perfect prisms with  $m=1$  and  $m=2$ !



Reduction of maximum : 5%



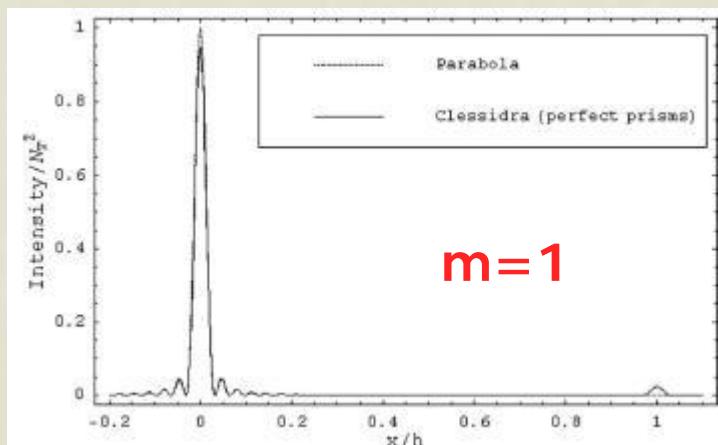
Reduction of maximum : 20%

# Outlook

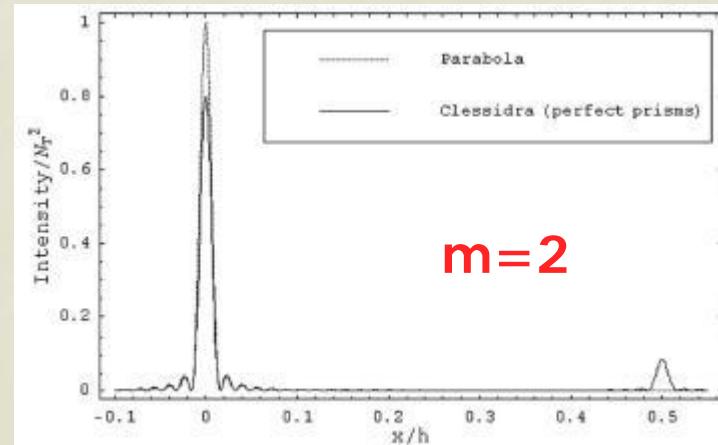
De Caro and Jark, JSR 15, 176 (2008):

Perfect prisms introduce periodic wavefield distortion into transmitted field. Peak-valley amplitude of distortion is  $\lambda/8$  for  $m=1$  and  $\lambda/4$  for  $m=2$ !  
 The Rayleigh criterion for diffraction limited optics allows  $<\lambda/4$  distortion!

Moderate loss of intensity into well localised secondary diffraction peaks.  
 To be blocked with pinholes upstream of focus.



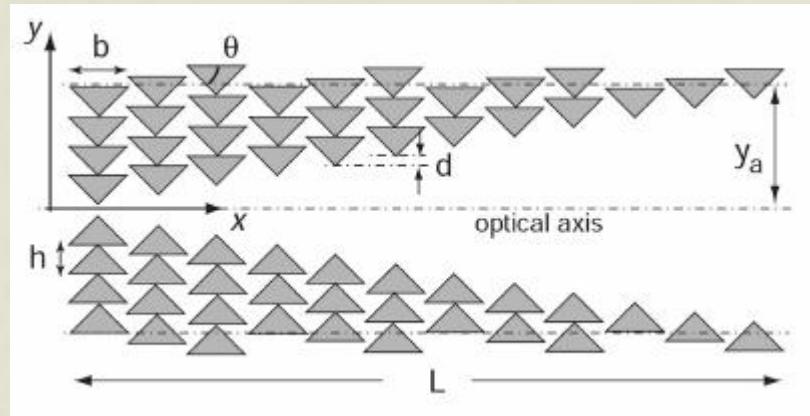
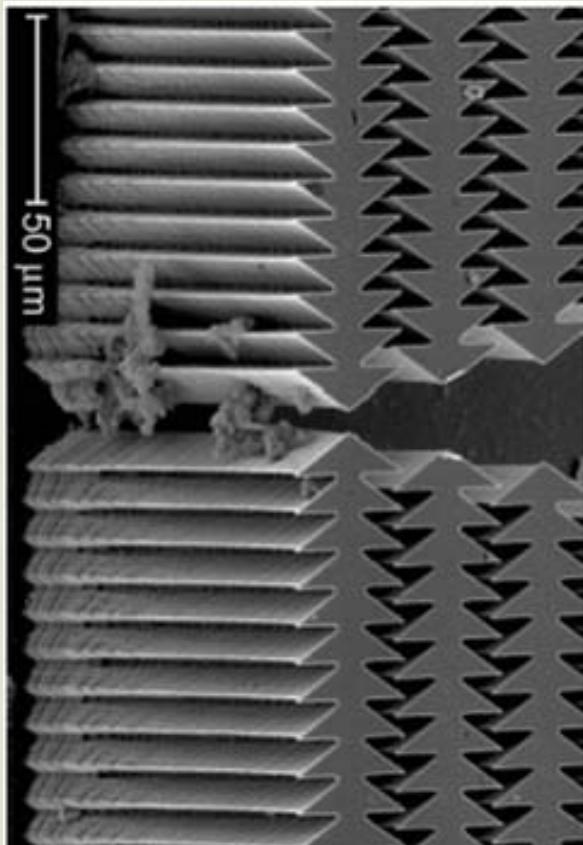
Reduction of maximum : 5%



Reduction of maximum : 20%

# Outlook: new concepts

B. Cederstroem et al, JSR 12, 340 (2005)



More absorbing,  
less distorting,  
larger peak  
separation, shorter  
focal length

problems in tips

# Outlook: disconnect

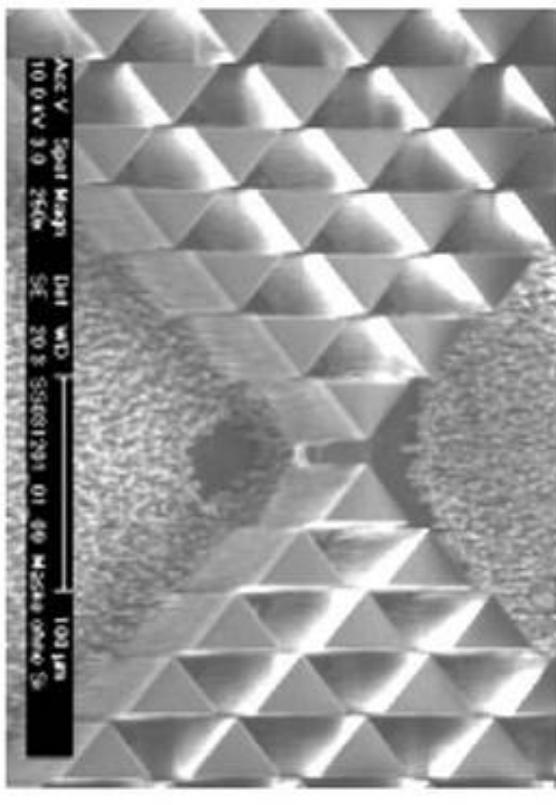
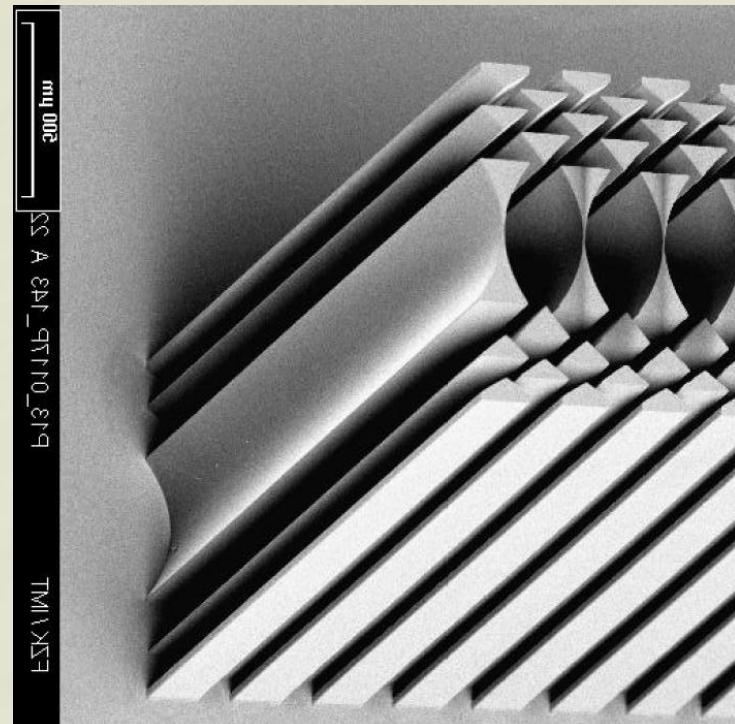


Fig. 7: SEM image of a CVD diamond X-ray lens (section view).  
Abb. 7: REM-Aufnahme einer Röntgenlinse aus CVD-Diamant (Ausschnitt).

IAF, Fraunhofer, Freiburg



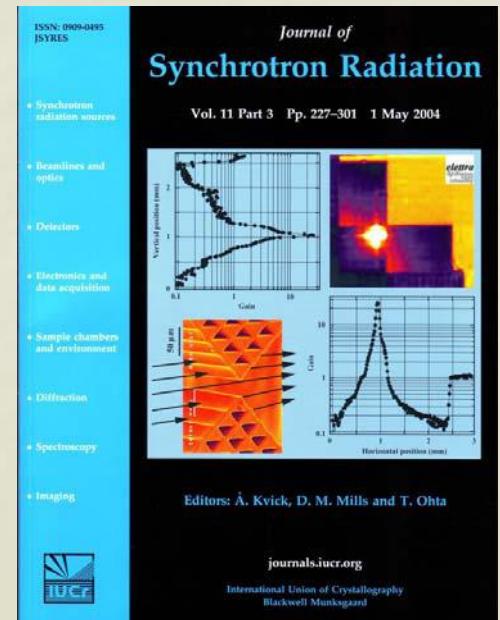
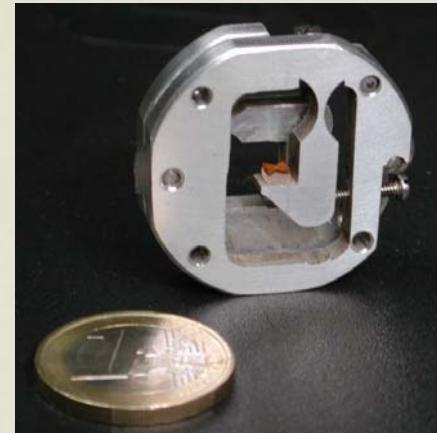
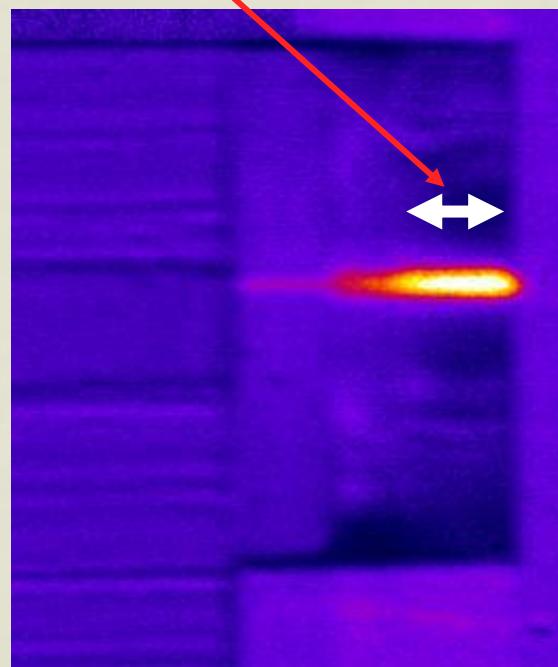
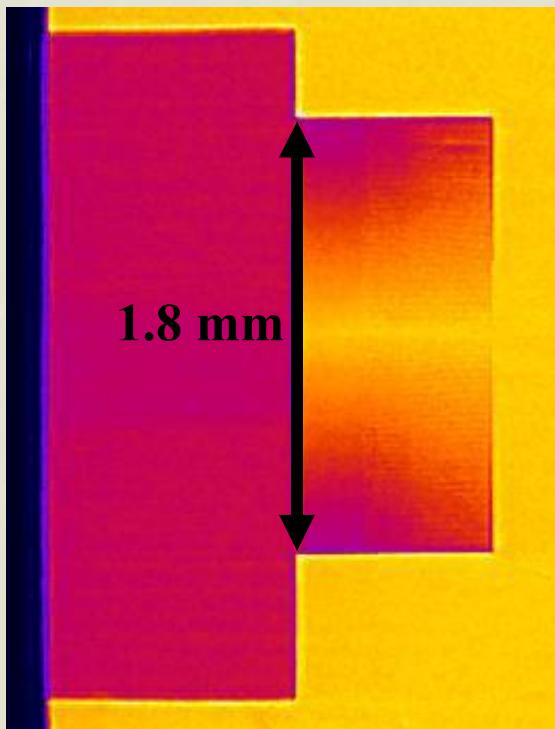
IMT @ FZK, Karlsruhe

get better tips with reduced rigidity

# Outlook: depth/aperture match

This was for  $h=12.83 \mu\text{m}$

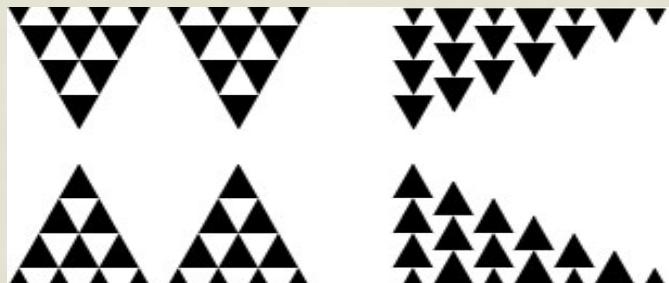
Aperture is  $140^*\text{h}$   
Etching depth is only  $25^*\text{h}$



# Conservative outlook

Take  $A=25*h$  matched to depth of  $25*h$ , as shown before

Stack M=2 or Cederstroem prism array



$h=12 \mu\text{m}$ :  $A=0.3 \text{ mm}$  and  $f=0.46 \text{ m}$  @ 8 keV ( $\lambda=0.155 \text{ nm}$ ).

Spatial resolution limit  $r=0.88*\lambda*f/A$   $r=210 \text{ nm}!$

!!needs spatially coherent beam, e.g.  $q=100 \text{ m}$  for  $s=23 \mu\text{m}!!$

image could be 110 nm

Average transmission >80%/>60% for one/bi-dimensional lens

# More ambitious outlook

Take  $A=50*h$  matched to depth of  $50*h$

Stack  $M=2$  or Cederstroem prism array



$h=6 \mu\text{m}$ ,  $A=0.3 \text{ mm}$  and  $f=0.116 \text{ m}$  @ 8 keV ( $\lambda=0.155 \text{ nm}$ ).

Spatial resolution limit  $r=0.88*\lambda*f/A$   $r=53 \text{ nm}!$

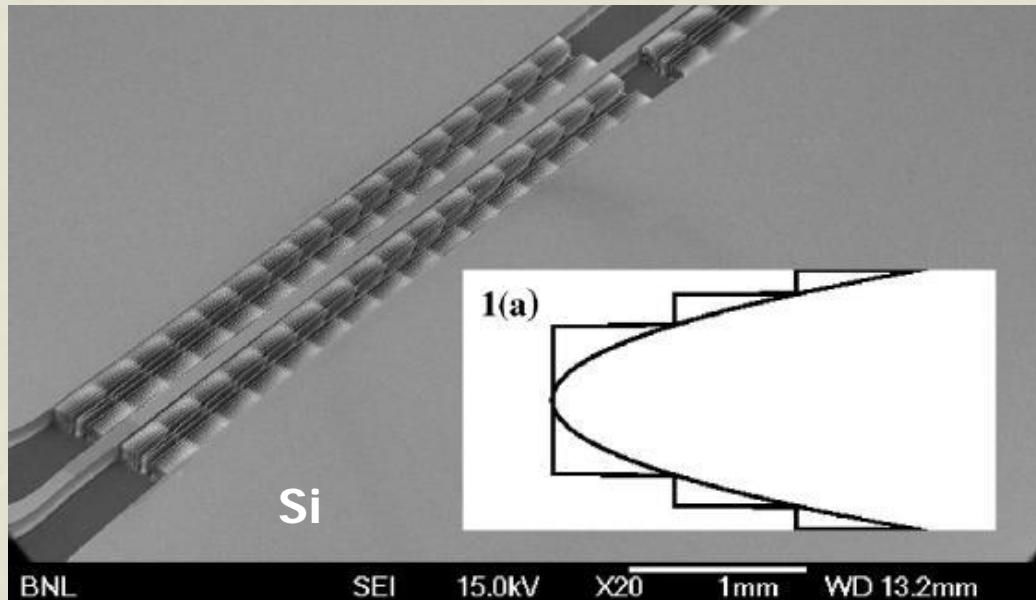
!!needs spatially coherent beam, e.g.  $q=100 \text{ m}$  for  $s=23 \mu\text{m}!!$

image could be 27 nm

Average transmission  $\approx 70\%/\approx 50\%$  for one-/bi-dimensional lens

# Fresnel lens outlook

Evans-Lutterodt et al, PRL 99 (13),  
134801 (2007)



Arrived already at  
 $A=0.3$  mm,  $f=0.1$  m  
image size <<320 nm fwhm  
Stein et al, JVST B26, 122 (2008),  
priv. comm. Evans-Lutterodt

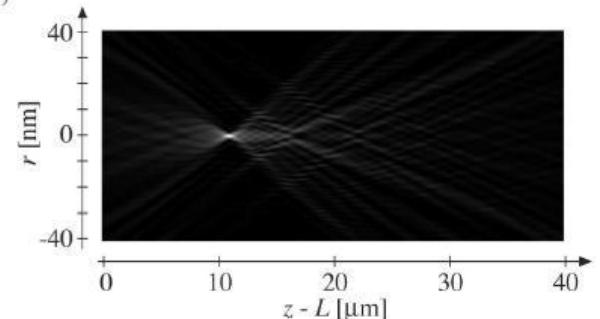
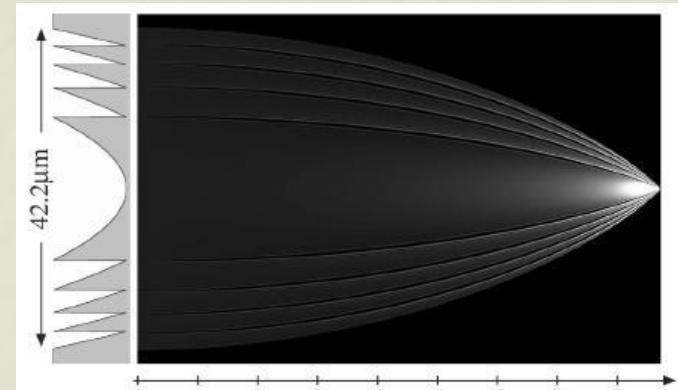
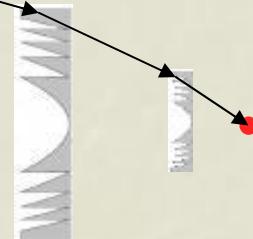
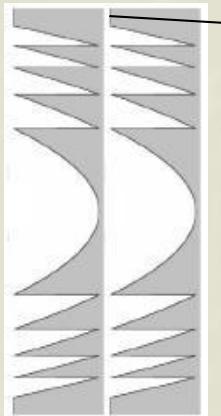
Only center segment is  $>6 \mu\text{m}$ !

Relative efficiency  $\approx 25\%$   
for segments  $\approx 1.7 \mu\text{m}$   
and  $<10\%$  for  $\approx 0.7 \mu\text{m}$

In Si better shape fidelity at smaller dimensions than in photoresist!  
In turn etch depth limitation for RIE at 0.1 mm?

# Fresnel lens outlook: adiabatic

Schroer et al, PRL 94, 054802 (2005)



Follow adiabatically shrinking beam size

In 1166 lenses

Lens thickness:  $37.8 \mu\text{m} \dots 0.100 \mu\text{m}$

Lens aperture:  $42.2 \mu\text{m} \dots 0.224 \mu\text{m}$

Outer segment:  $4.5 \mu\text{m} \dots 0.024 \mu\text{m}$

focus  $r=2.21 \text{ nm}$  @ 27.6 keV

# Thank you for help

**DXRL:**

**Marco Matteucci, Fréderic Pérennès, Benedetta Marmiroli**

**IMM (Mainz):** **Laurence Singleton, Abdi Tunayar (EU action: EMERGE)**

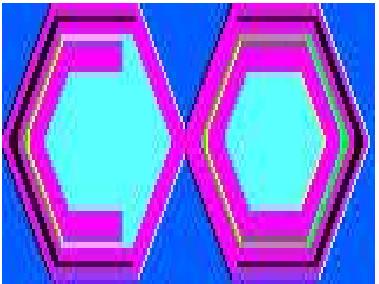
**SYRMEP:** **Lucia Mancini, Giuliana Tromba, Luigi Rigon, Francesco Montanari, Ralf Hendrick Menk, Diego Dreossi**  
**workshop:** **Gilio Sandrin, Ivan Cudin**

**IC-CNR:** **Liberato De Caro**

**ESRF-ID22:** **Jean Susini, Andrea Somogyi, Remi Tucoulou, Sylvain Bohic**  
**ESRF-BM05:** **Anatoly Snigirev, Irina Snigireva**

**More about project:**

<http://www.elettra.trieste.it/experiments/beamlines/microfluo/docs/clessidra.pdf>



# Carolyn MacDonald

## UAlbany Center for X-ray Optics

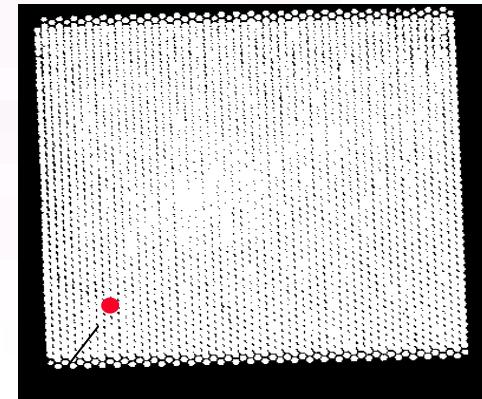
### Outline

#### Structure of Polycapillaries

- Physics of Reflection, endin imits
- iver ence
- Ali nment and Characteri ation
  - Source An le
  - ransmission vs Ener y
  - Spot Si e
- Gain and liouville s heorem
- efect Analysis
- Applications
  - MicroXR
  - XR
  - Astronomy
  - herapy

# Polycapillary Optics

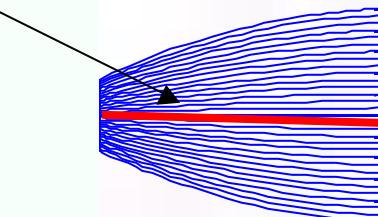
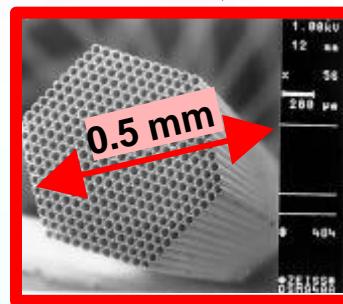
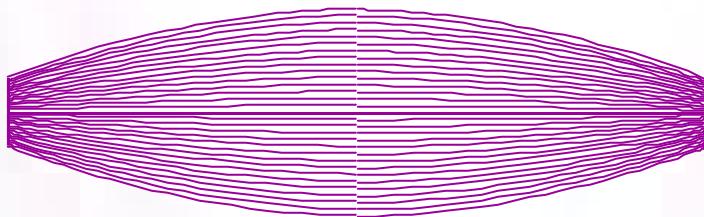
## COLLIMATING



multifiber

50 mm x 50 mm output  
250 mm input focal len th  
12  $\mu\text{m}$  channel

## FOCUSING



monolithic

## How do they work? Maxwell's equations for a non-magnetic insulator:

$$\left. \begin{array}{l} \nabla \cdot \vec{E} = 0 \\ \nabla \cdot \vec{B} = 0 \\ \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \nabla \times \vec{B} = \mu_0 \epsilon \frac{\partial \vec{E}}{\partial t} \end{array} \right\} \Rightarrow$$

$$\frac{\partial^2 \vec{E}}{\partial t^2} = \frac{1}{\mu_0 \epsilon} \nabla^2 \vec{E}$$

$$v = \frac{1}{\sqrt{\mu_0 \epsilon}} = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \sqrt{\frac{\epsilon_0}{\epsilon}} = \frac{c}{n}$$

$\Rightarrow$  n, index of refraction =  $\sqrt{\frac{\epsilon}{\epsilon_0}}$

So, given an incident plane wave of the form:

$$\vec{E} = \vec{E}_0 e^{i\omega t}$$

we expect a response

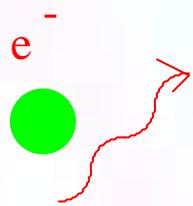
$$\vec{E} = \epsilon \vec{E} = \epsilon_0 \vec{E} + \vec{P}$$

hence

$$\vec{E} = \epsilon_0 \vec{E} + \vec{P} \Rightarrow \epsilon = \epsilon_0 + \frac{\vec{P}}{\vec{E}}$$

need to model  
the response,  $\vec{P}$   
of the material  
to the EM wave

## Free Electrons in one dimension:



$$E = E_0 \cos \omega t$$

$$P = \quad x$$

number of  
electrons per  
volume

$$F = m\ddot{x} = qE = qE_0 \cos \omega t$$

$$x = x_0 \cos \omega t$$

$$\Rightarrow -m\omega^2 x_0 = qE_0 \Rightarrow x_0 = \frac{-qE_0}{m\omega^2}$$

$$P_0 = Nqx_0 = \frac{-Nq^2}{m\omega^2} E_0$$

charge on an  
electron

$$\Rightarrow \epsilon = \epsilon_0 + \frac{-}{m\omega^2} \frac{2}{\omega^2} = \epsilon_0 \left( 1 - \frac{\frac{2}{m\epsilon_0}}{\omega^2} \right)$$

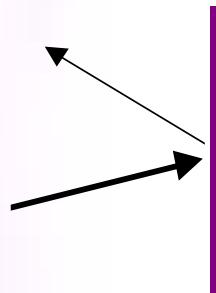
$$\epsilon = \epsilon_0 \left( 1 - \frac{\omega_p^2}{\omega^2} \right)$$

x displacement of  
the electron due to  
the electric field

# Index of Refraction

$$n = \sqrt{\frac{\epsilon}{\epsilon_0}} = \sqrt{1 - \frac{\omega_p^2}{\omega^2}} \approx 1 - \frac{1}{2} \frac{\omega_p^2}{\omega^2} = 1 - \delta \Rightarrow \delta = \frac{1}{2} \left( \frac{30 \text{ eV}}{10 \text{ eV}} \right)^2 \approx 4.5 \times 10^{-6}$$

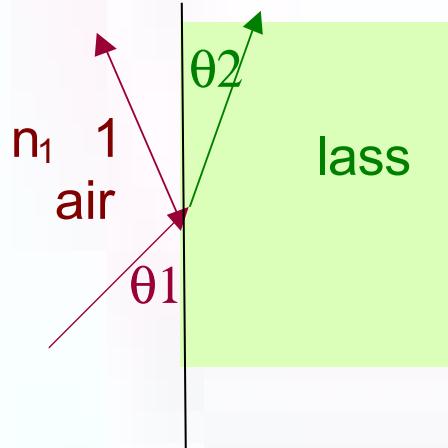
Consequences for normal incidence mirror:



$$R(\theta = 0) = \left( \frac{n_1 - n_2}{n_1 + n_2} \right)^2 = \frac{\delta^2}{2} \approx 10^{-11}$$



Total External Reflection



$$n_1 \sin(90 - \theta_1) = n_2 \sin(90 - \theta_2)$$

$$(1) \cos(\theta_1) = (1 - \delta) \cos(\theta_2)$$

$$(1) \cos(\theta_c) = (1 - \delta) \cos(0) \Rightarrow 1 - \frac{\theta_c^2}{2} \doteq 1 - \delta \Rightarrow \theta_c \doteq \sqrt{2\delta}$$

$$\theta_c = \frac{\omega_p}{\omega} \approx 3 \times 10^{-3} \quad R=1$$



# Damping

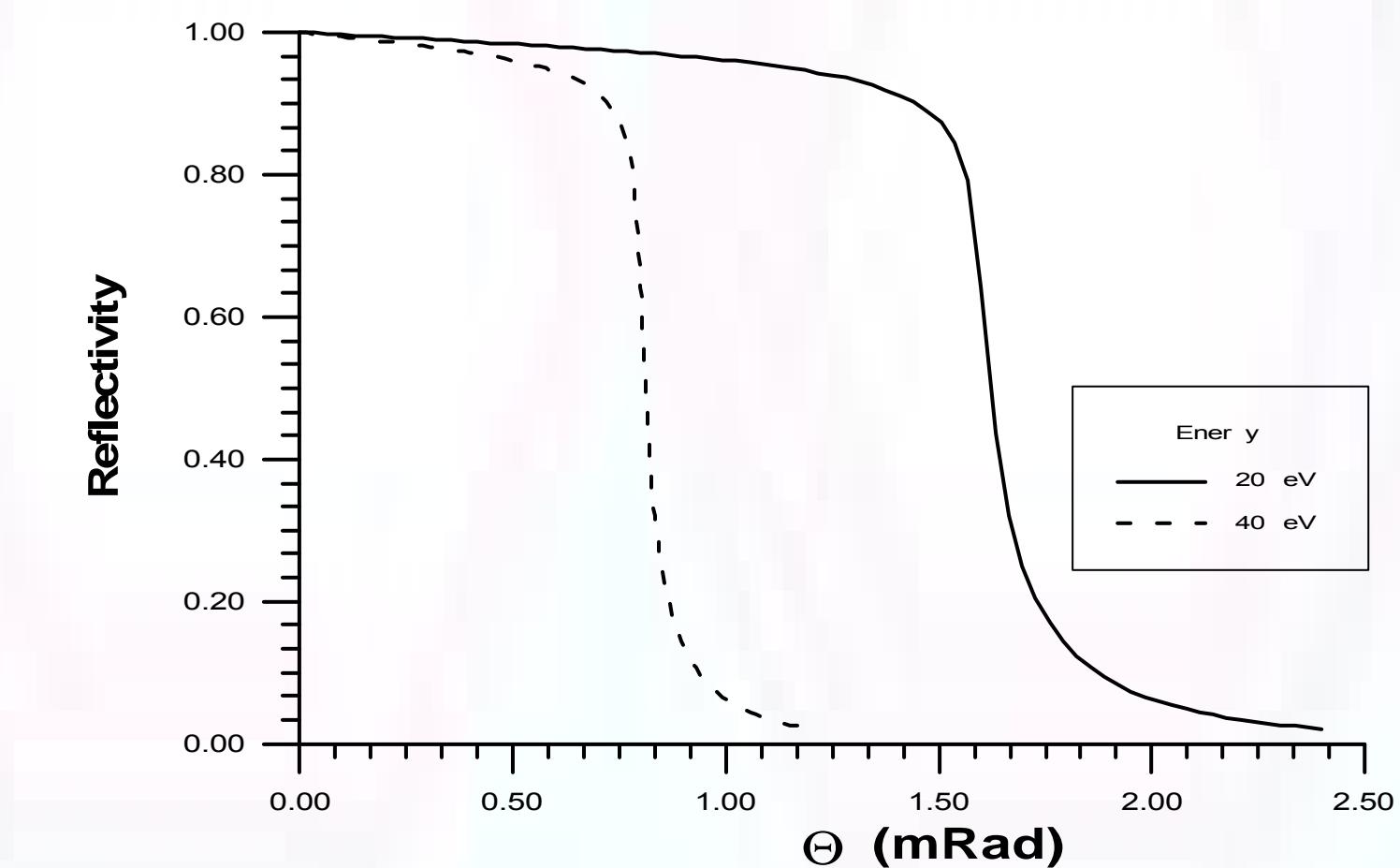
$$F = m\ddot{x} = -kx - b\dot{x} + qE$$

$$x = x_0 \cos(\omega t + \phi)$$

$$n = 1 - \delta - i\beta$$

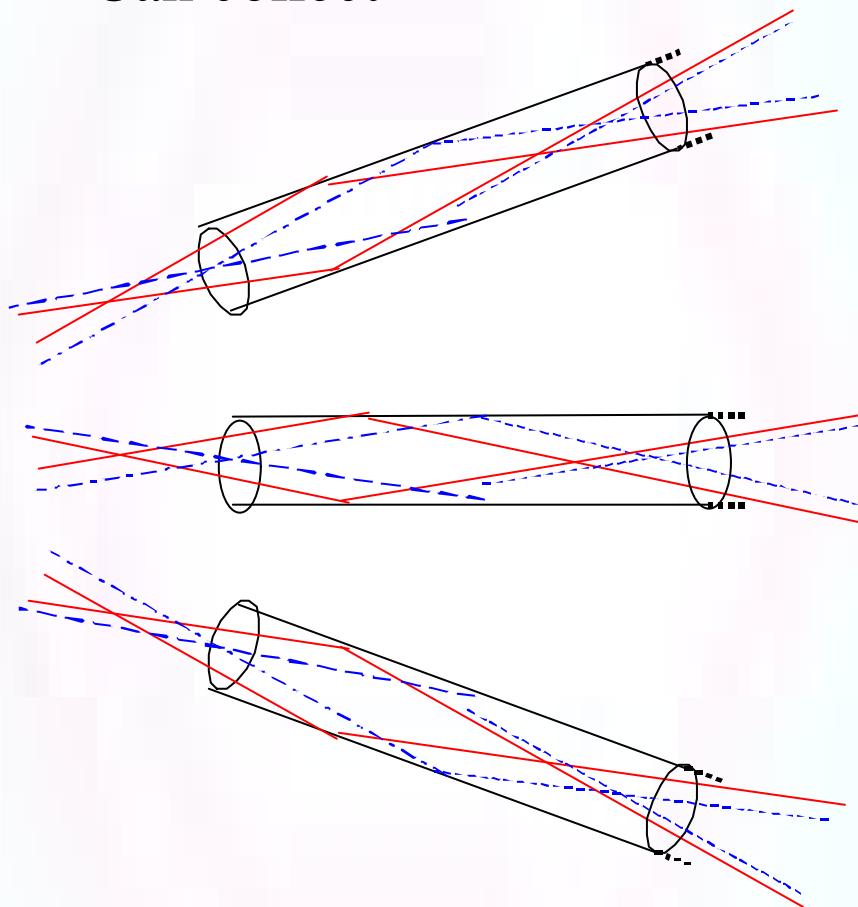
$$R < 1$$

Reflectivity vs Angle

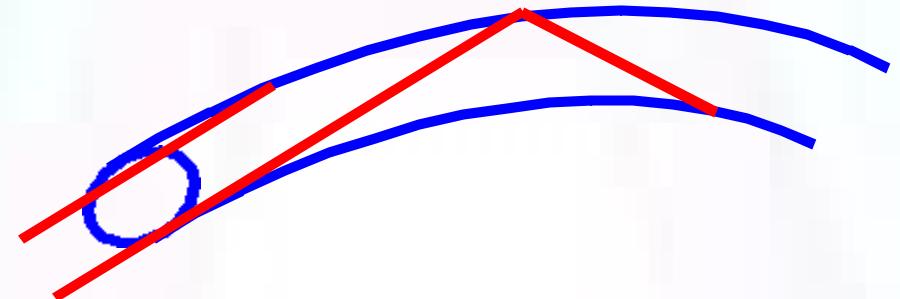


# X rays in hollow capillary tubes:

Can collect



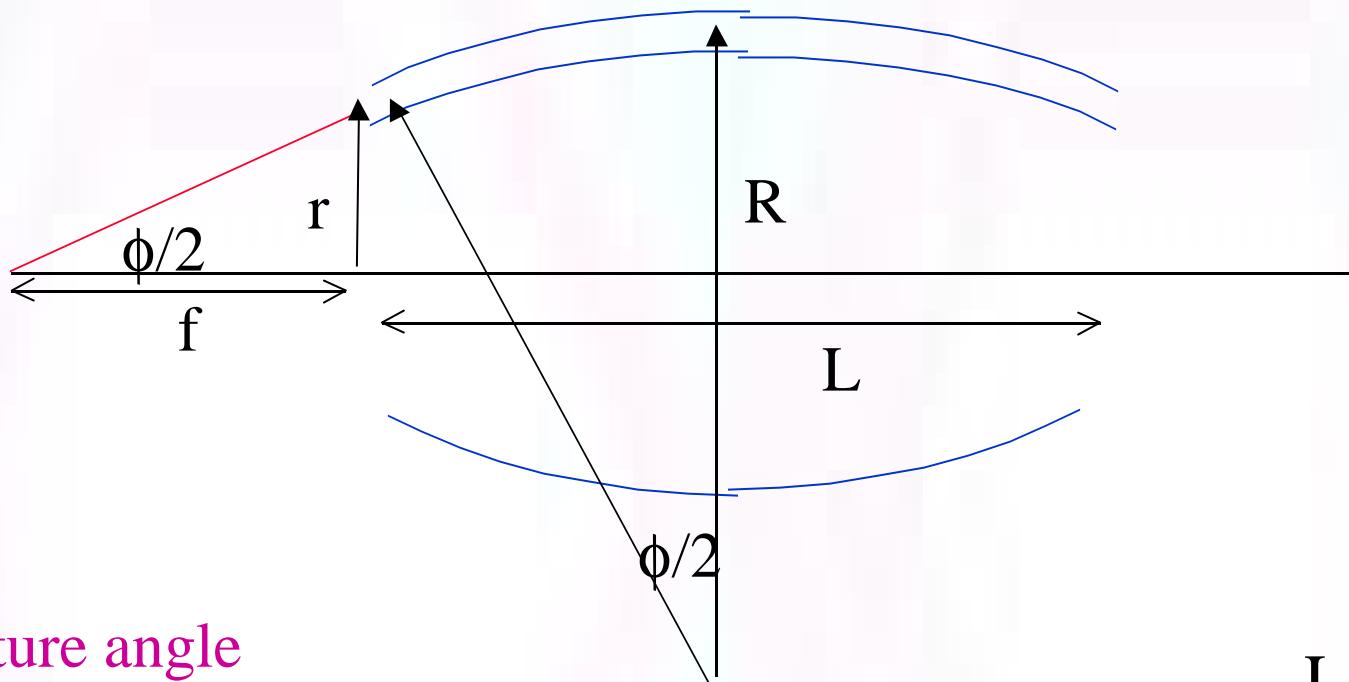
And redirect beams



To make a lens

# How much bending is required for a lens?

Approximate outermost fiber of lens as circle of radius R



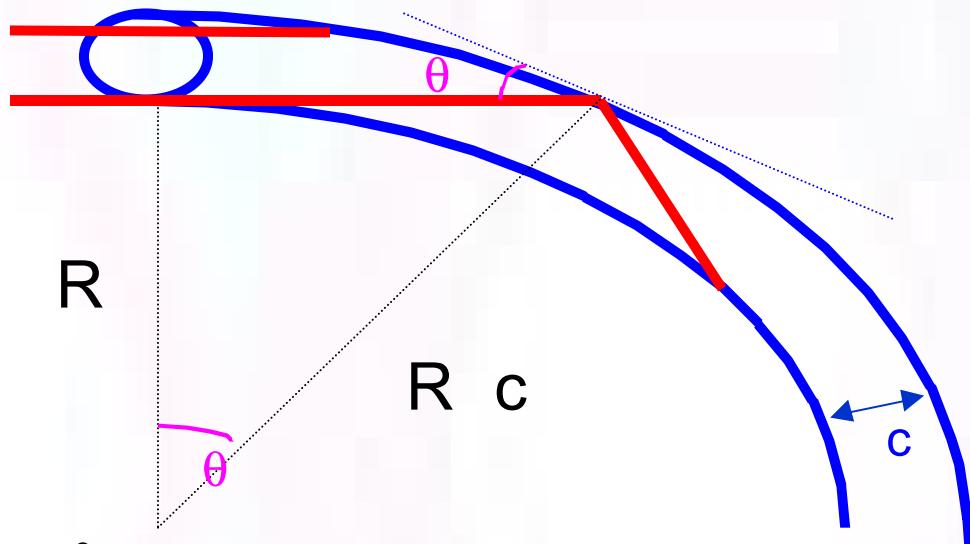
Capture angle

$$\phi = 2 \operatorname{atan} \left( \frac{r}{f} \right)$$

$$L \approx R\phi \Rightarrow R \approx \frac{L}{\phi}$$

$$f = 50 \text{ mm}, \quad r = 5 \text{ mm} \quad \Rightarrow \phi = 11.5^\circ \quad L = 100 \text{ mm} \quad \Rightarrow R \approx 1 \text{ m}$$

## Cutoff Energy dependence on bend radius and channel size

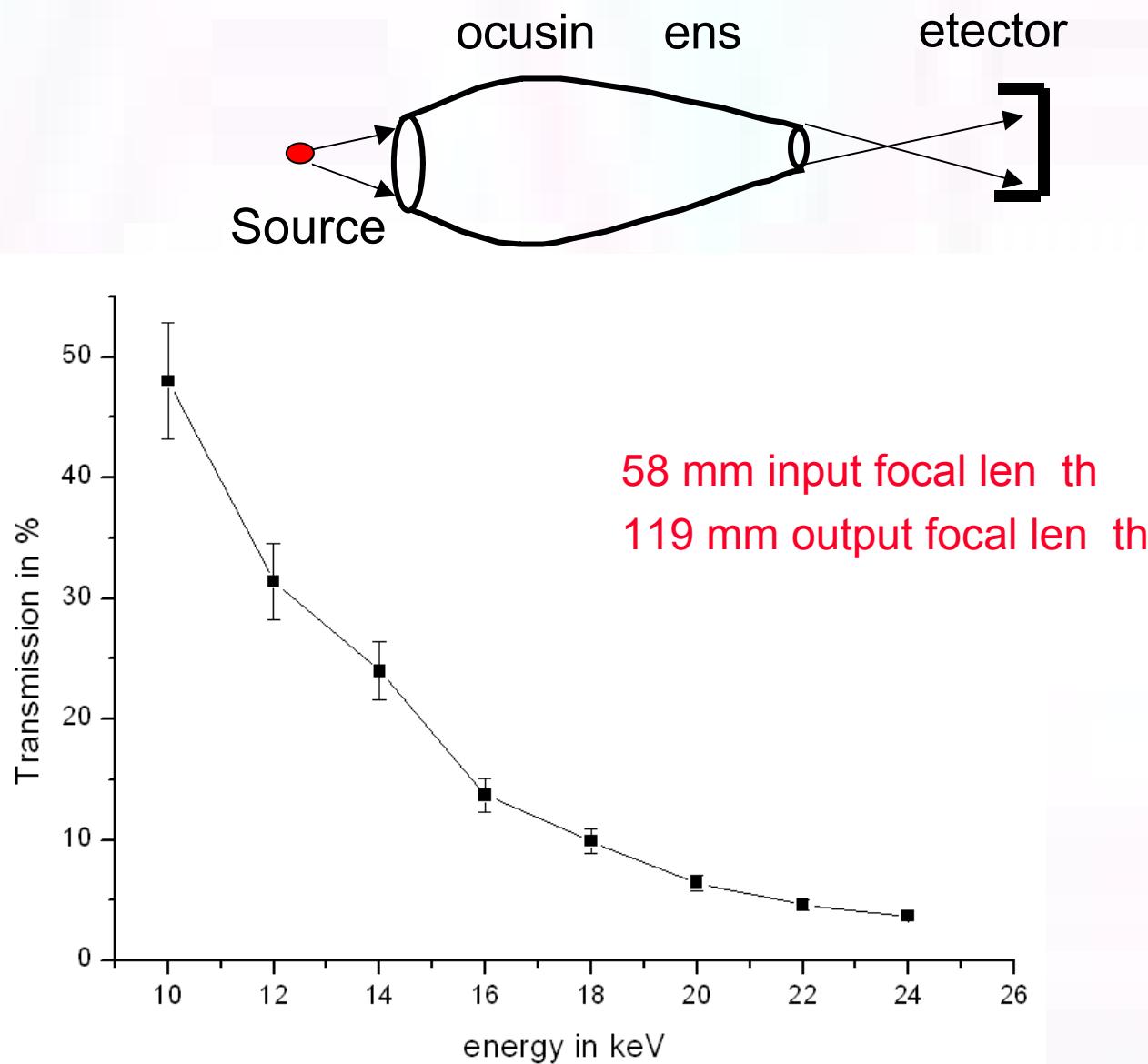


$$\cos(\theta) = \frac{R}{R+c} \Rightarrow 1 - \frac{\theta^2}{2} \approx \frac{1}{1 + \frac{c}{R}} \approx 1 - \frac{c}{R}$$

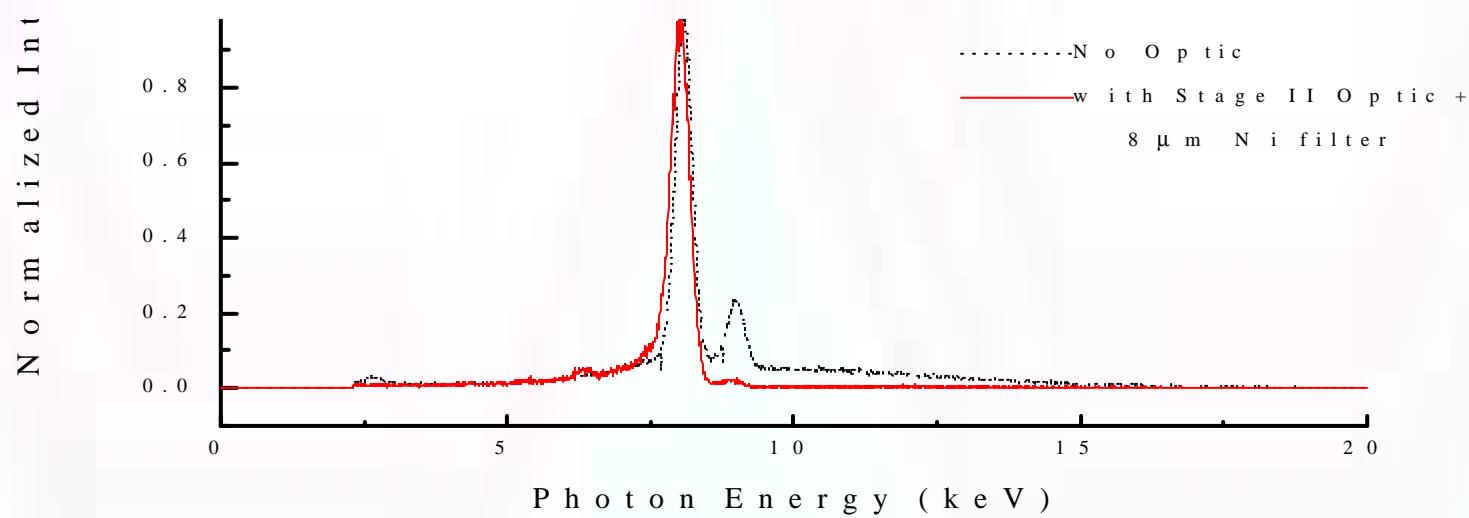
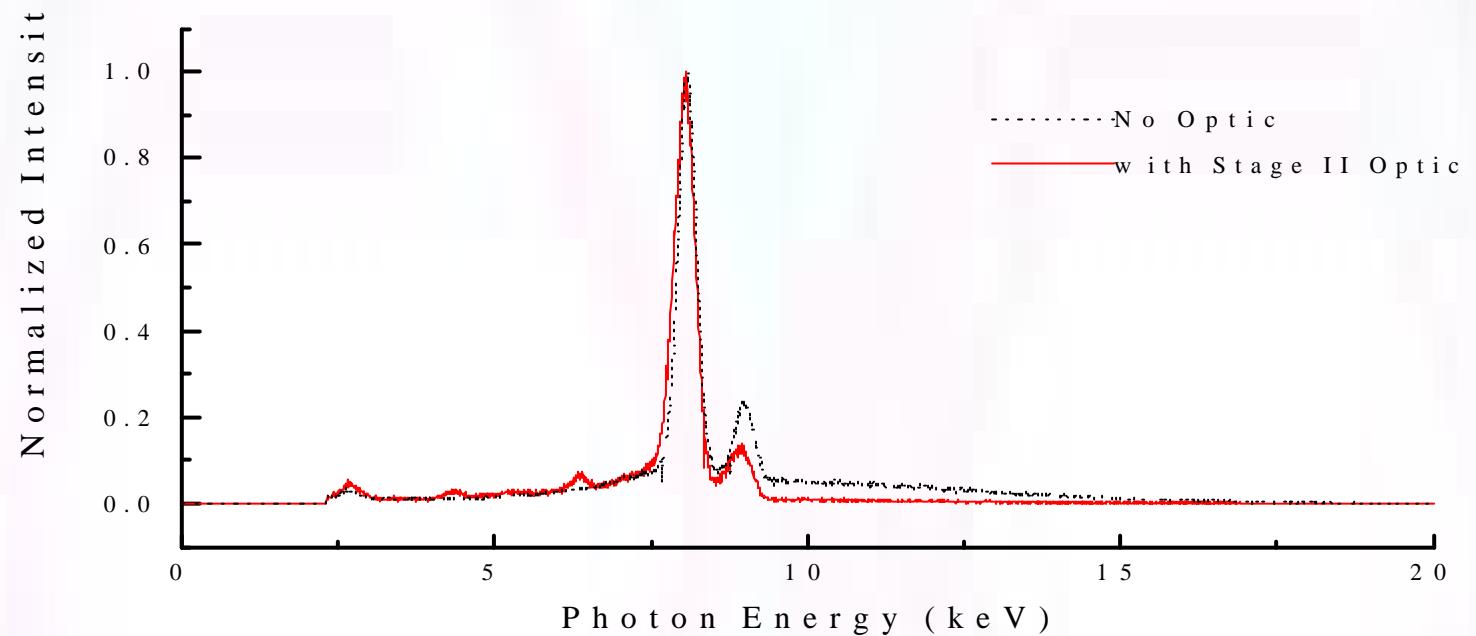
$$\theta^2 \approx \frac{2c}{R} < \theta_c^2 = \left( \frac{\omega_{\text{plasma}}}{\omega} \right)^2 = \left( \frac{E_{\text{plasma}}}{E} \right)^2 \Rightarrow E < E_{\text{plasma}} \sqrt{\frac{R}{2c}}$$

$$c = 2 \mu\text{m} \quad R = 1 \text{ m} \quad E_{\text{plasma}} = 30 \text{ eV} \quad \Rightarrow \quad E < 15 \text{ keV}$$

# Transmission



# Beam Filtering

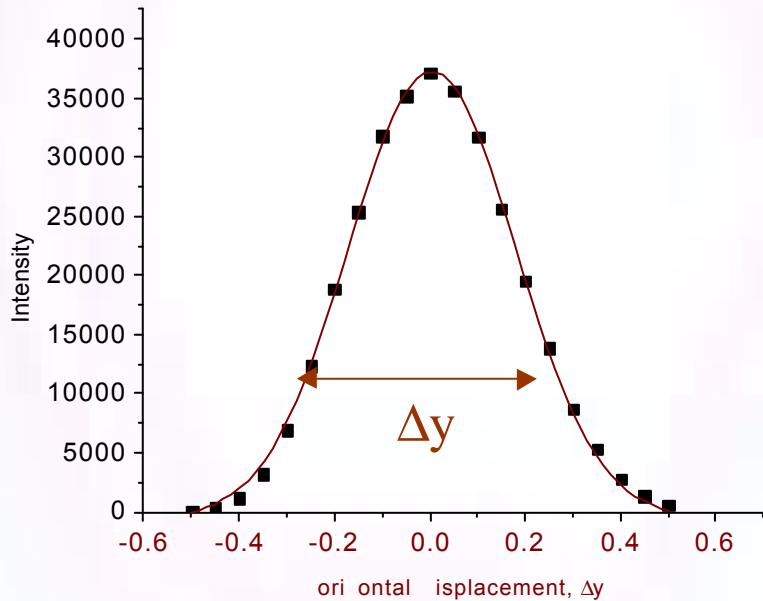
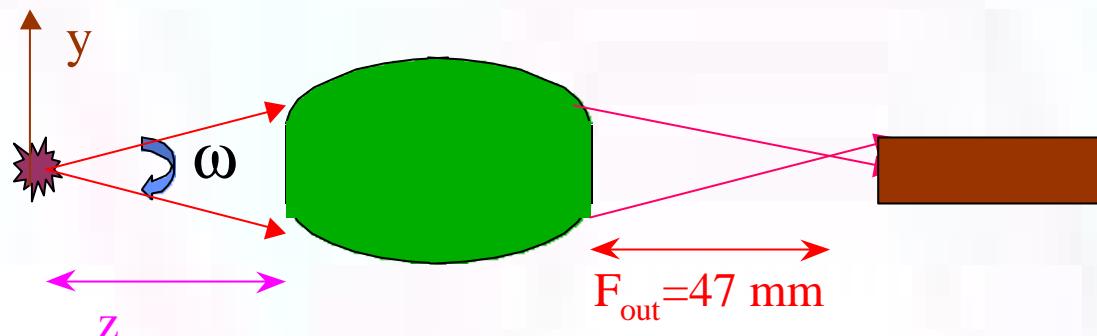


# Characterization of Polycapillary Optics

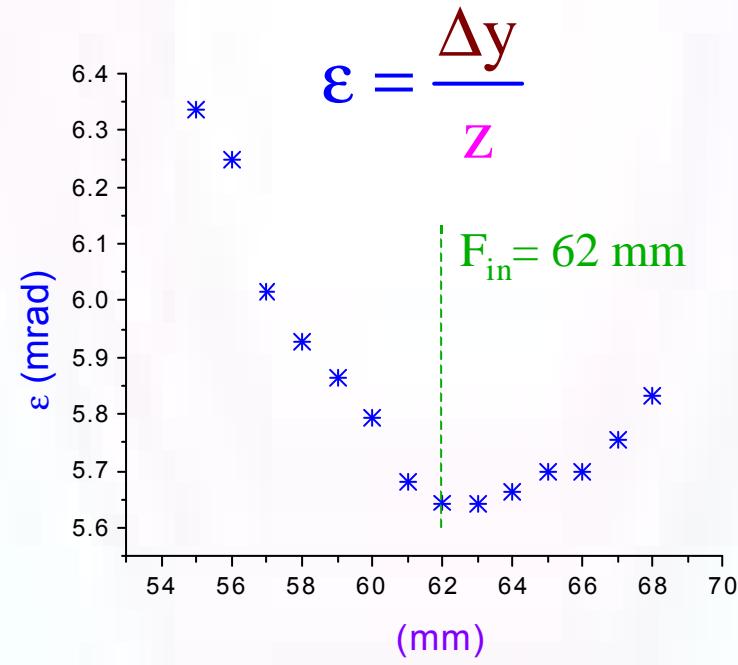
Capture Angle,

$\omega = 3^\circ$

$\Omega = 2 \text{ millisteradian}$

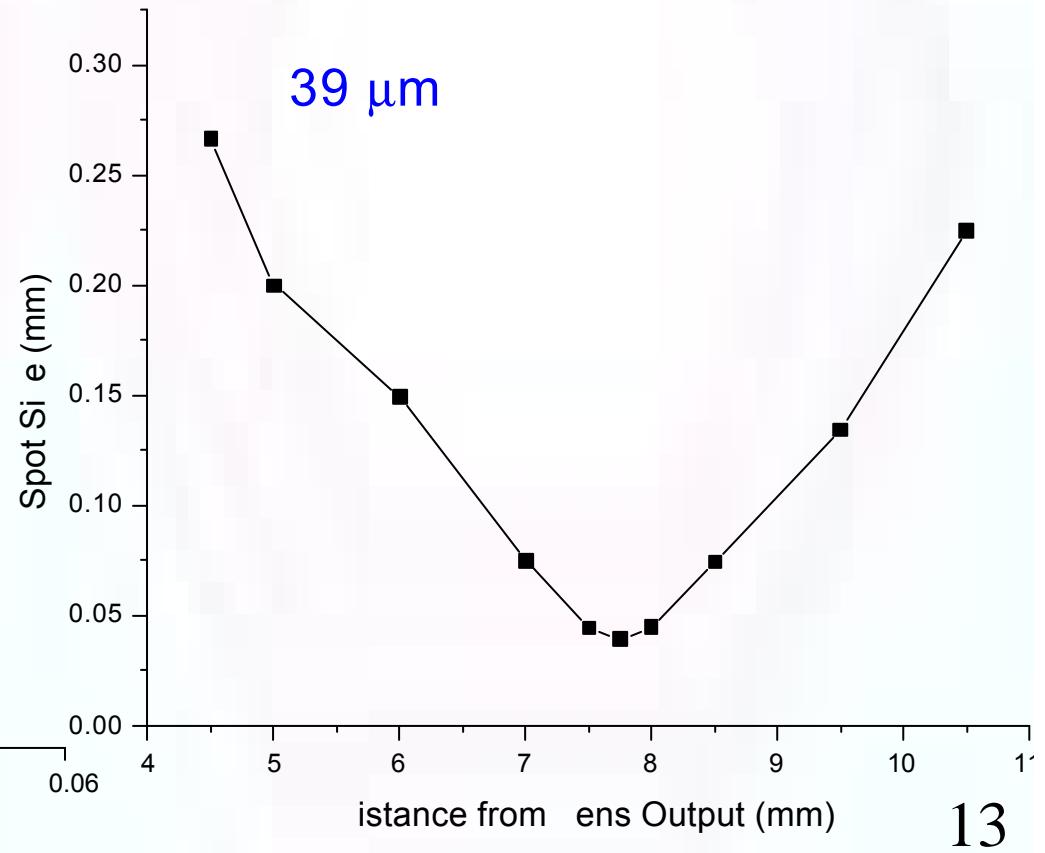
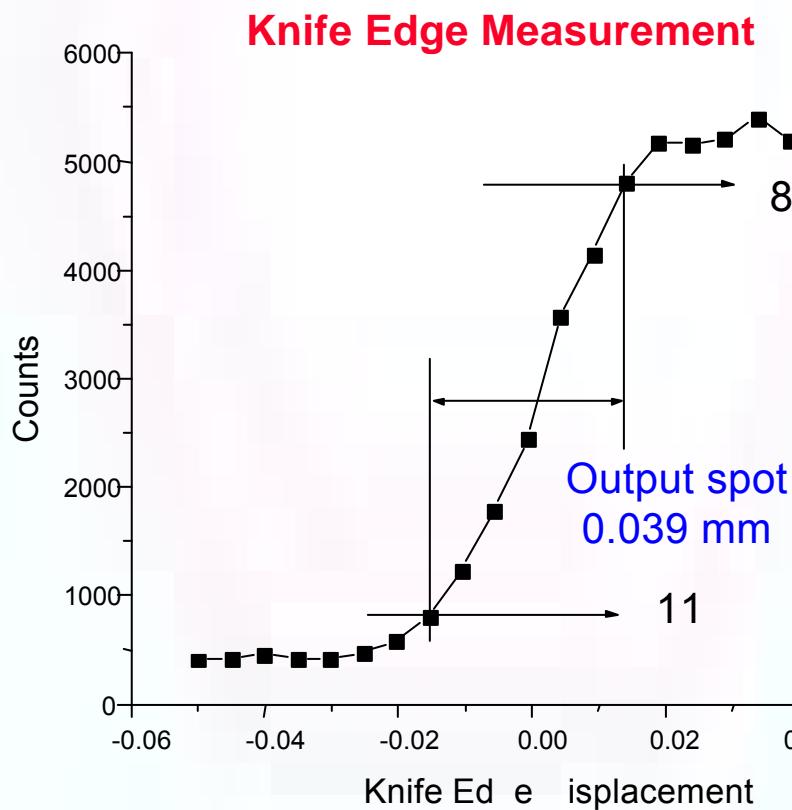
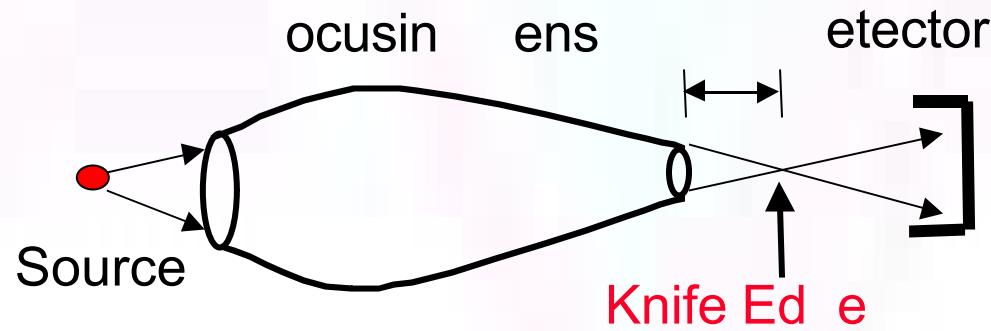


transmission 9.9

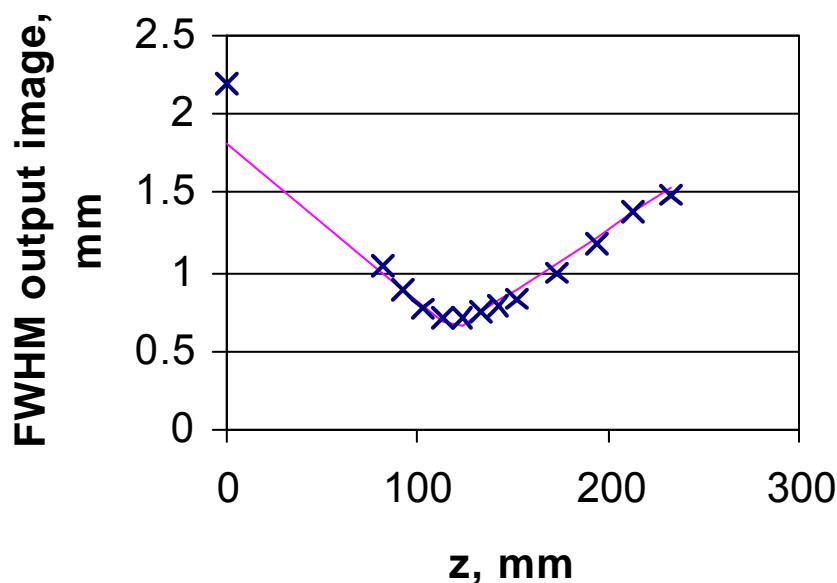
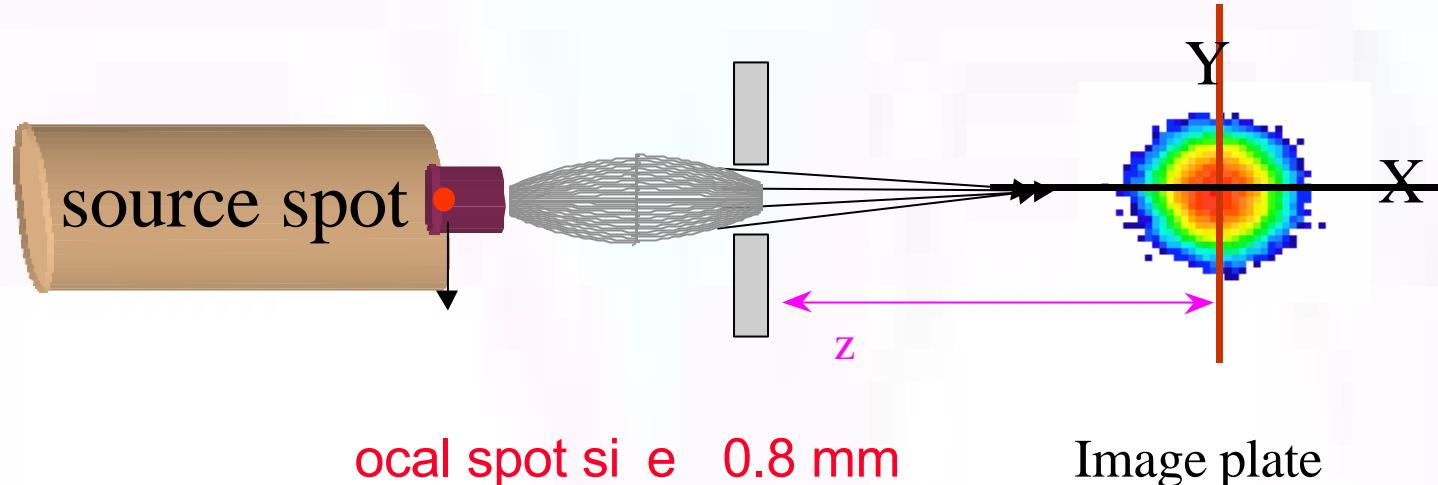


Input focal length

# Focusing Lens Output Spot Measurement



## Focusing Optic Output



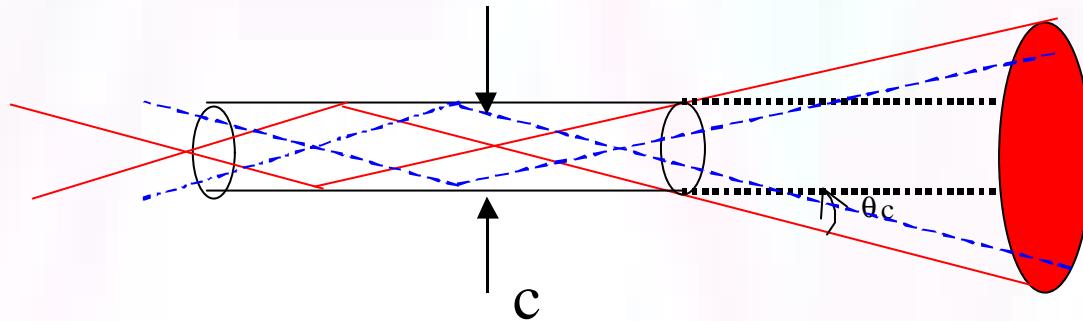
data  
 linear fit

Global Divergence =

$$\text{slope} = 2\beta = 0.55^\circ$$

# FOCAL SPOT SIZE

## Minimum due to Local Divergence 2a

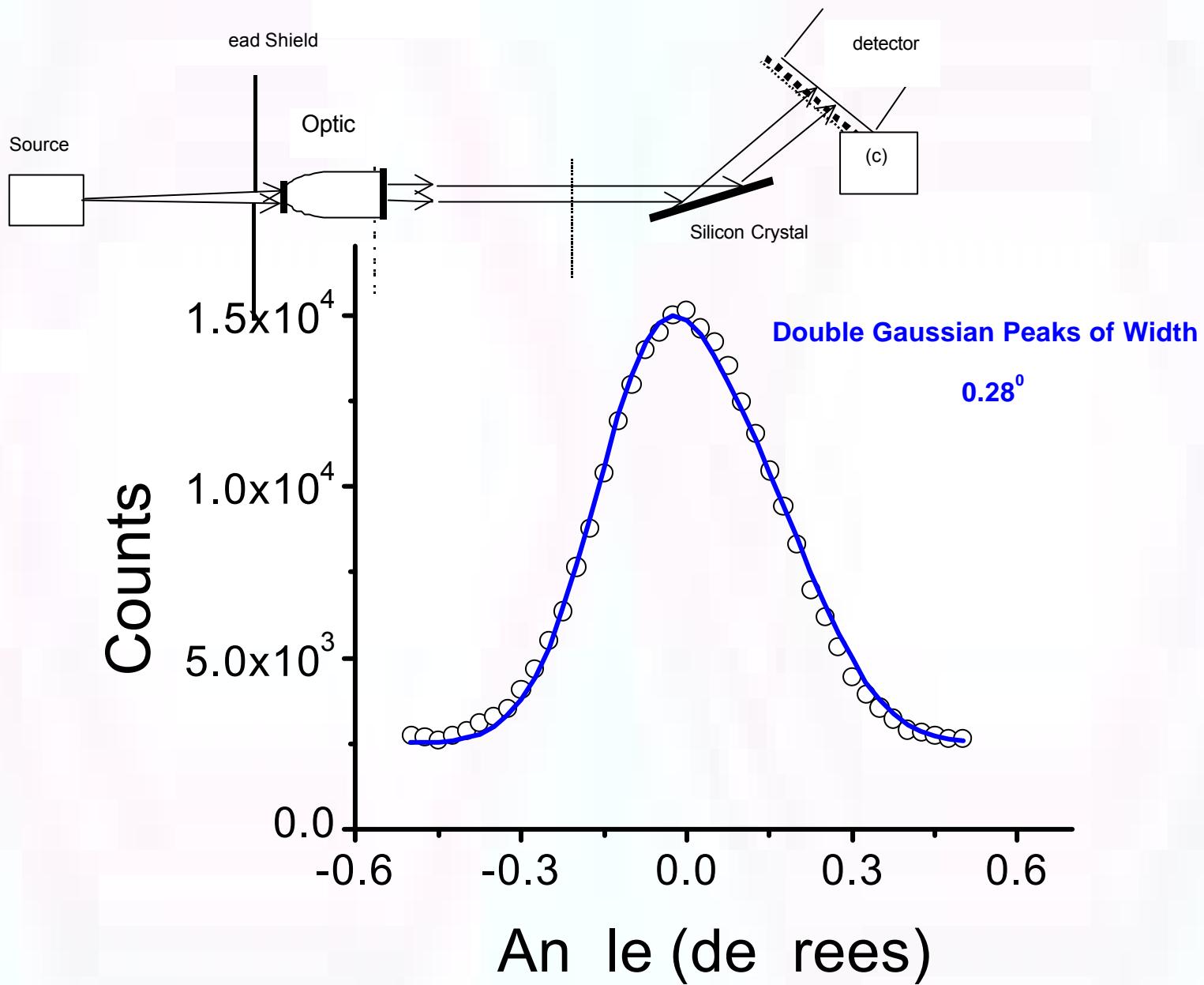


Minimum size :

$$d = c + 2\alpha f = c + 1.3 \theta_c f$$

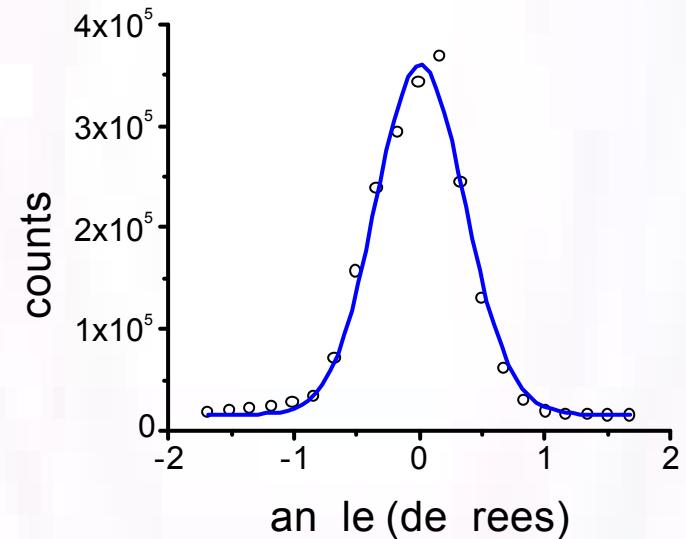
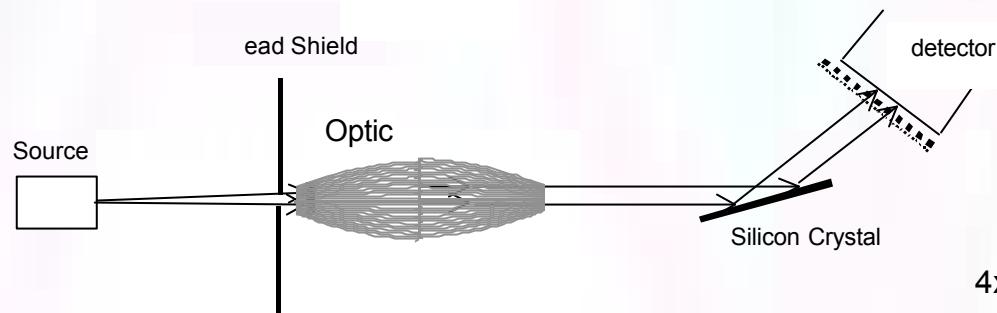
$$c = 5 \mu\text{m} \quad 2\alpha = 0.28^\circ \quad \begin{cases} f = 50 \text{ mm} \\ f = 5 \text{ mm} \end{cases} \quad \Rightarrow d = 250 \mu\text{m} \quad \Rightarrow d = 30 \mu\text{m}$$

# Rocking Curve collimating optic



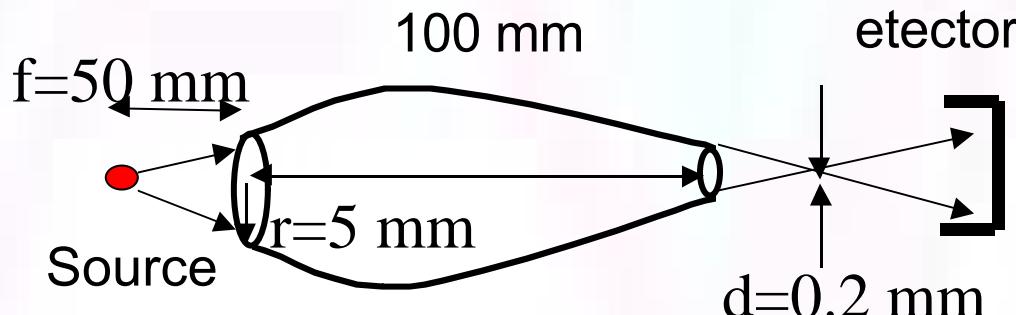
# Global divergence

Rocking Curve focusing optic



$$\text{Rocking Curve Width} = 0.83^\circ = 2\alpha + 2\beta = 0.28^\circ + 0.55^\circ$$

## Relative to What?



To make the optic look good: compare to flux through a pinhole of diameter < spot size compared to source at focal point:

$$F_{\text{no optic}} = \frac{P_{\text{source}}}{4\pi(f_{\text{in}} + L + f_{\text{out}})^2} \pi \left(\frac{d}{2}\right)^2 \quad F_{\text{Lens}} = \frac{P_{\text{source}}}{4\pi(f_{\text{in}})^2} \pi r_{\text{Lens}}^2 T$$

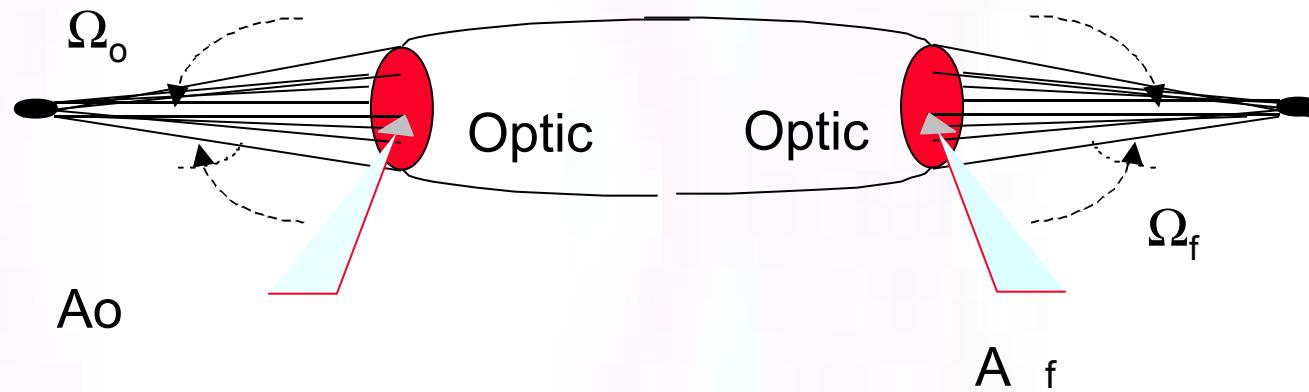
$$\text{Gain} = \frac{F_{\text{Lens}}}{F_{\text{no optic}}} = \left( \frac{f_{\text{in}} + L + f_{\text{out}}}{f_{\text{in}}} \right)^2 \left( \frac{r_{\text{Lens}}}{d/2} \right)^2 T$$

$$d = 200 \mu\text{m} \quad r_{\text{Lens}} = 5 \text{ mm} \quad f = 50 \text{ mm} \quad L = 100 \text{ mm} \Rightarrow \text{Gain} = 8000$$

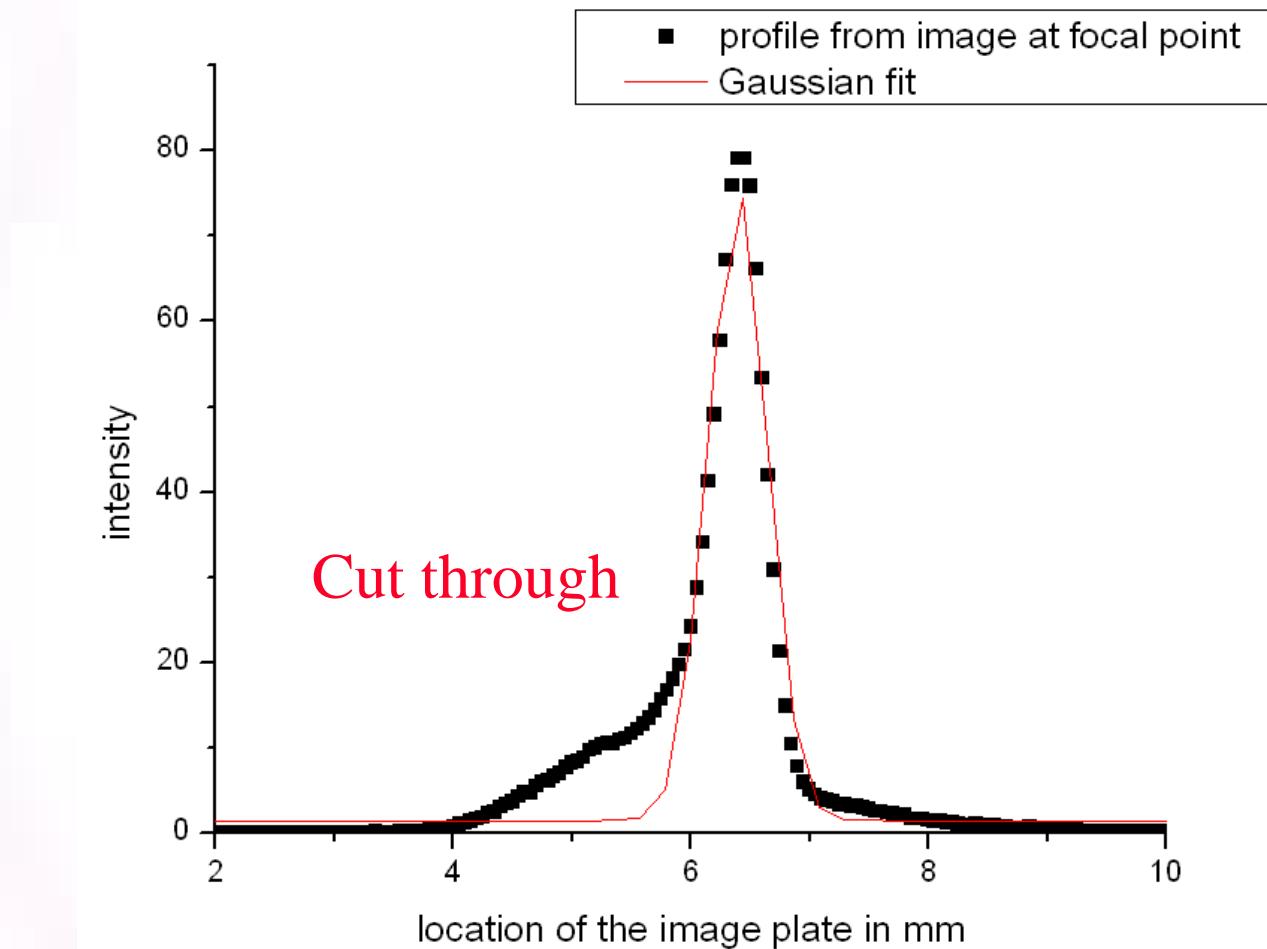
## Liouville's Theorem

Angle area product cannot decrease

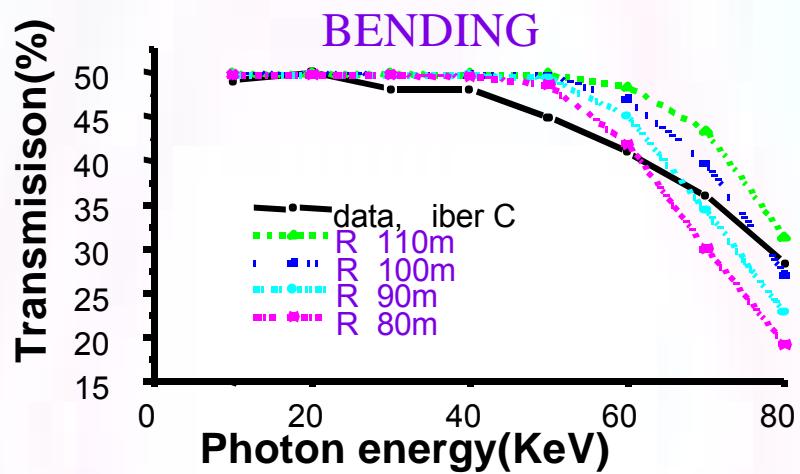
$$A_f \Omega_f \geq A_o \Omega_o$$



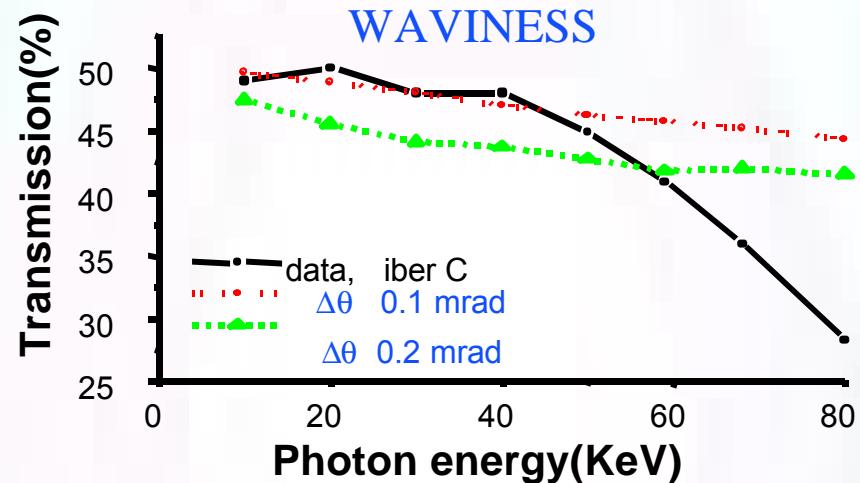
# Optics Defects



# Optic defects



**Bending:**  $\lambda_b = 10 \text{ cm}$   
parameter: bending radius,  $R$



**Waviness:**  
 $\lambda_r$   $\lambda_b$   
parameter:  
Modeled by random angle shifts of  
 $\delta\theta$  after each bounce

# Optic defects

$$\lambda \approx 1 \text{ } \mu\text{m}$$

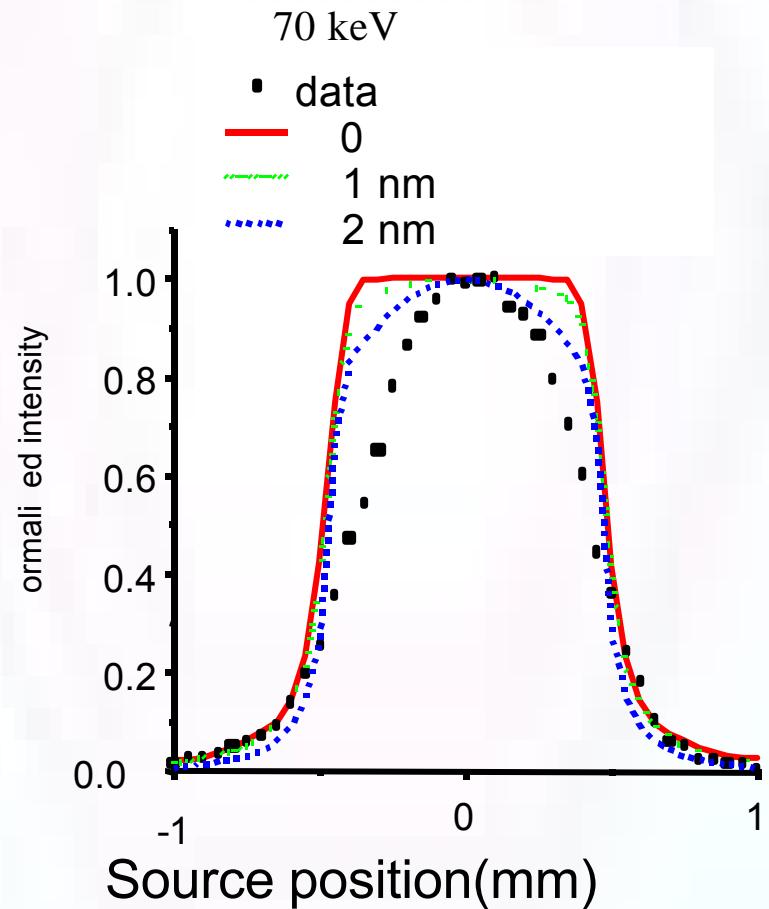
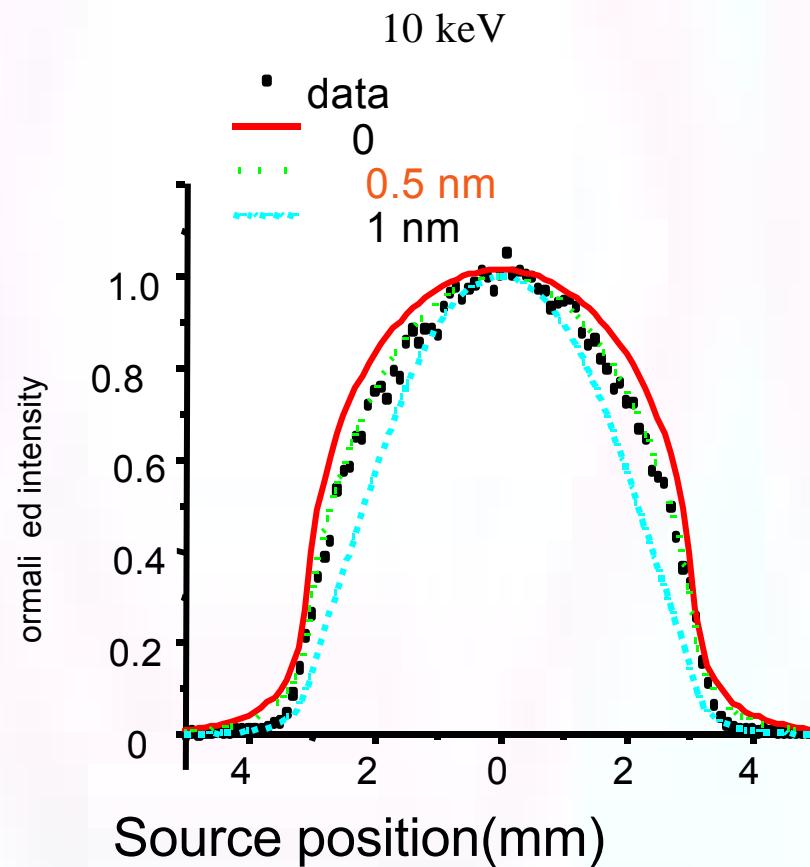
Roughness:

parameters:

correlation len th  
rms hei ht

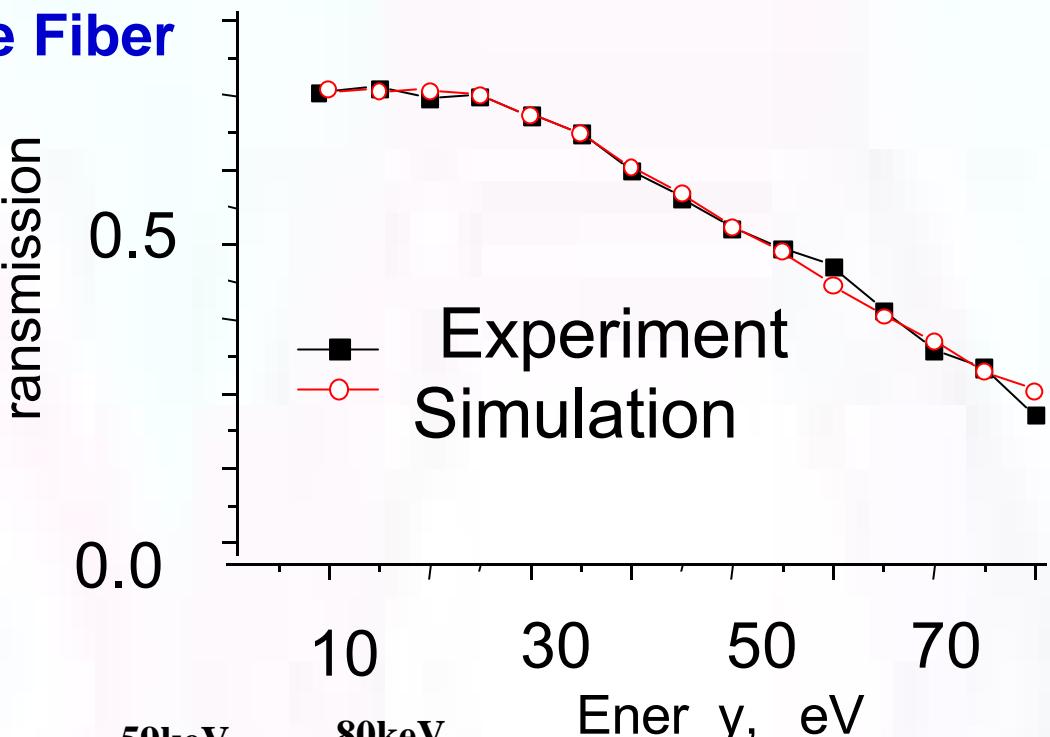
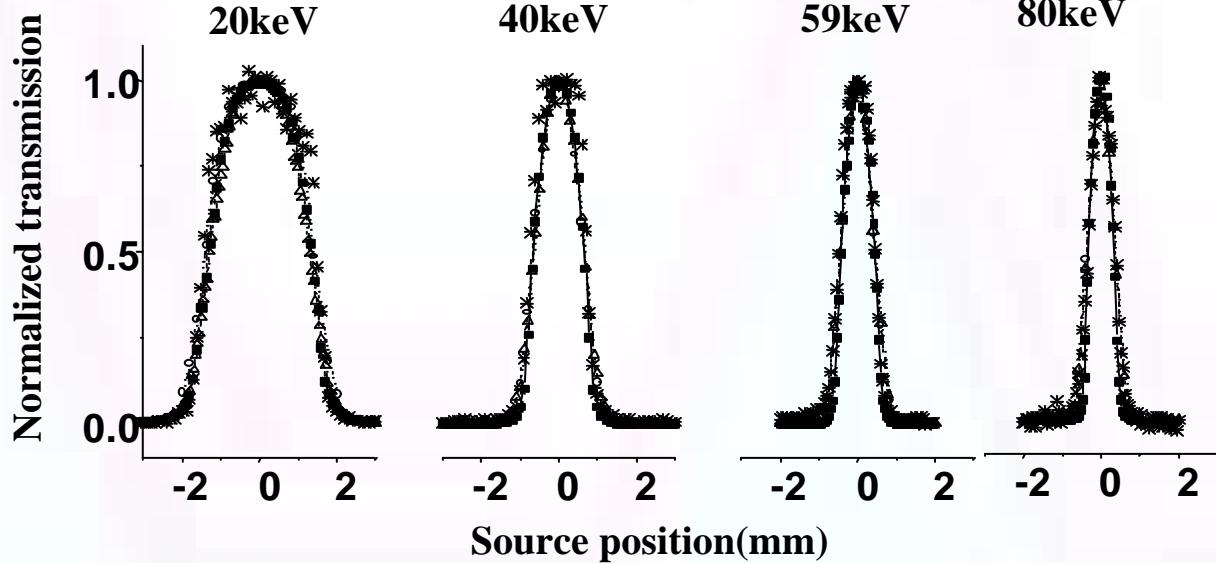
Roughness correlation

$$g(\Delta x) = \frac{1}{L} \int_0^L Z(x)Z(x + \Delta x)dx = \overline{Z}^2 e^{-\frac{|\Delta x|}{s}}$$

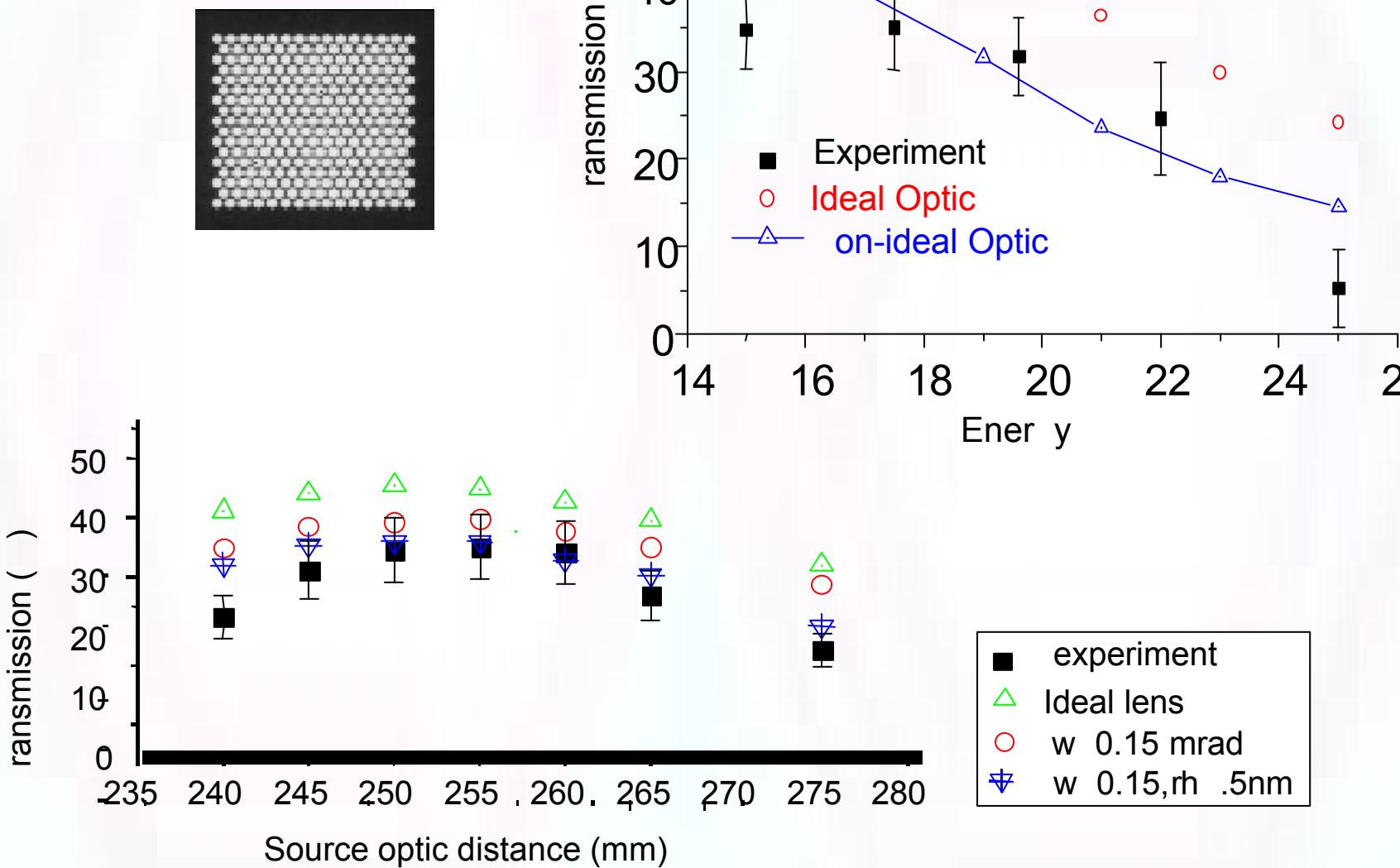


# Simulation Analysis: Single Fiber

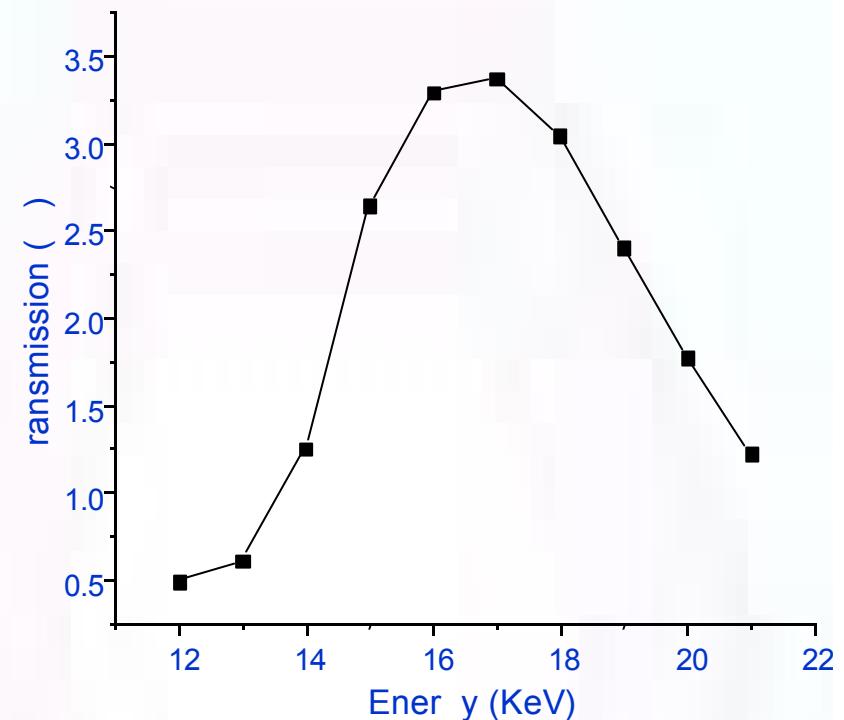
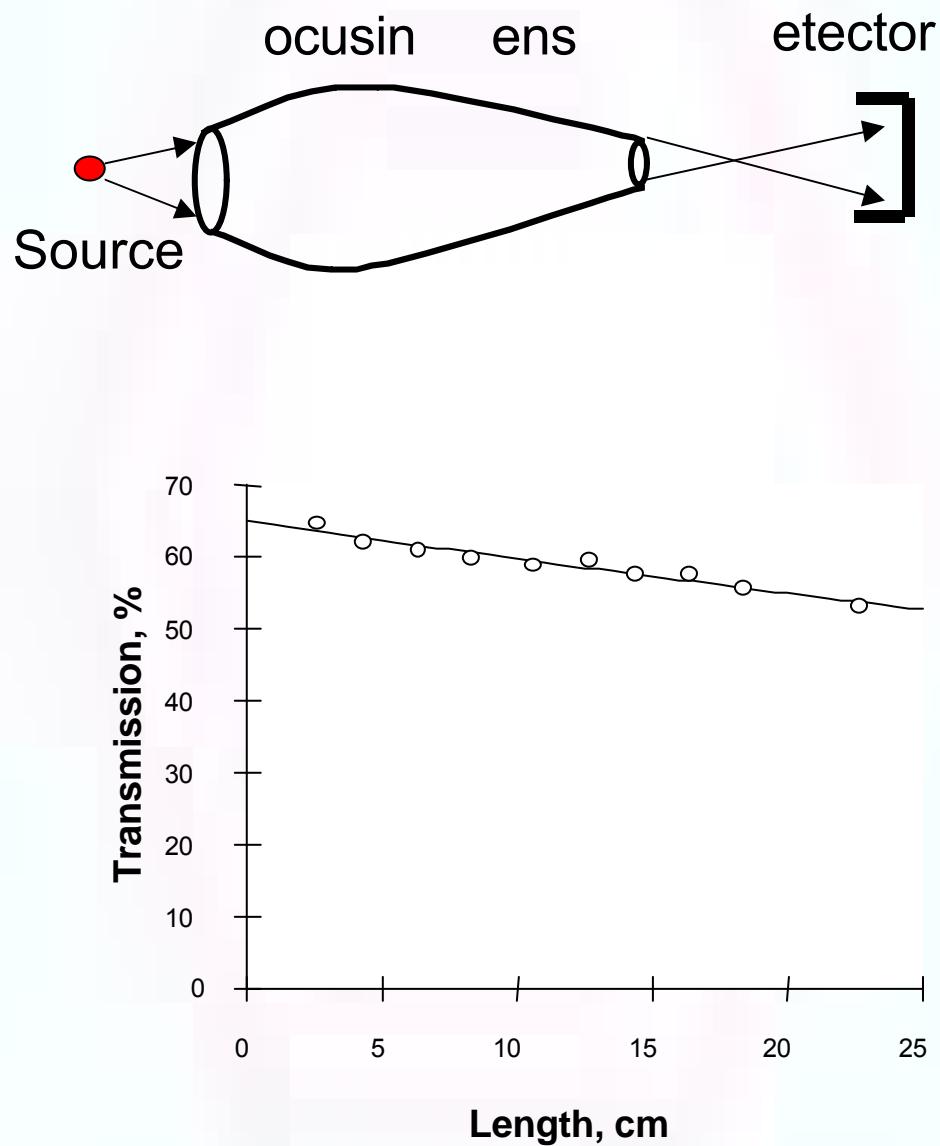
simulation with  
**w=0.15 mrad** and  
**R=120 m.**



# Simulation Analysis: Lens made from fibers

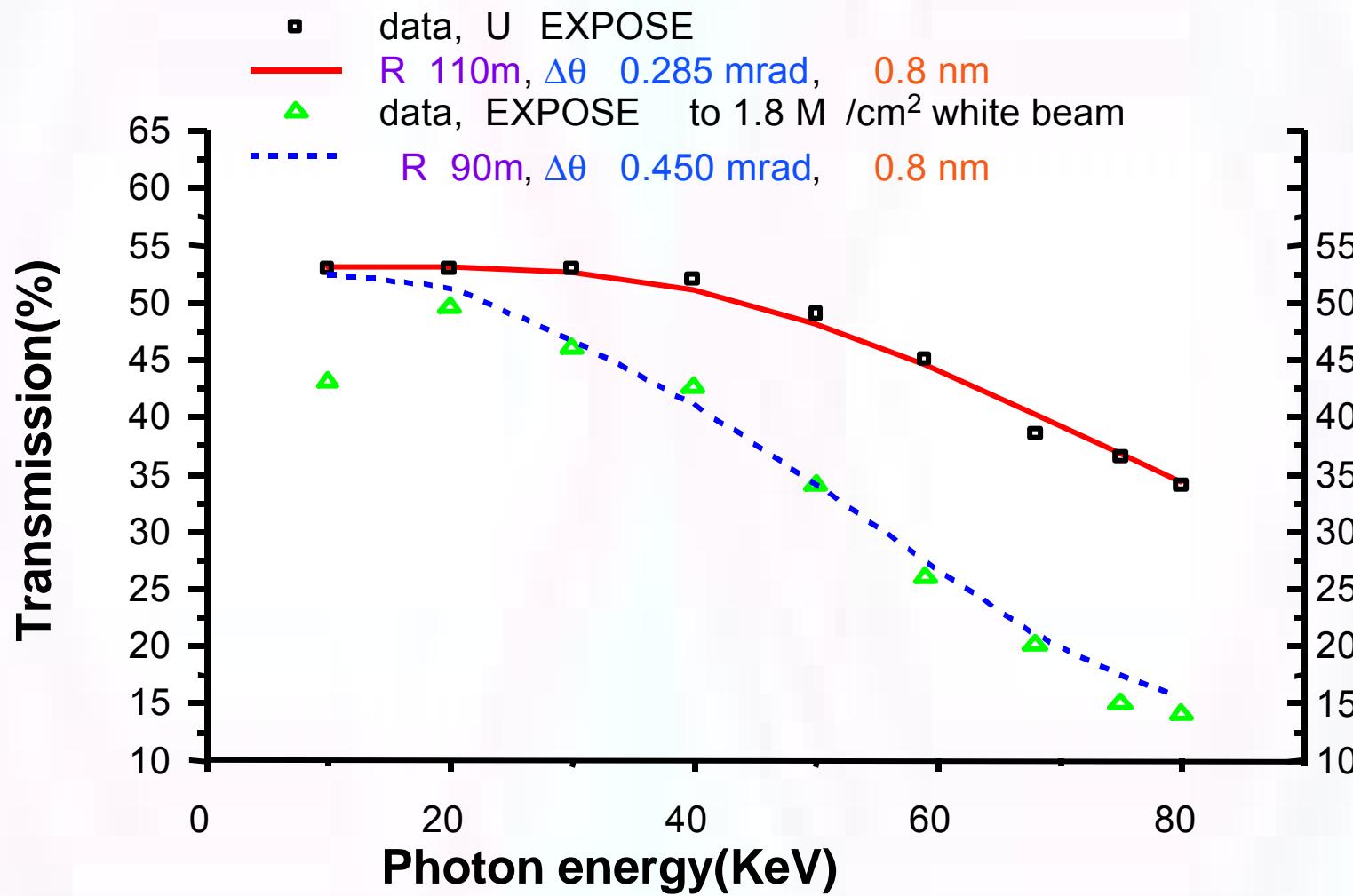


# Optics Defect: Channel Blockage



39 mm input focal length  
7.8 mm output focal length  
30  $\mu$ m glass in length of lens

# Application to Radiation Damage





## Characteristics of Polycapillary Focusing Optics:

Type Beam Focusing, Polychromatic

Useful X-ray Energy Range Typically 0.1 - 30 keV

Collection Solid Angle Up to 20 degrees

Working Distance 2.5mm 5mm 10mm 20mm  
50mm 100mm

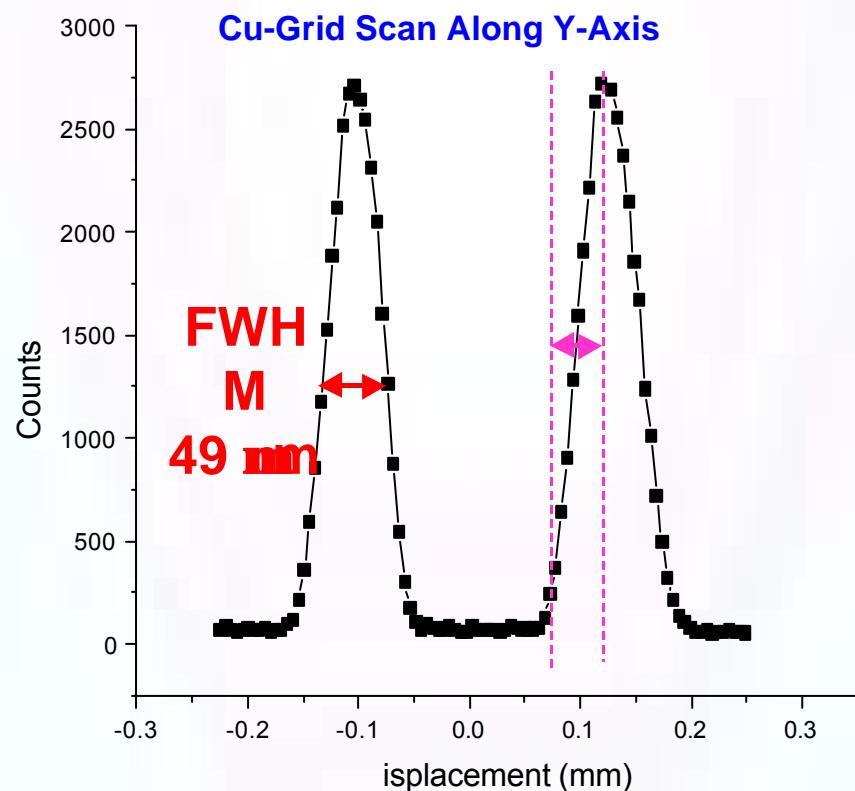
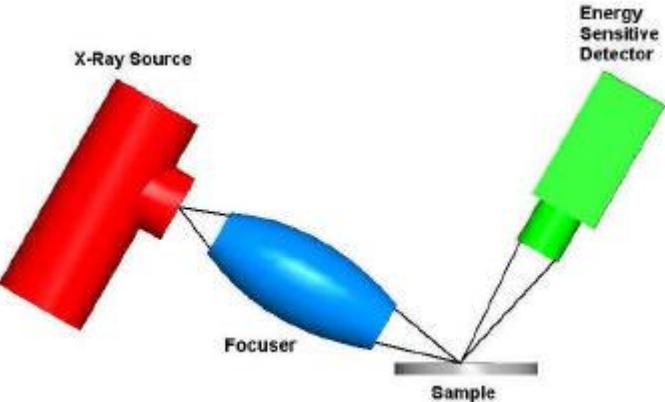
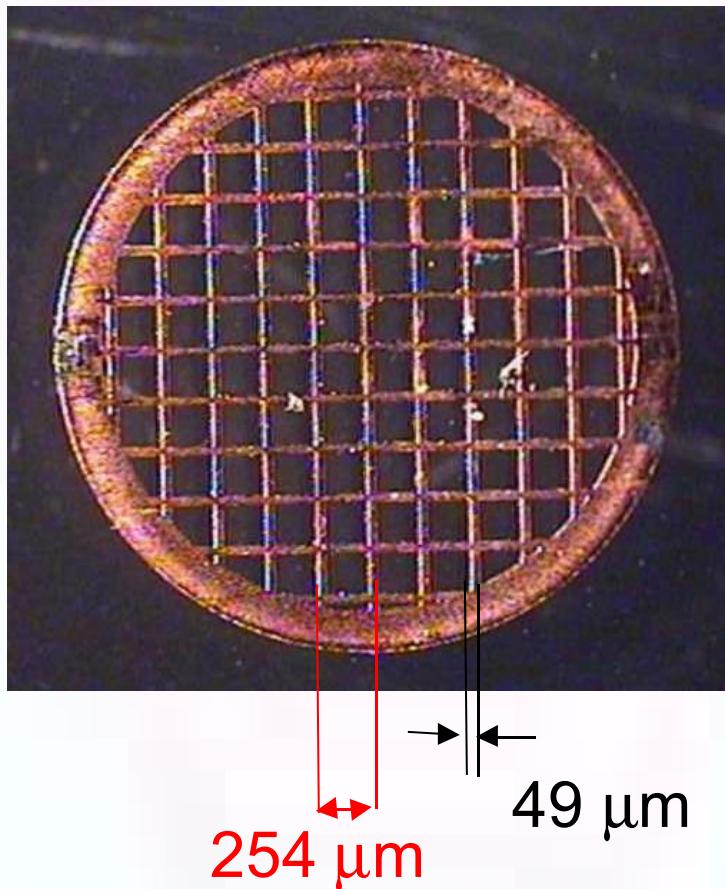
Focused beam size  
(Mo K $\alpha$ , FWHM, 17.4keV) 10um 18um 30um 45um  
100um 180um

Gain (Compared to pinhole aperture  
100 mm from source) 100x - 10000x

# Applications: XRF

Spatial Resolution of MXR with 39  $\mu\text{m}$  spot

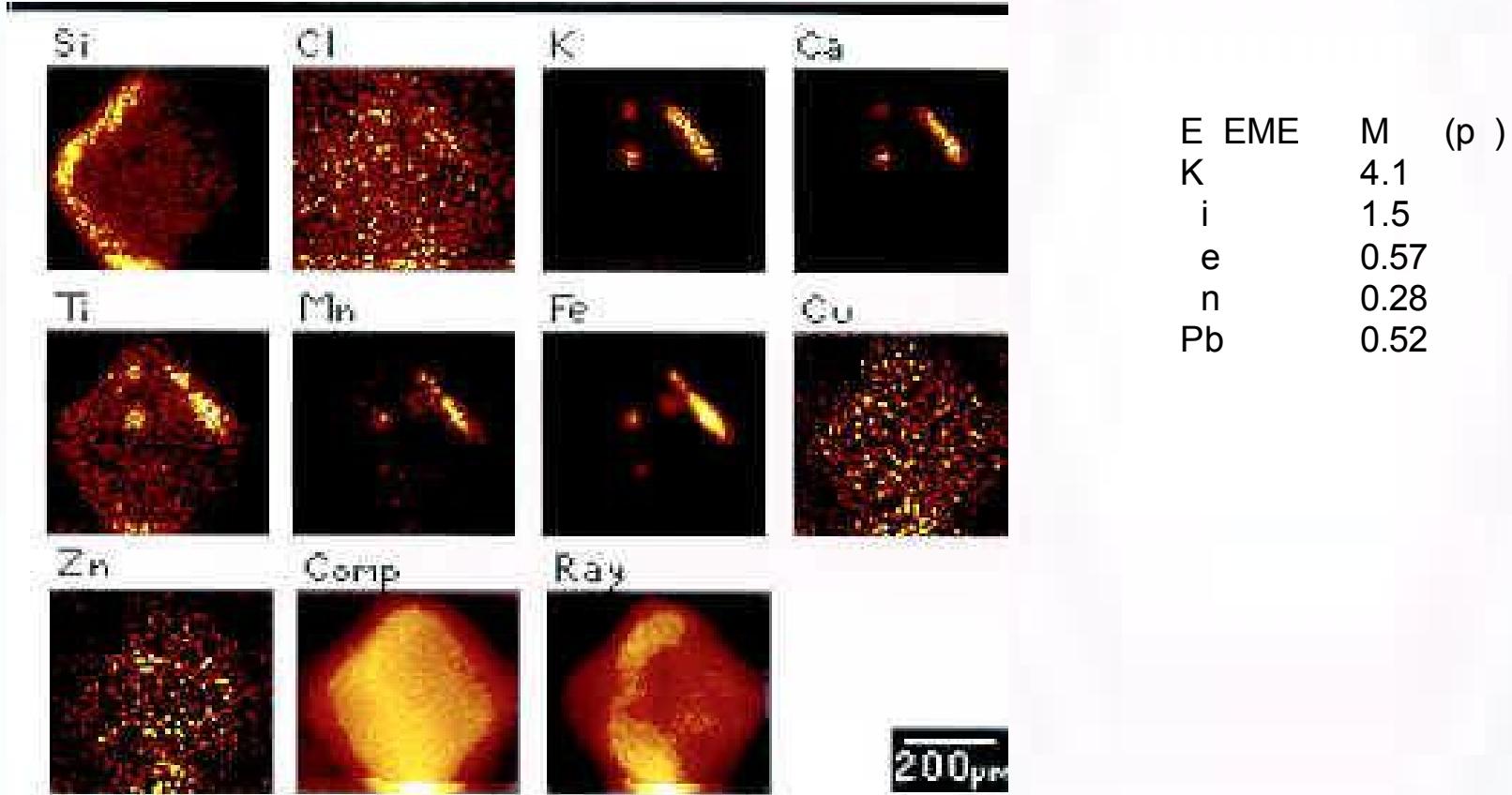
Micrograph of Cu grid



# Applications: XRF

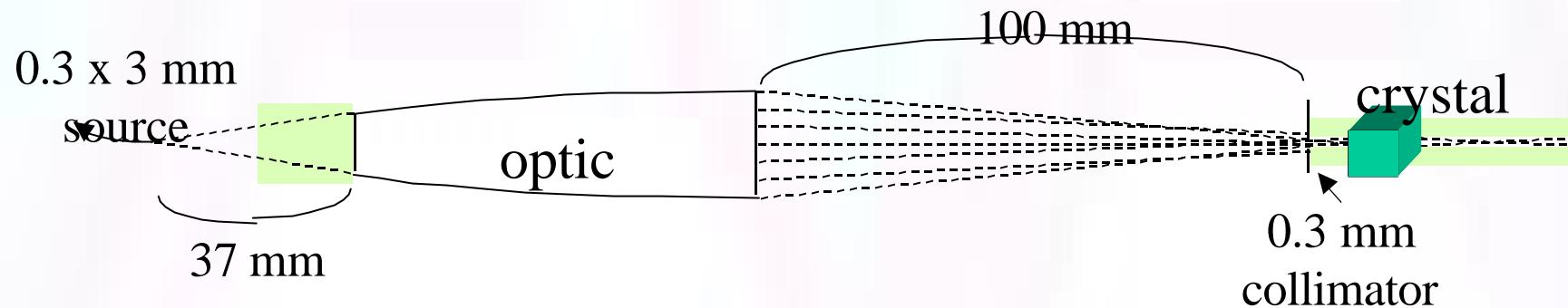
## Elemental Mapping

MXRF maps of a quartz phenocryst with small volcanic glass inclusions



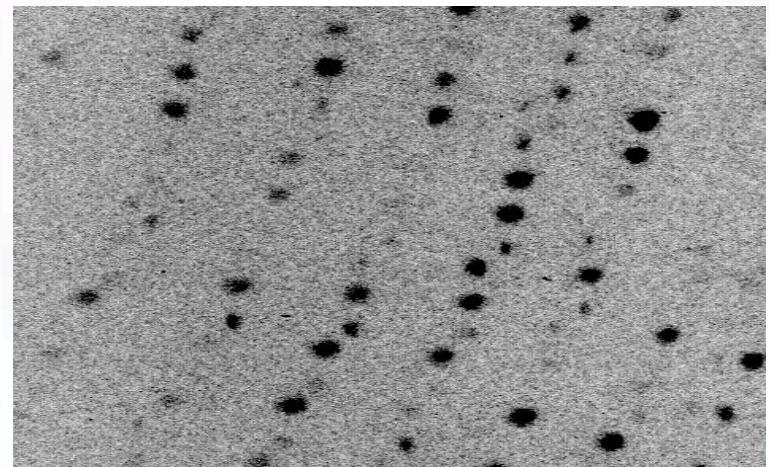
Courtesy of Ning Gao, XOS

# Applications: Protein Crystallography



ysosyme pattern taken in  
20 seconds with 2.8  
rotating anode, comparable to 30-35  
min. without optic

linear R factor without optic 6.4  
with optic on same sample: 6.9

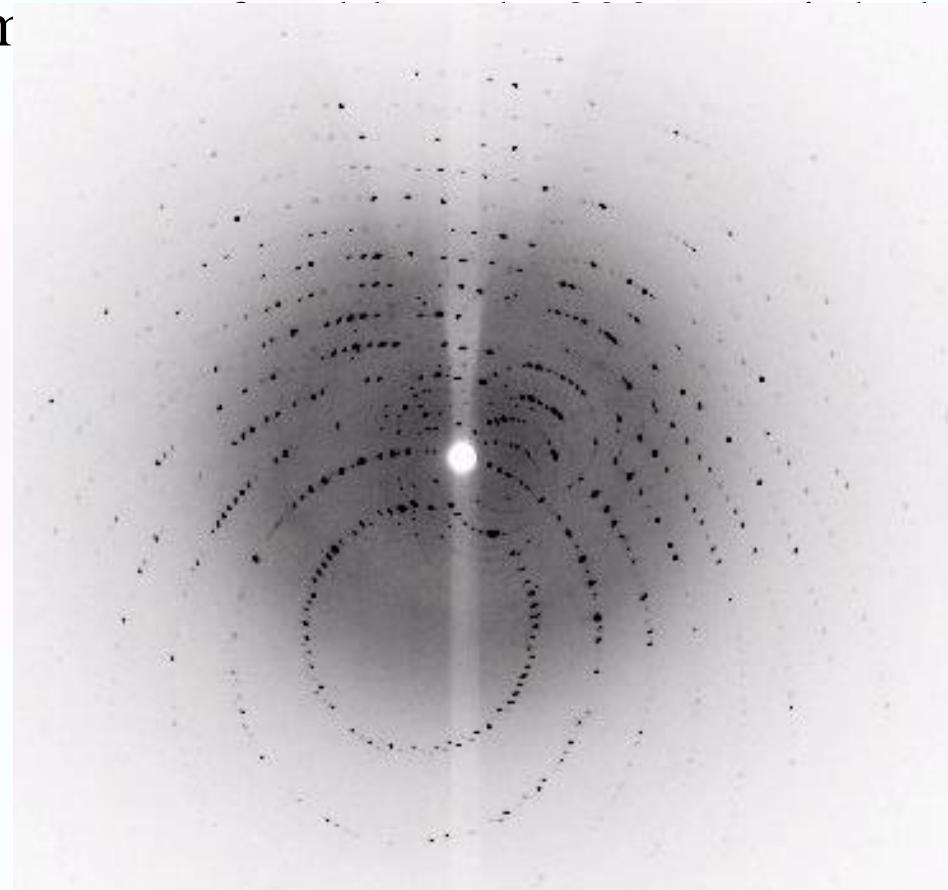


# Applications: Protein Crystallography

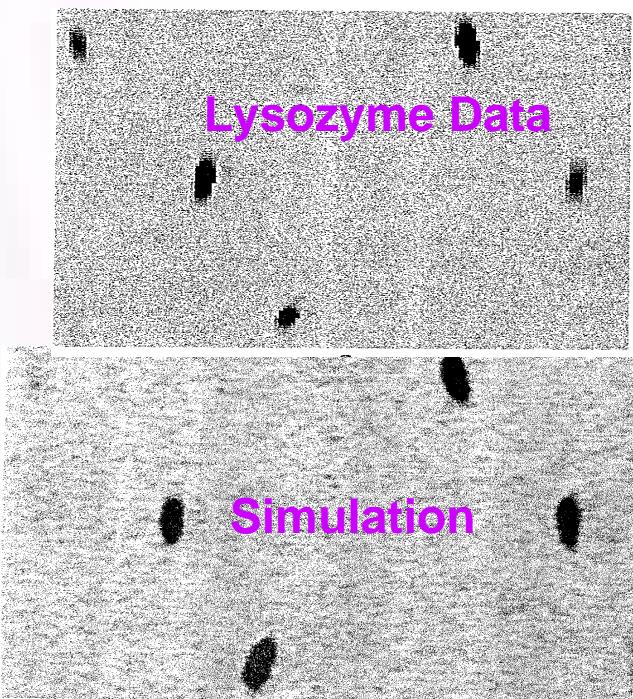
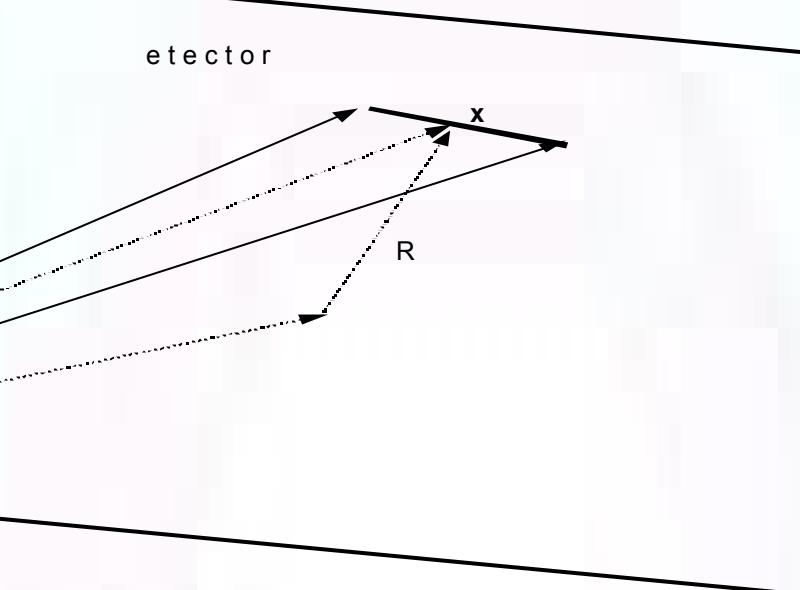
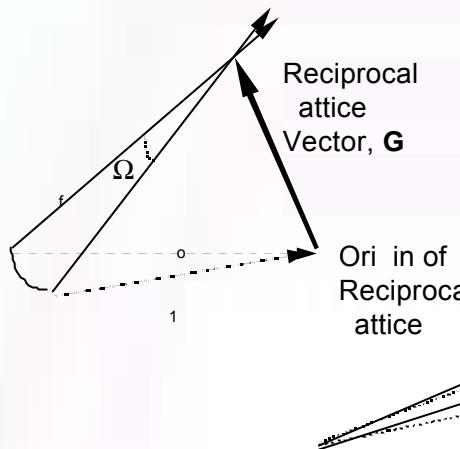
Source: 37 kV, **25 W**

Optic: 5.8 mm input, 136 mn

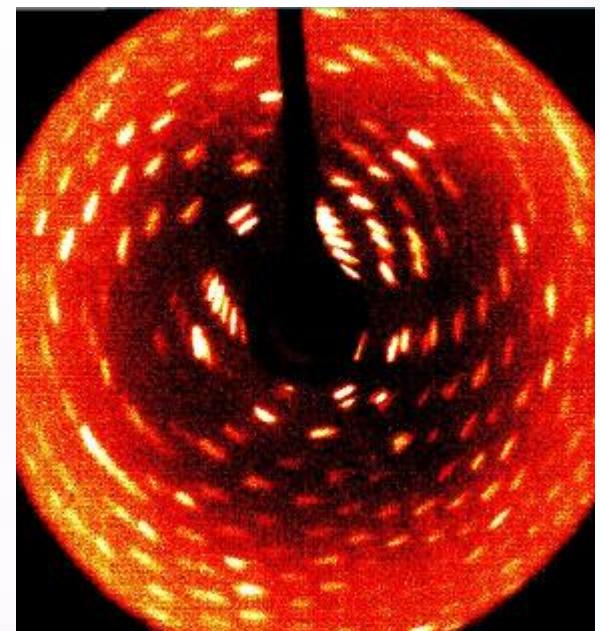
Crystal size	Less than 200 $\mu\text{m}$
oscillation angle	1.5 deg (44 frames)
time / frame	60 min
PINdiode intensity	$3 \times 10^{-4}$
resolution	2.0 $\text{\AA}$
R-factor	5.2%



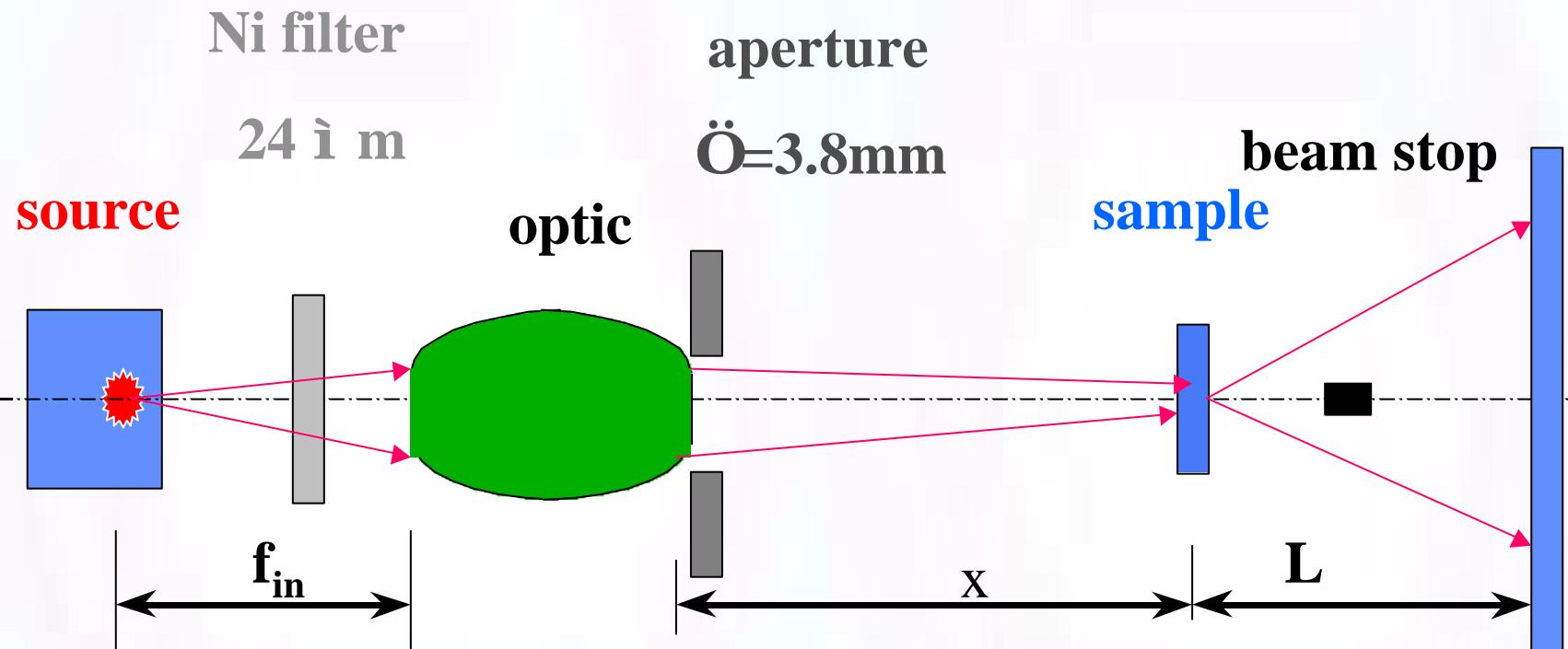
# Applications: Protein Crystallography



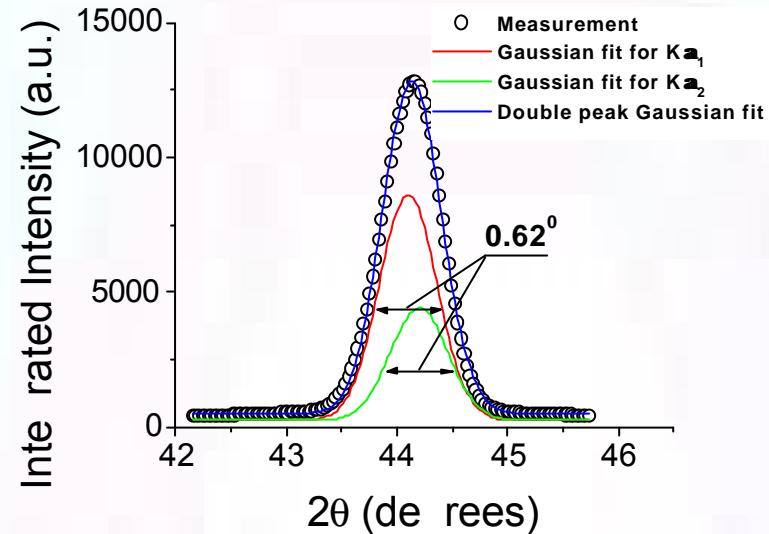
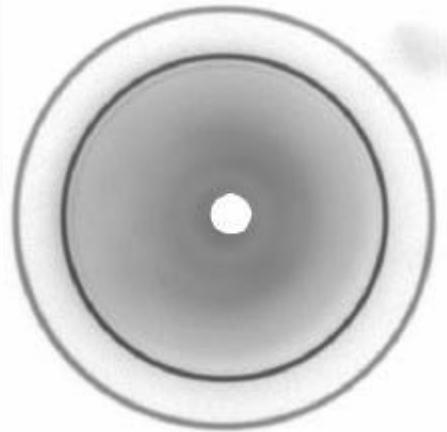
5 min  
1 mA  
2.1



# Applications: Powder Diffraction

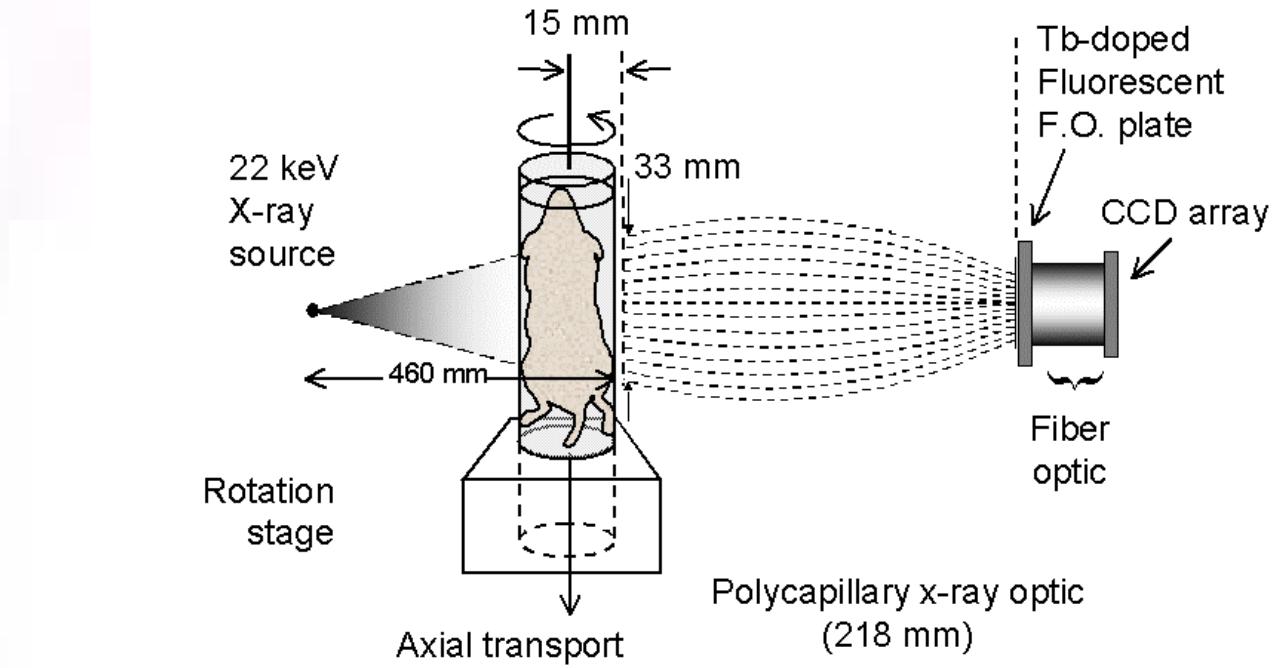


# Applications: Powder Diffraction



Optic Results	Relative diffracted beam Intensity	at sample at focus, plate at 66-75 mm	
		Peak width	Avera Pea error
one	1	0.7	0.23
f 47	5	1.1	0.3
f 119	113	1.9	0.2

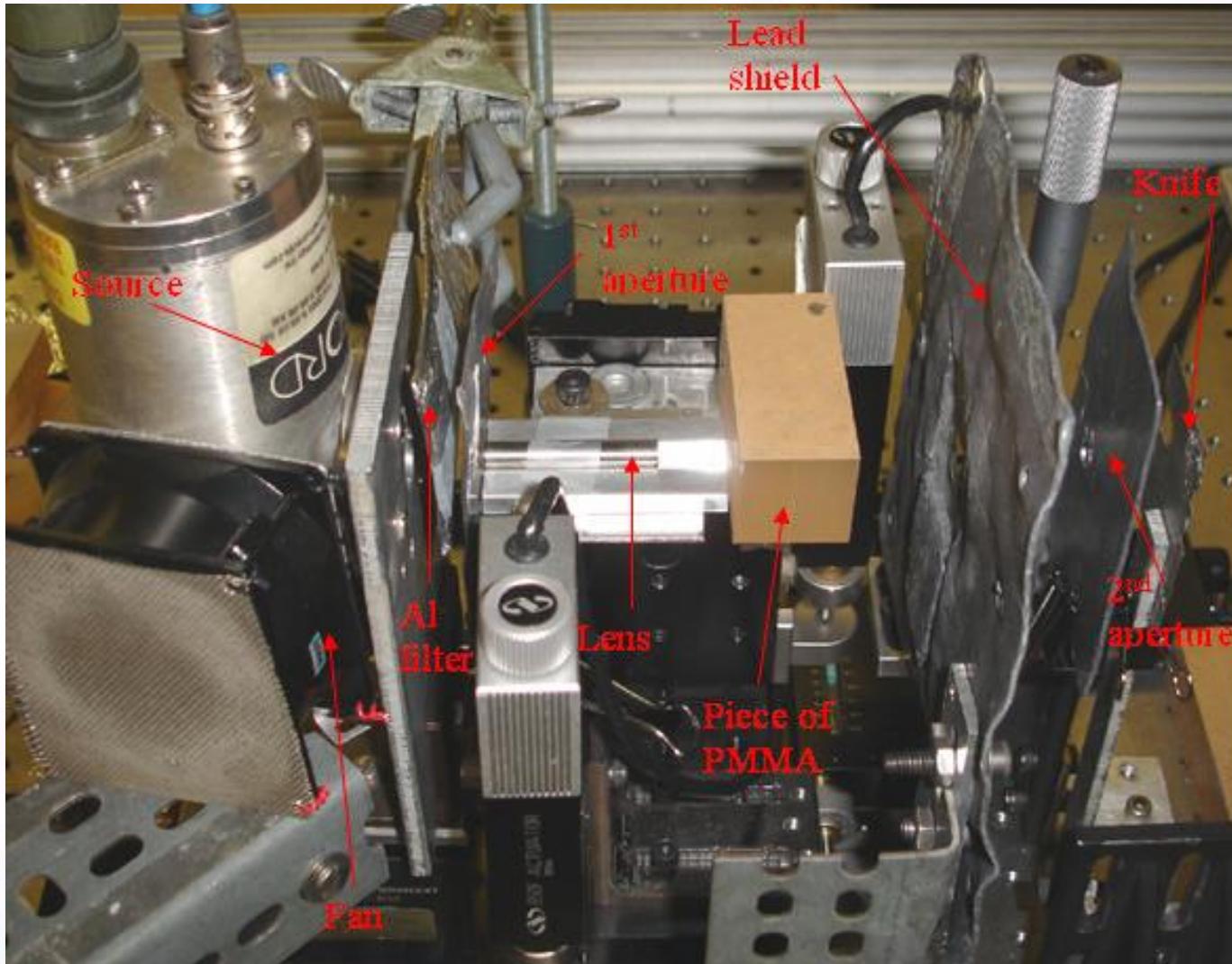
# Applications: mSPECT/CT



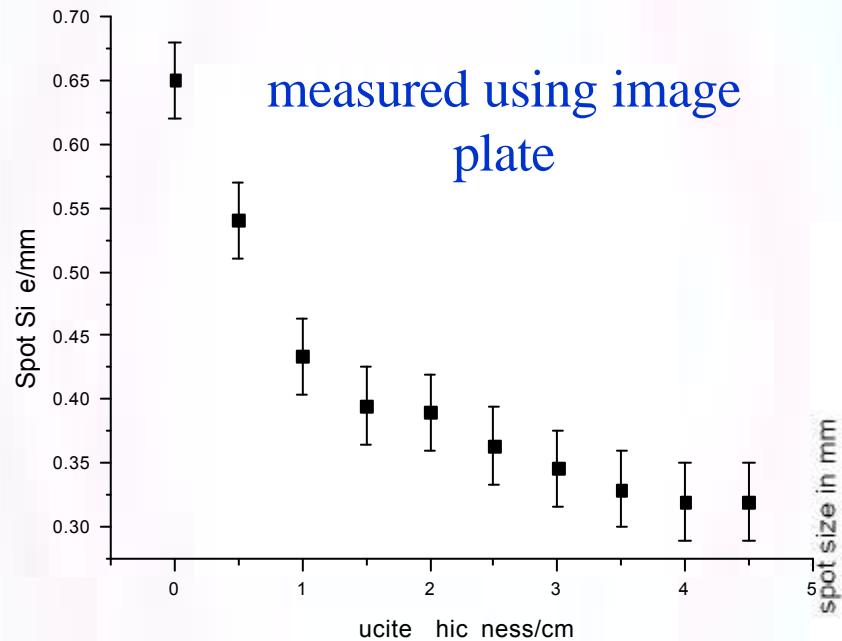
E. Ritman et al., Mayo clinic

## Applications: Orthovoltage Therapy

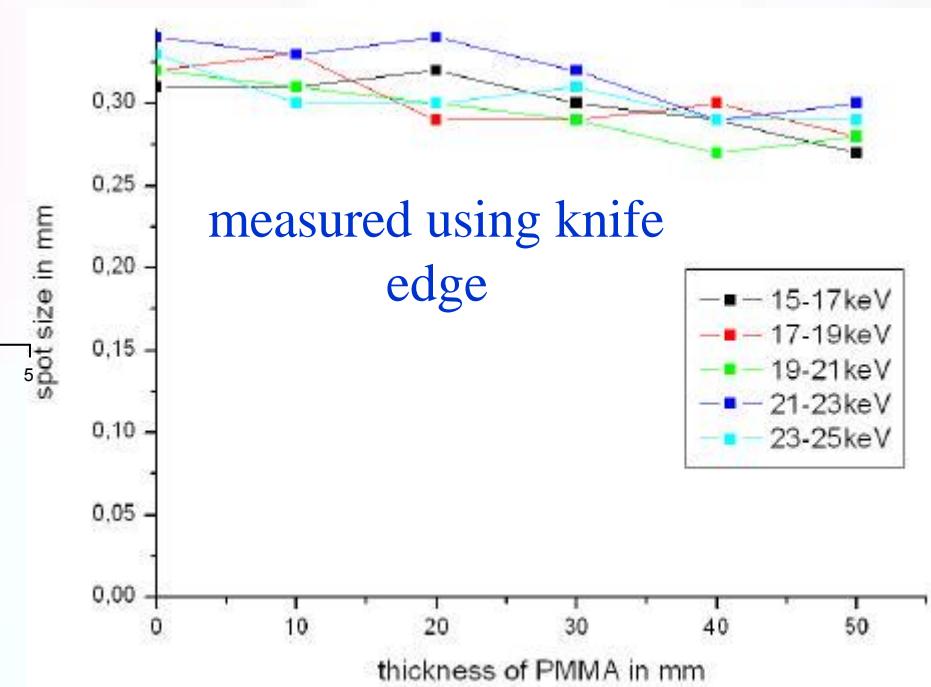
Will the spot size increase due to intervening “tissue”?



# Applications: Orthovoltage Therapy



**Beam hardening**



# Applications: Synchrotron Focusing and Astronomy

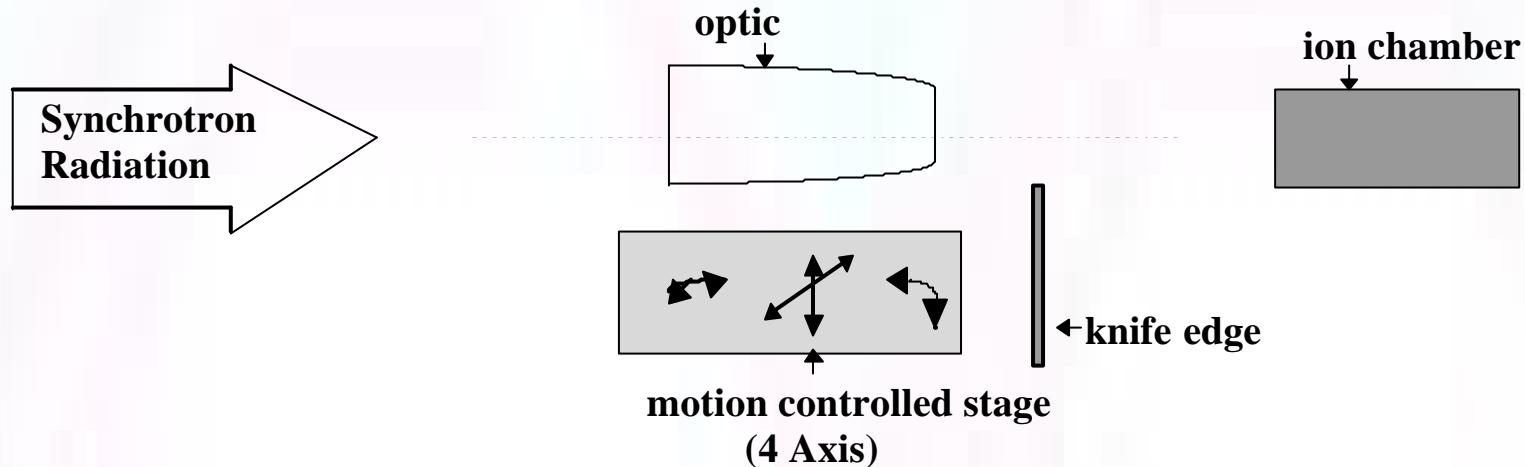


Table 1. Results for monolithic focusing optic.

X-Ray Energy (eV)	Spot size (mm)	transmission (%)	measured Gain 350 $\mu\text{m}$ pinhole	calculated Gain 350 $\mu\text{m}$ pinhole	calculated Gain 90 $\mu\text{m}$ pinhole	calculated Gain 10 $\mu\text{m}$ pinhole
6	0.09	36	78	81	645	911
8	0.08	49	96	110	933	1359
10	0.09	39	83	87	624	842
12	0.09	39	74	87	654	903
white	0.17	42	11	89	243	266

## References

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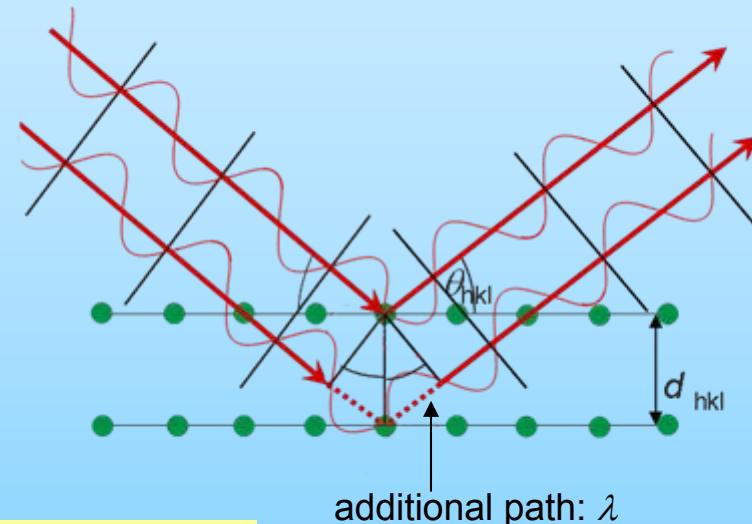
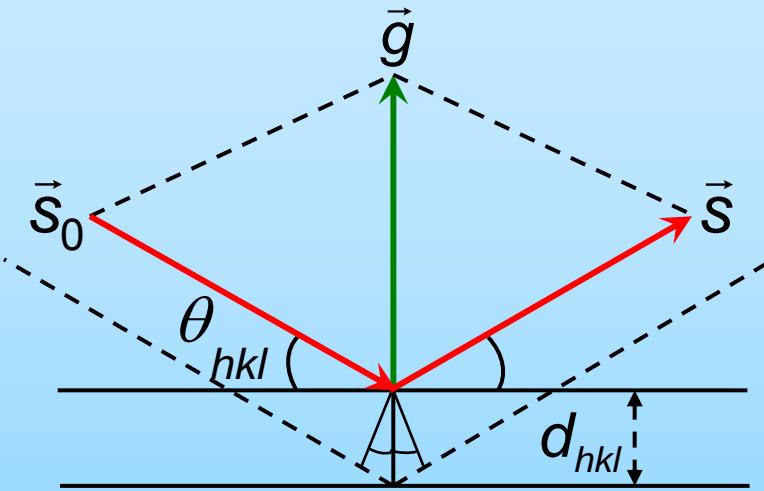
# FOCUSING OF X-RAYS USING CRYSTAL OPTICS

Eckhart Förster

Friedrich-Schiller-University Jena,  
Institute for Optics and Quantum Electronics,  
X-Ray Optics Group  
07743 Jena, Germany

Workshop: Focus on X-Ray Focusing, San Diego, August 13, 2008

## Real space



$$n \lambda = 2 d_{hkl} \sin \theta_{hkl}$$

$\vec{s}_0$ : incident beam wave vector

$\vec{s}$ : Bragg reflected beam wave vector

$\theta_{hkl}$ : Bragg angle

$d_{hkl}$ : distance between the reflecting planes

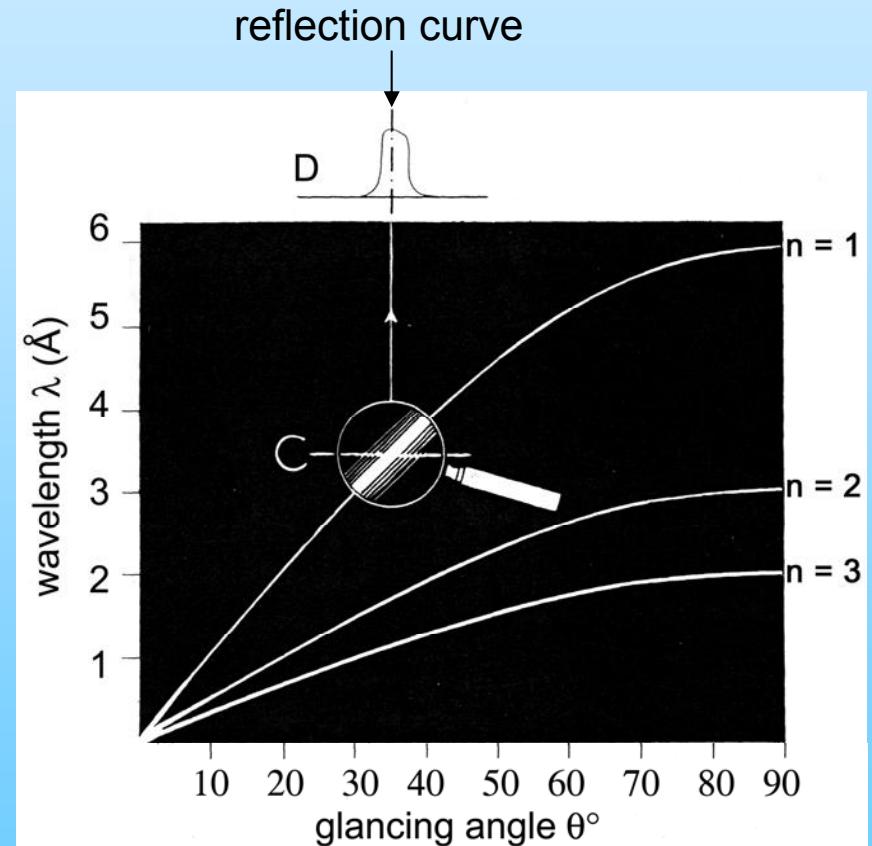
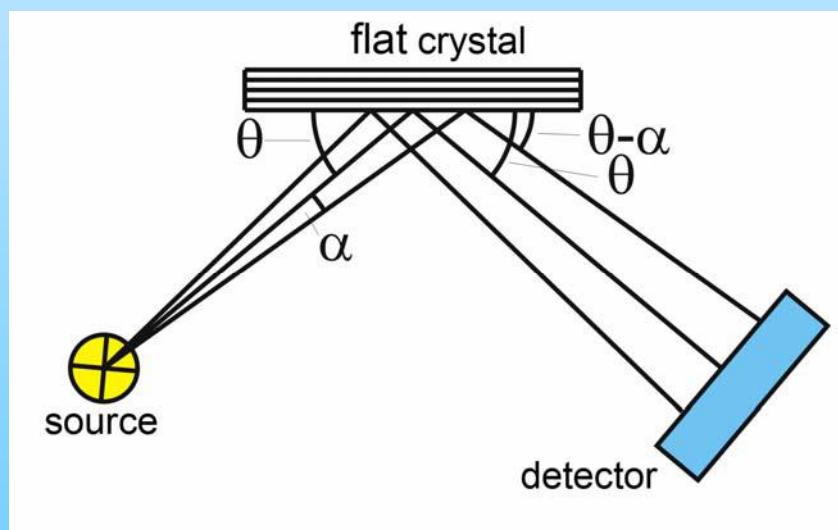
$\vec{g}$  normal of reflecting planes,  
reciprocal lattice vector

$hkl$  indices of reflecting planes

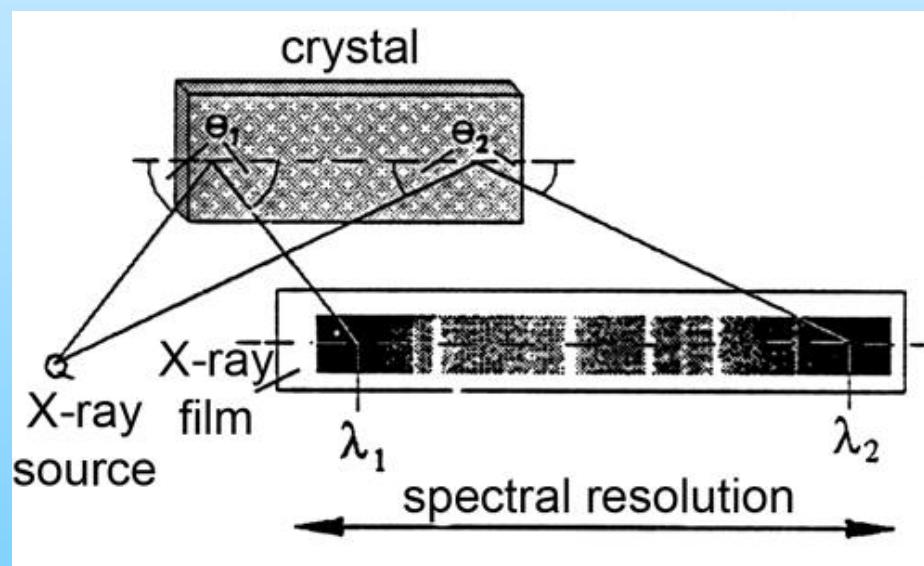
$n$  1, 2, ..., diffraction order

# Scheme of Bragg-Reflection: DuMond-Graphs

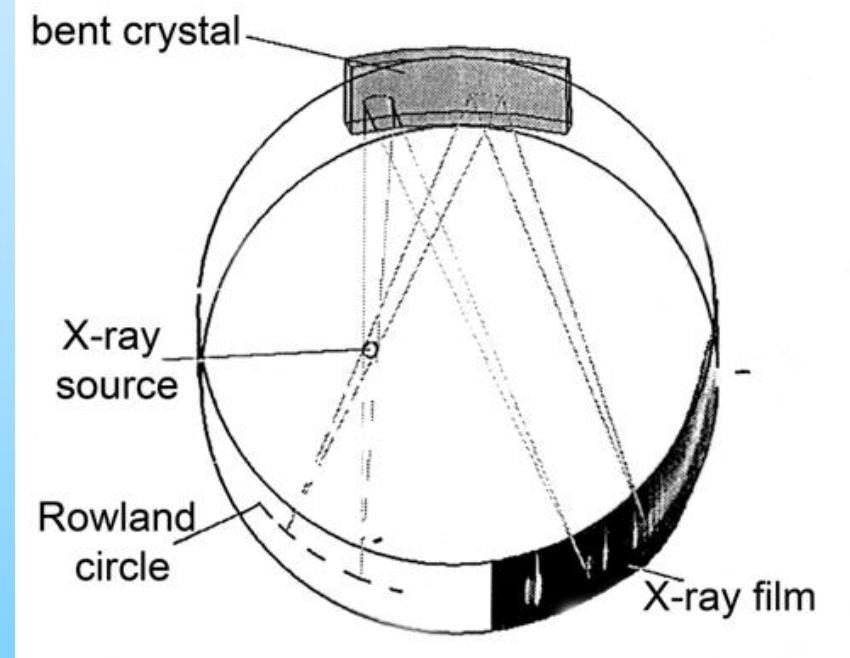
flat crystal, symmetrical reflection  
 $n \lambda = 2 d \sin \theta$



# X-Ray Spectrometer with Flat and Bent Crystals



X-ray spectrometer  
with a single flat crystal

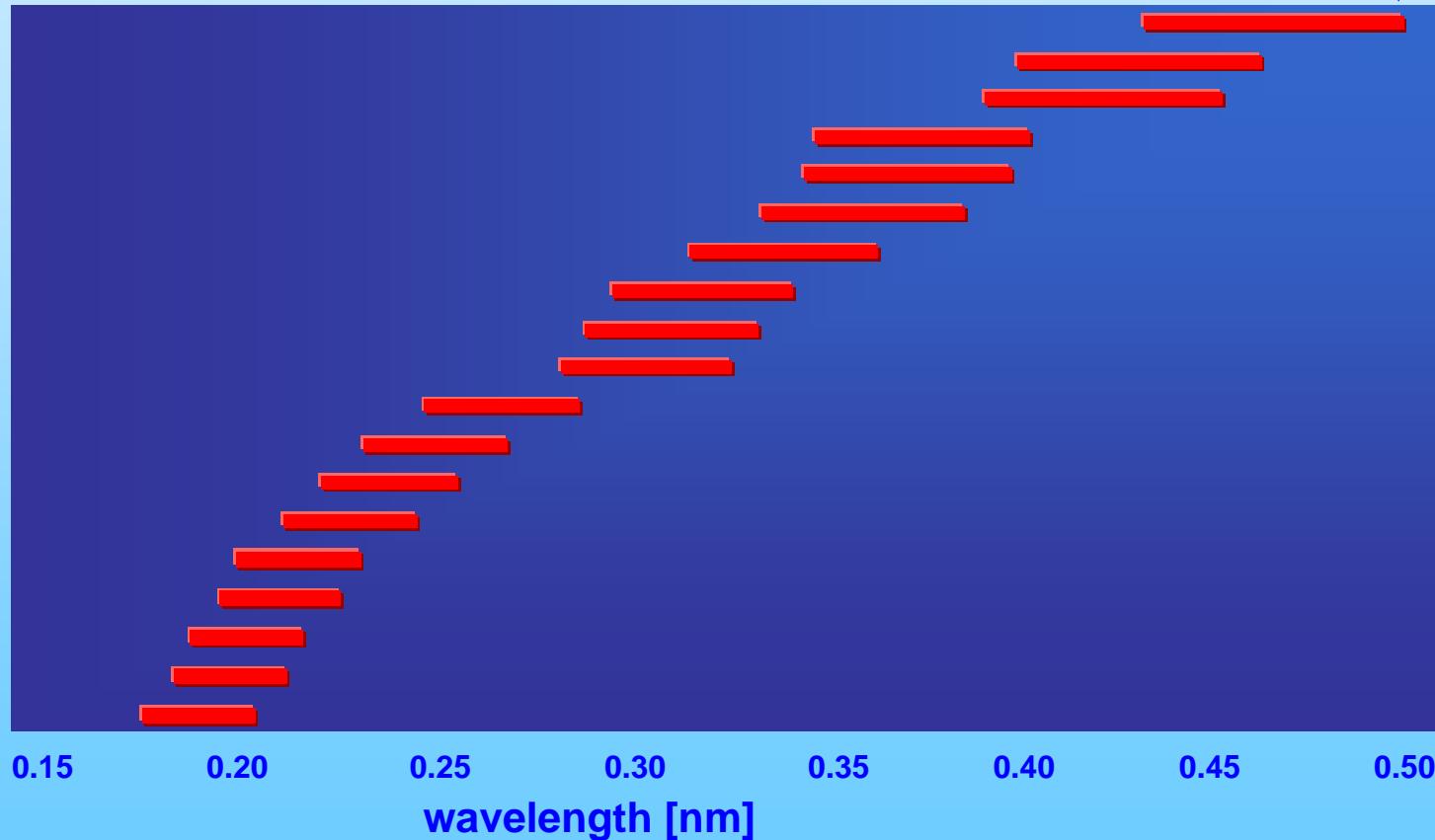


Johann spectrometer  
with a bent crystal

# Application Range of Crystal Reflection

Application range of crystal reflection for Bragg angles  $60^\circ - 89^\circ$

Quartz (11.0)  
 Quartz (10.2)  
 Quartz (11.1)  
 Ge (220)  
 Quartz (20.1)  
 Si (220)  
 Quartz (11.2)  
 Ge (311)  
 Quartz (20.2)  
 Si (311)  
 Ge (400)  
 Si (400)  
 Ge (331)  
 Si (331)  
 Quartz (13.0)  
 Ge (422)  
 Si (422)  
 Ge (333/511)  
 Si (333/511)



X-ray imaging is best, if  $\theta$  is maximal.

# Toroidal Bent Crystals for Focusing of X-Ray from fs Laser Plasma

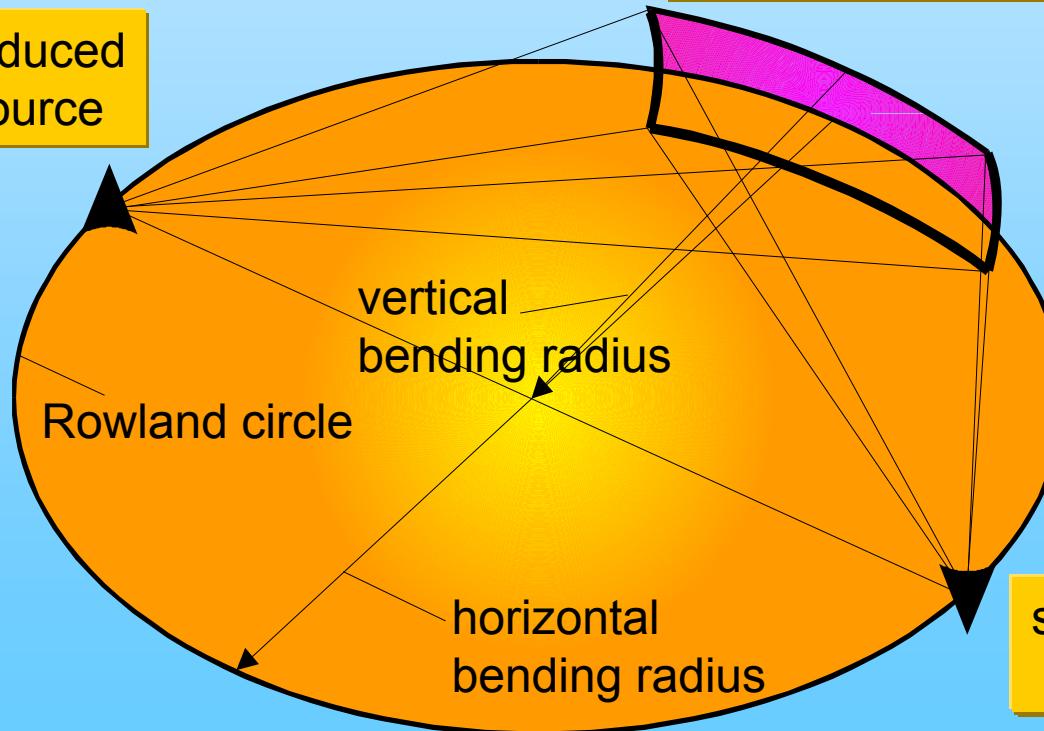
$$\text{focal lengths: } f_h = (R_h/2) \cdot \sin \theta_B$$

$$f_v = R_v/(2 \cdot \sin \theta_B)$$

$$\text{Point to point focussing } R_v / R_h = \sin^2 \theta$$

toroidally bent crystal

laser produced  
X-ray source

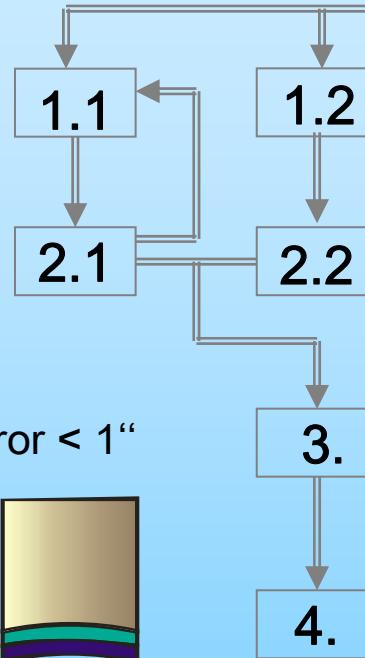
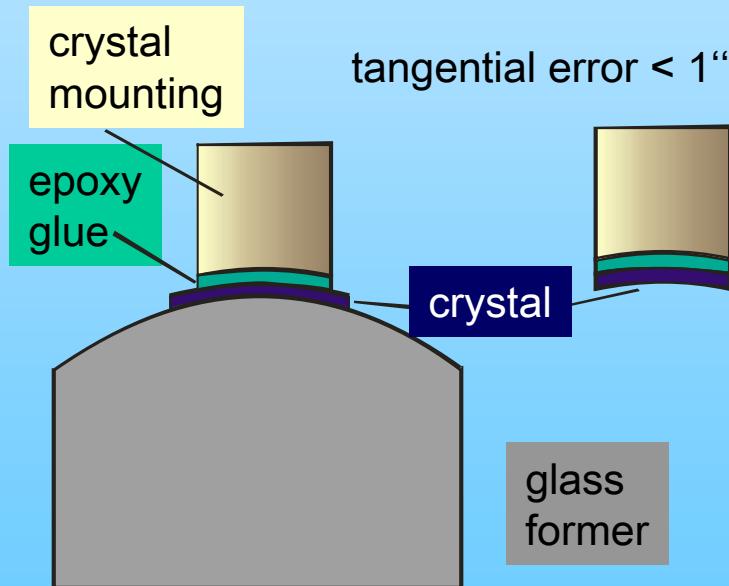


sample crystal

# Fabrication and Test of Toroidally Bent Crystals

grinding and polishing of toroidal glass formers

control of surface quality and bending radius  $\Delta R/R < 0.001$



X-ray topography → 'perfect' crystal block

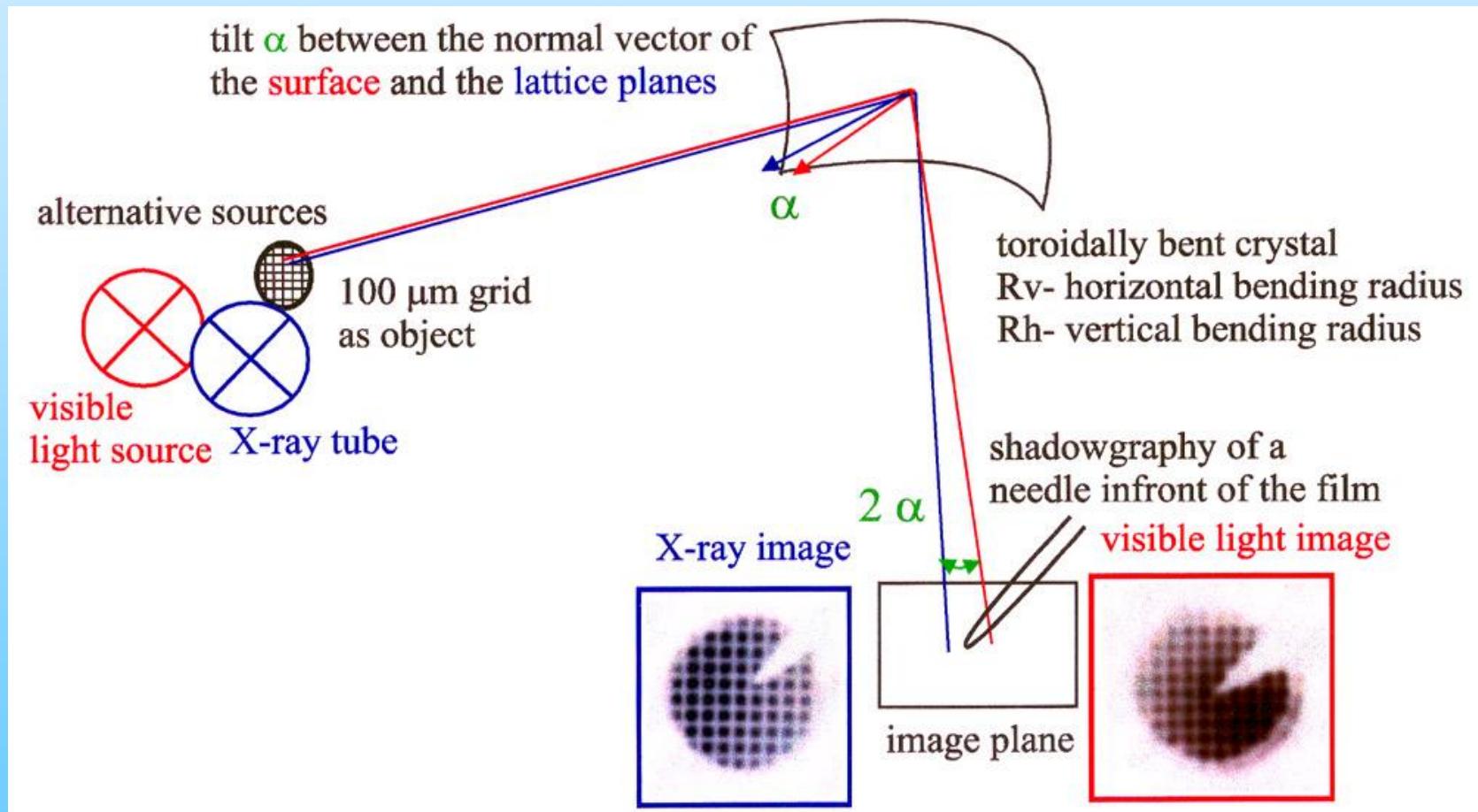
oriented sawing (accuracy: 10' to 10''), grinding, polishing → 70 µm thick discs

optical contact with glass form sticking to crystal mounting with epoxy glue

optical and X-Ray imaging tests,

$$\text{Relation of the Curvature Radii: } R_v/R_h = \sin^2\theta$$

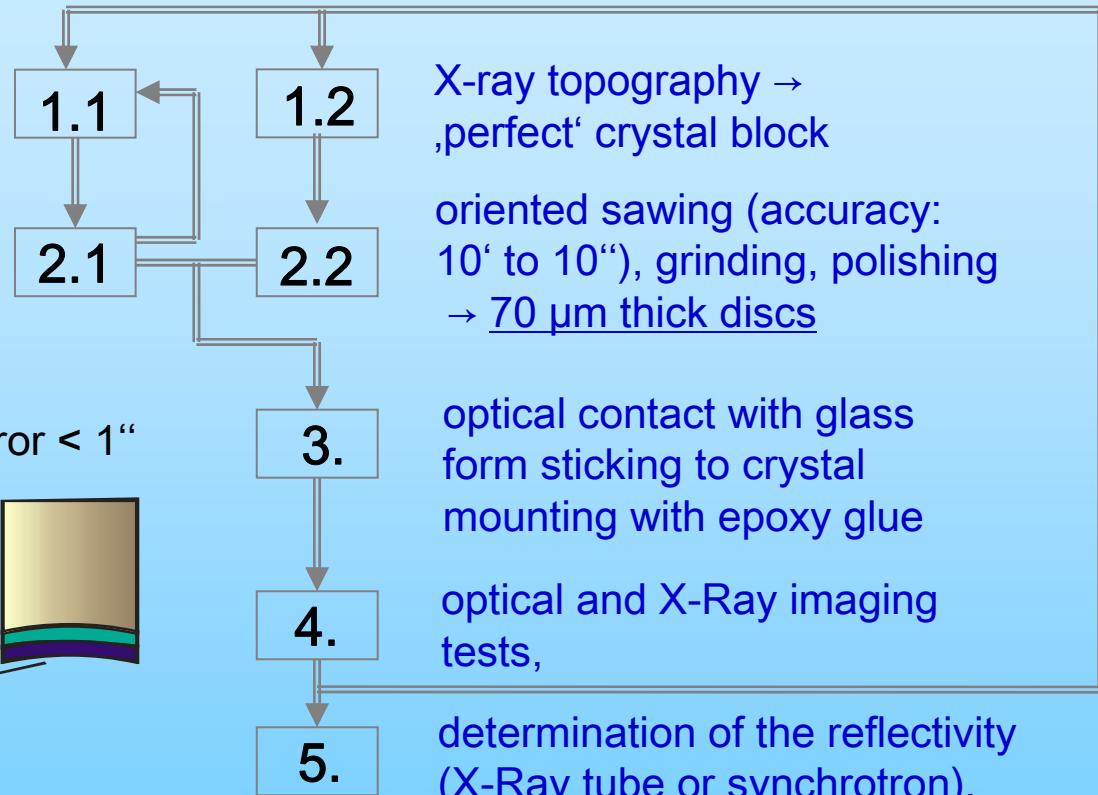
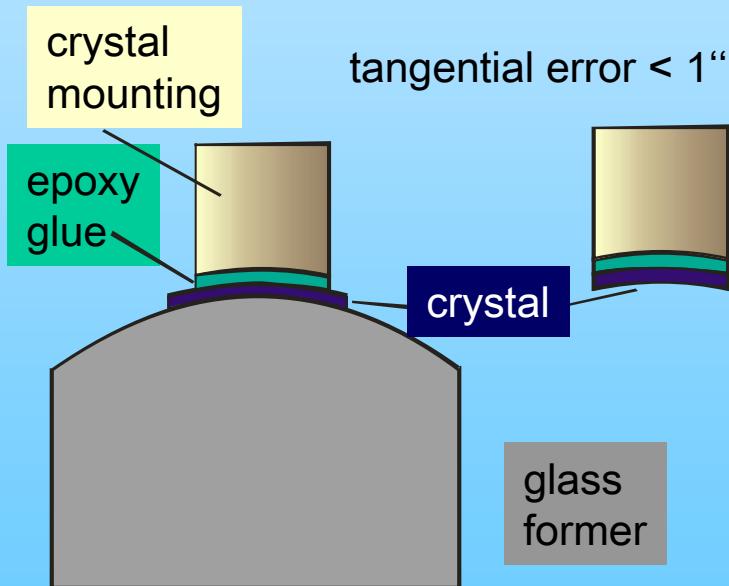
# Test of Bent Crystals for Monochromatic Imaging



# Fabrication and Test of Toroidally Bent Crystals

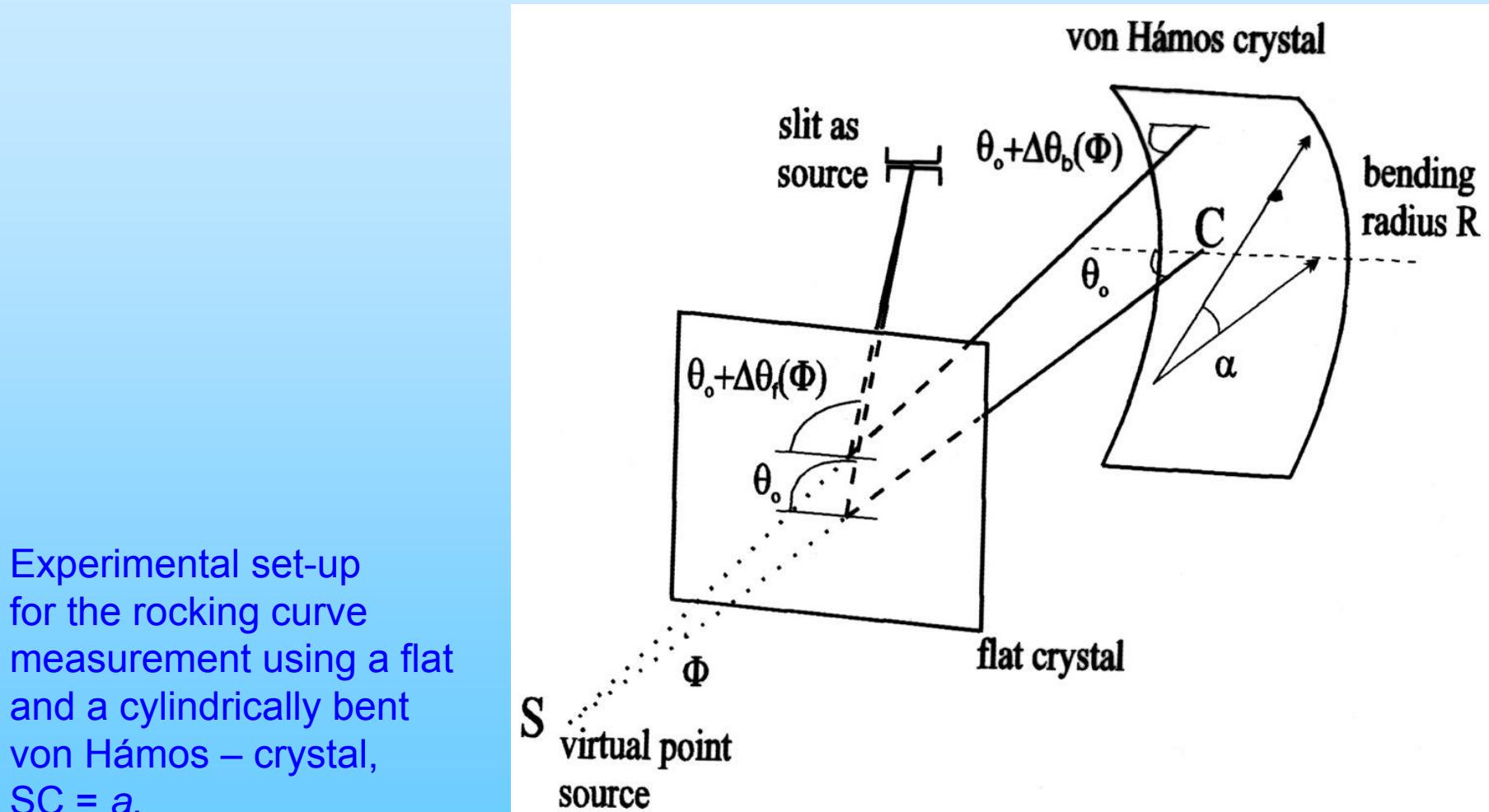
grinding and polishing of toroidal glass formers

control of surface quality and bending radius  $\Delta R/R < 0.001$



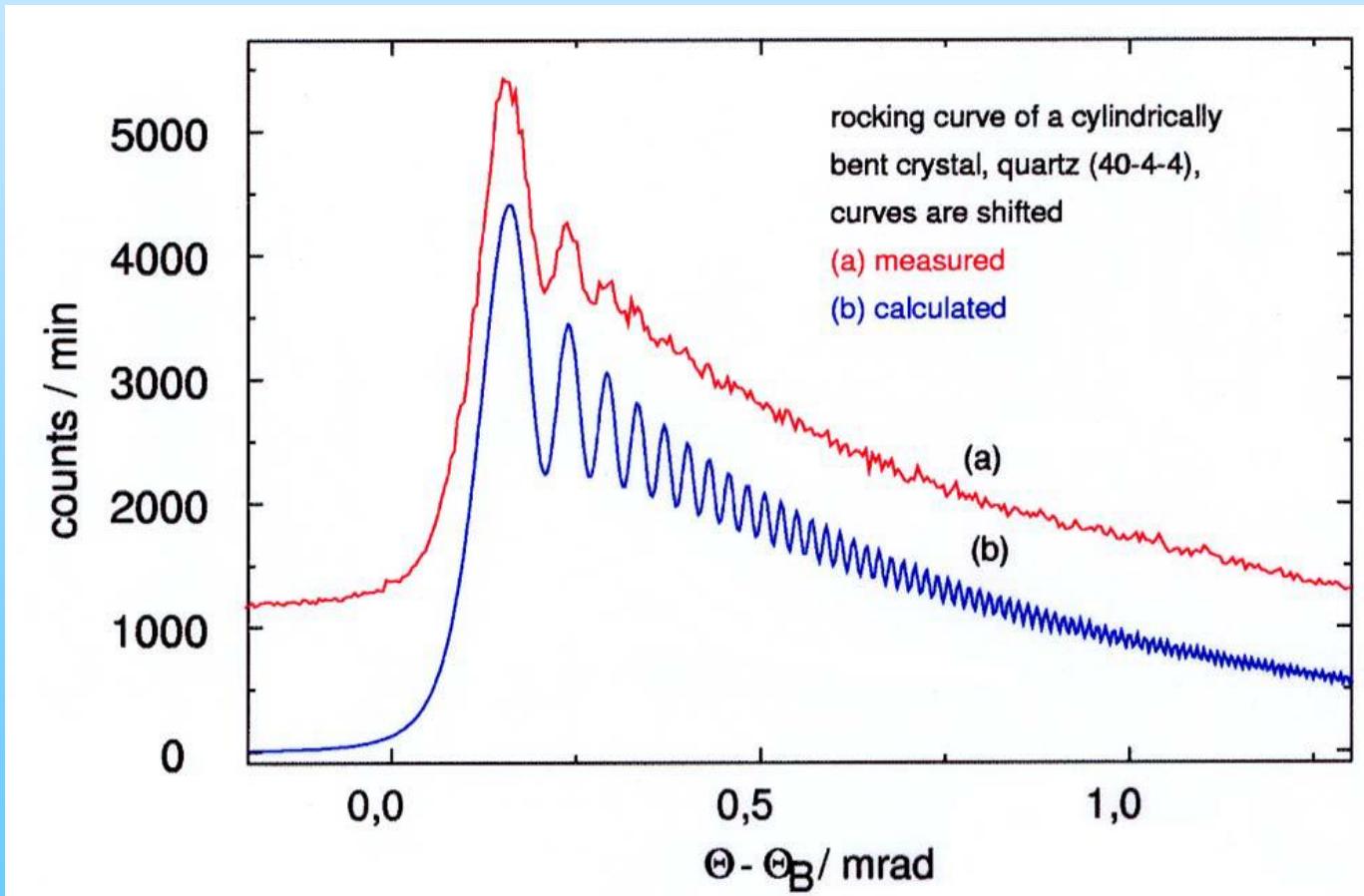
$$\text{Relation of the Curvature Radii: } R_v/R_h = \sin^2\theta$$

# Experimental Setup for Reflection Curve Measurement

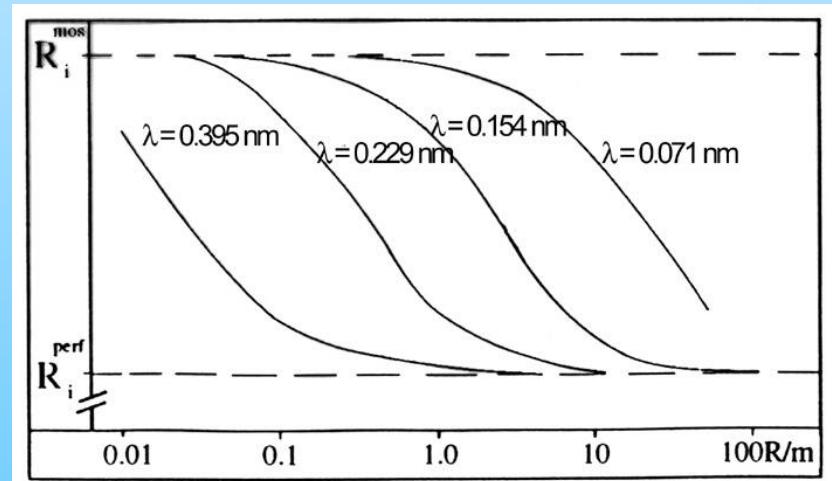
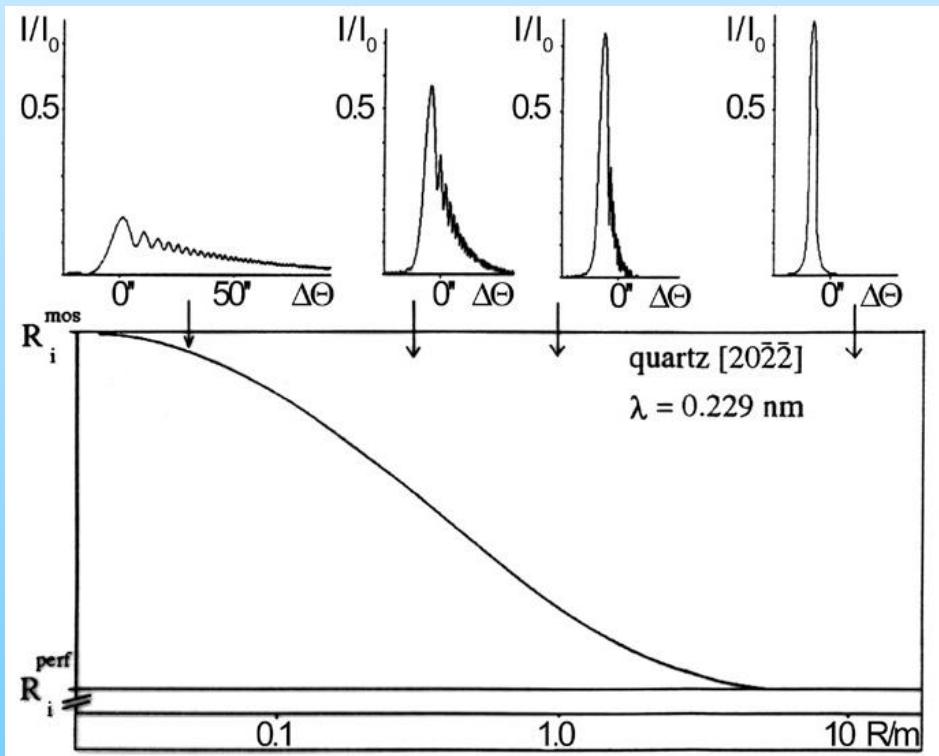


# Reflection Curves of a Cylindrically Bent Quartz 40. $\overline{4}$

$$E_{\text{det}} = \iiint d\alpha d\phi d\lambda J_s(\alpha, \phi, \lambda) \times C \left( \sigma(\alpha, \phi) - \frac{\Delta\lambda}{\lambda} \tan \theta_0 \right)$$



# Dependency of the Reflection Power of the Curvature Radius

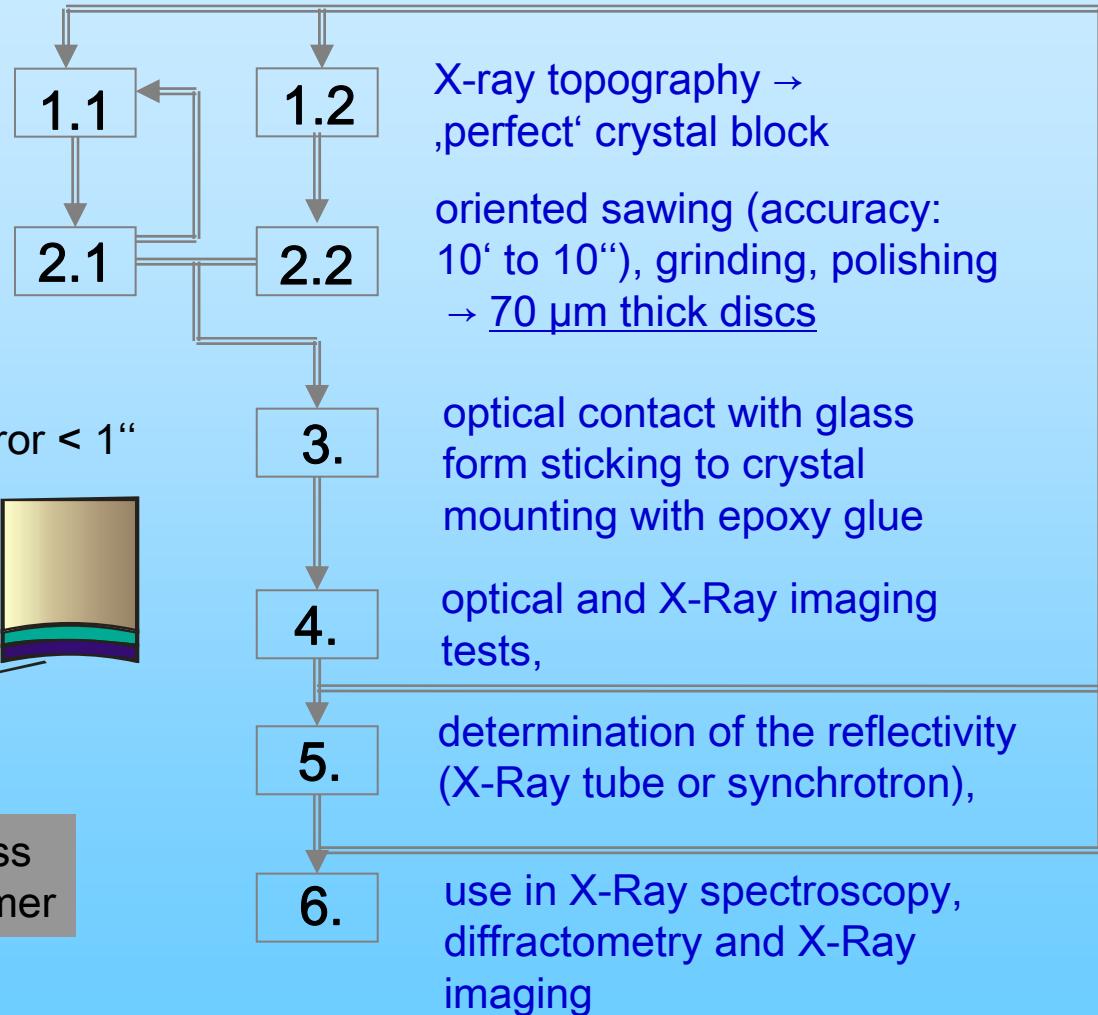
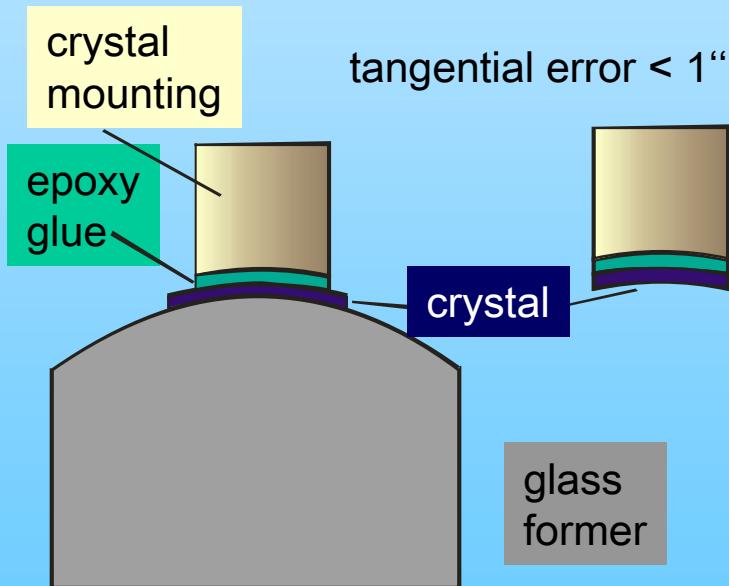


I. Uschmann et al., J. Appl. Cryst. **26** (1993), 405

# Fabrication and Test of Toroidally Bent Crystals

grinding and polishing of toroidal glass formers

control of surface quality and bending radius  $\Delta R/R < 0.001$



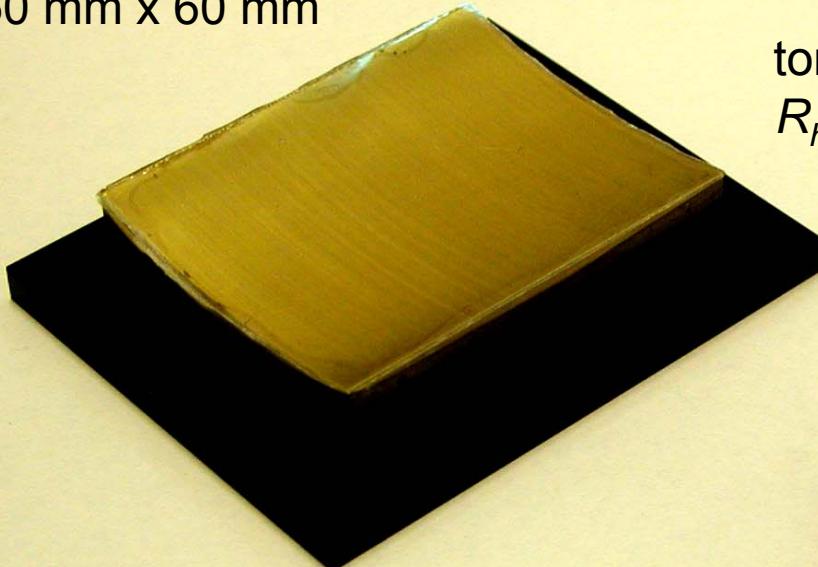
$$\text{Relation of the Curvature Radii: } R_v/R_h = \sin^2\theta$$

# Typical Bent Crystal Parameters

cylindrically bent mica

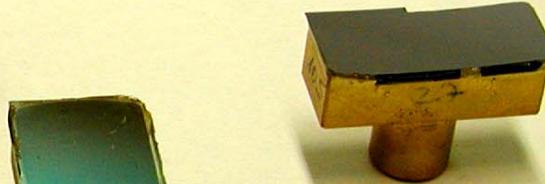
$R = 100$  mm

50 mm x 60 mm



toroidally bent GaAs 400

$R_h = 200$  mm,  $R_v = 189.4$  mm



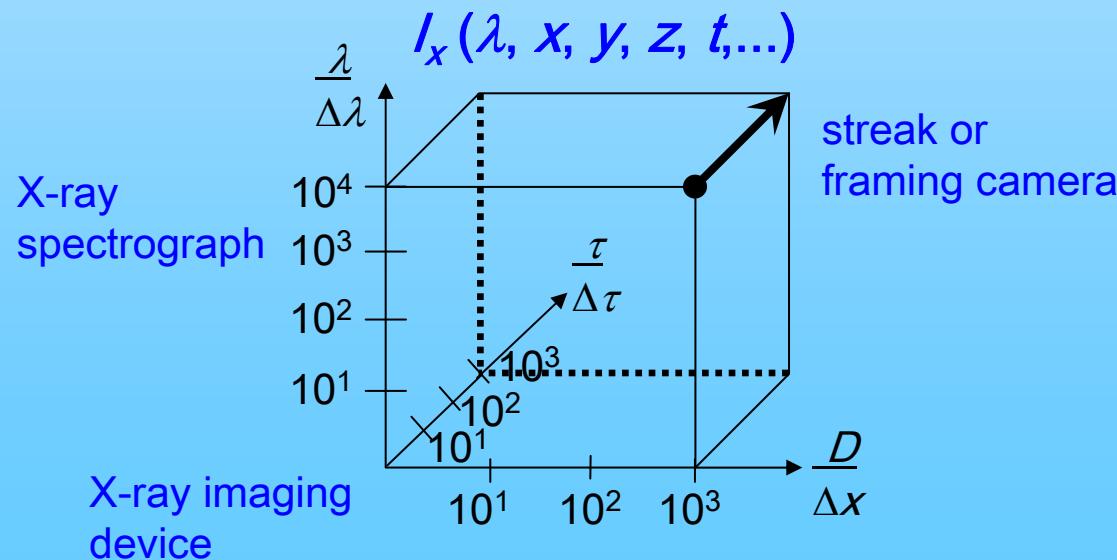
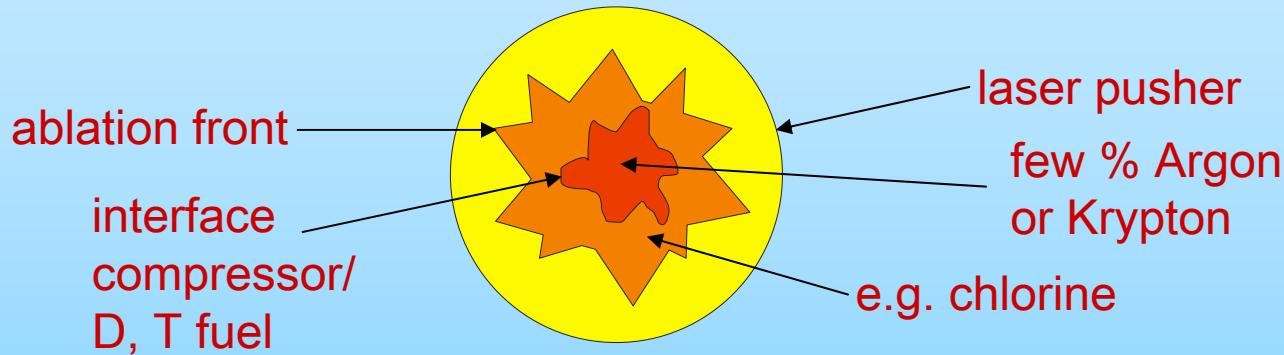
toroidally bent quartz 10.-1

$R_h = 500$  mm,  $R_v = 400$  mm

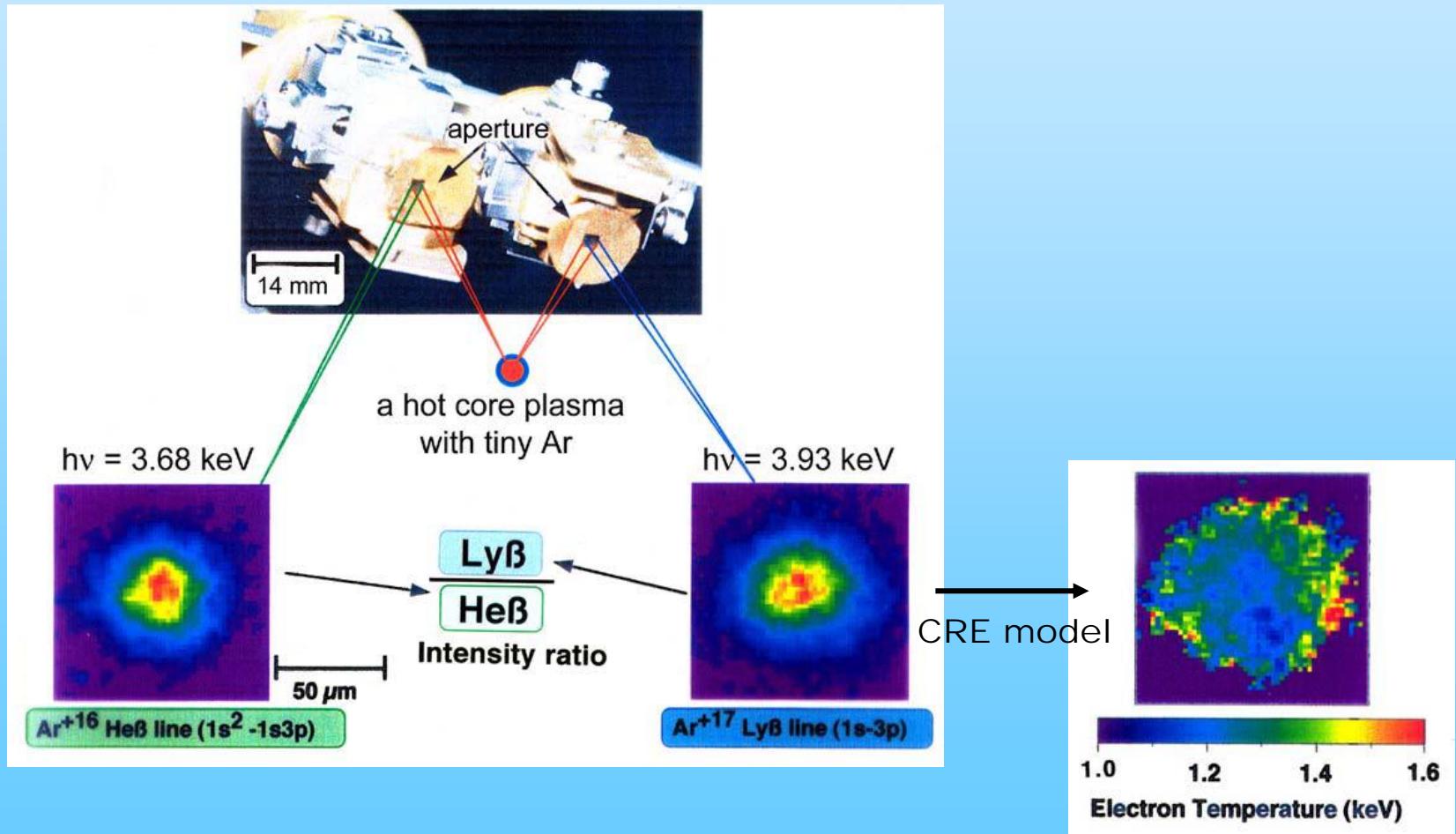


High power laser:  $E_L > 10^6 \text{J}$ ,  $\tau_L < 1\text{ns}$ ,  $\lambda_L < 0.5\mu\text{m}$

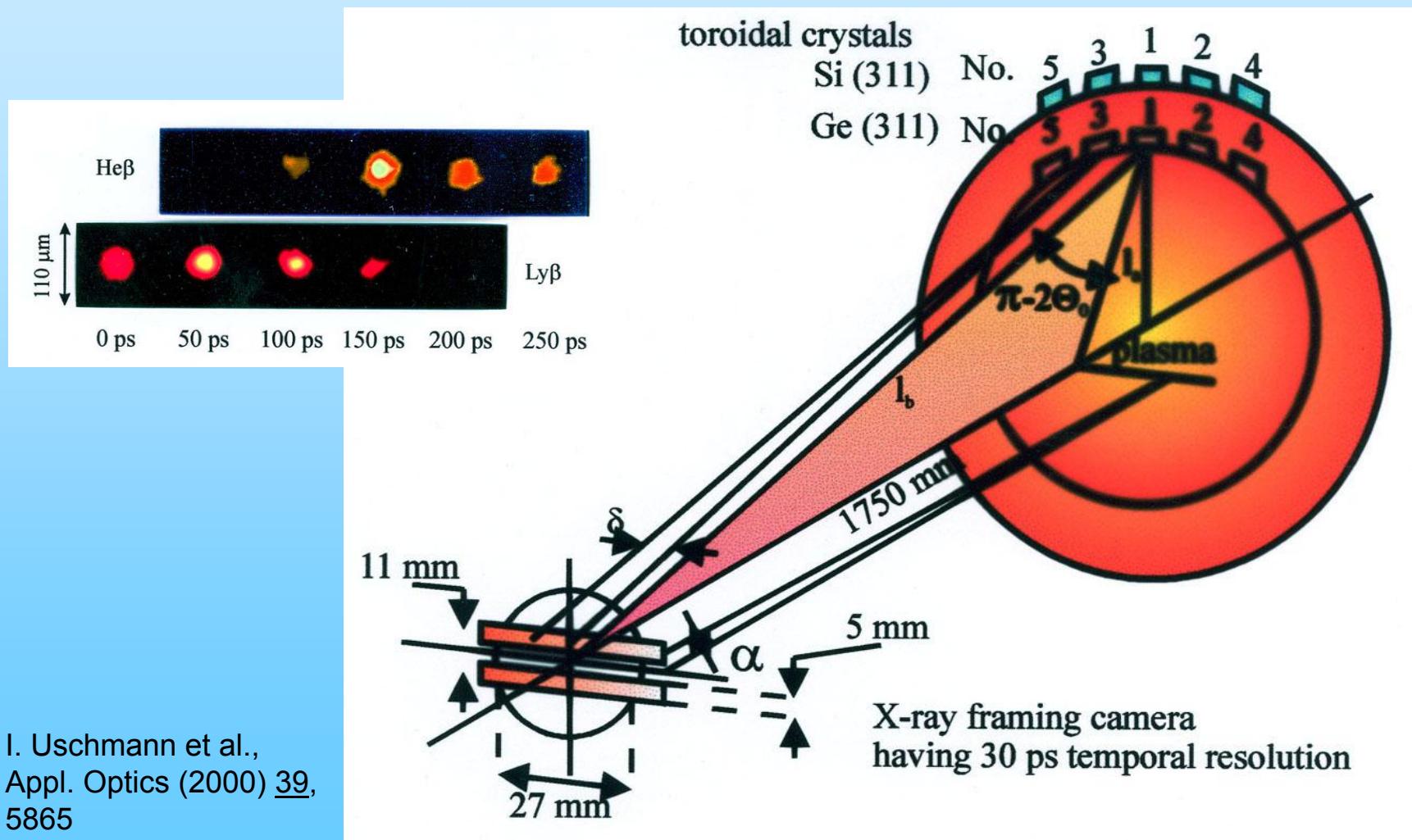
main aim: suppression of Rayleigh-Taylor instabilities



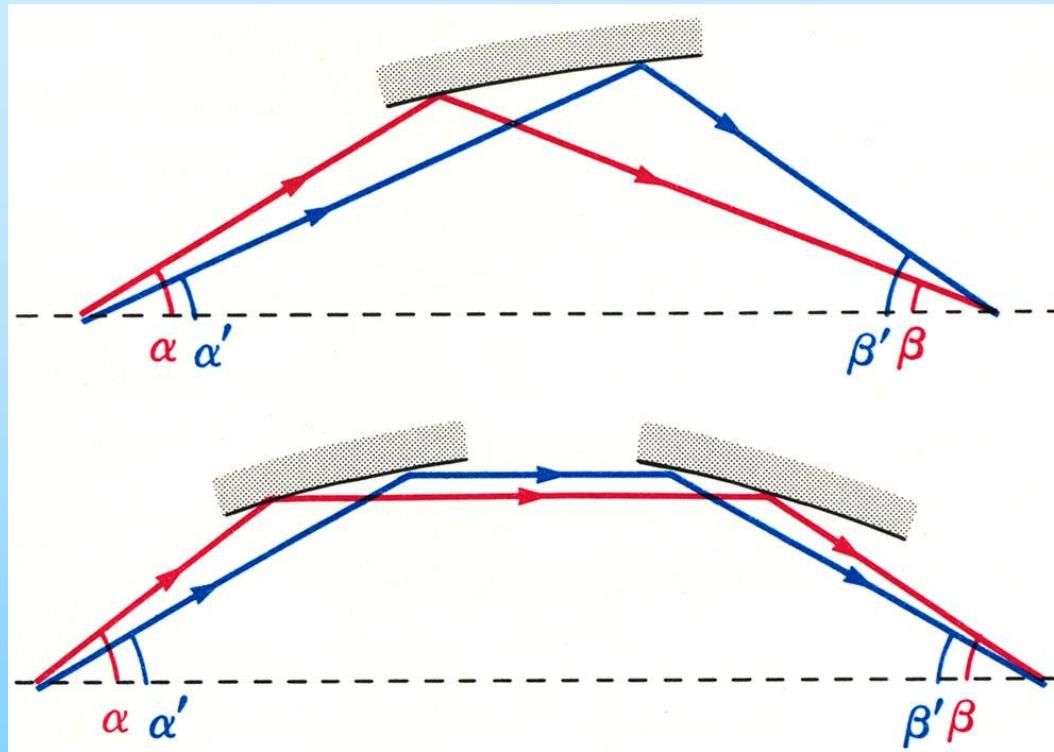
# X-Ray Monochromatic Camera Using Two Toroidal Crystals



# Ten Channel Imaging System

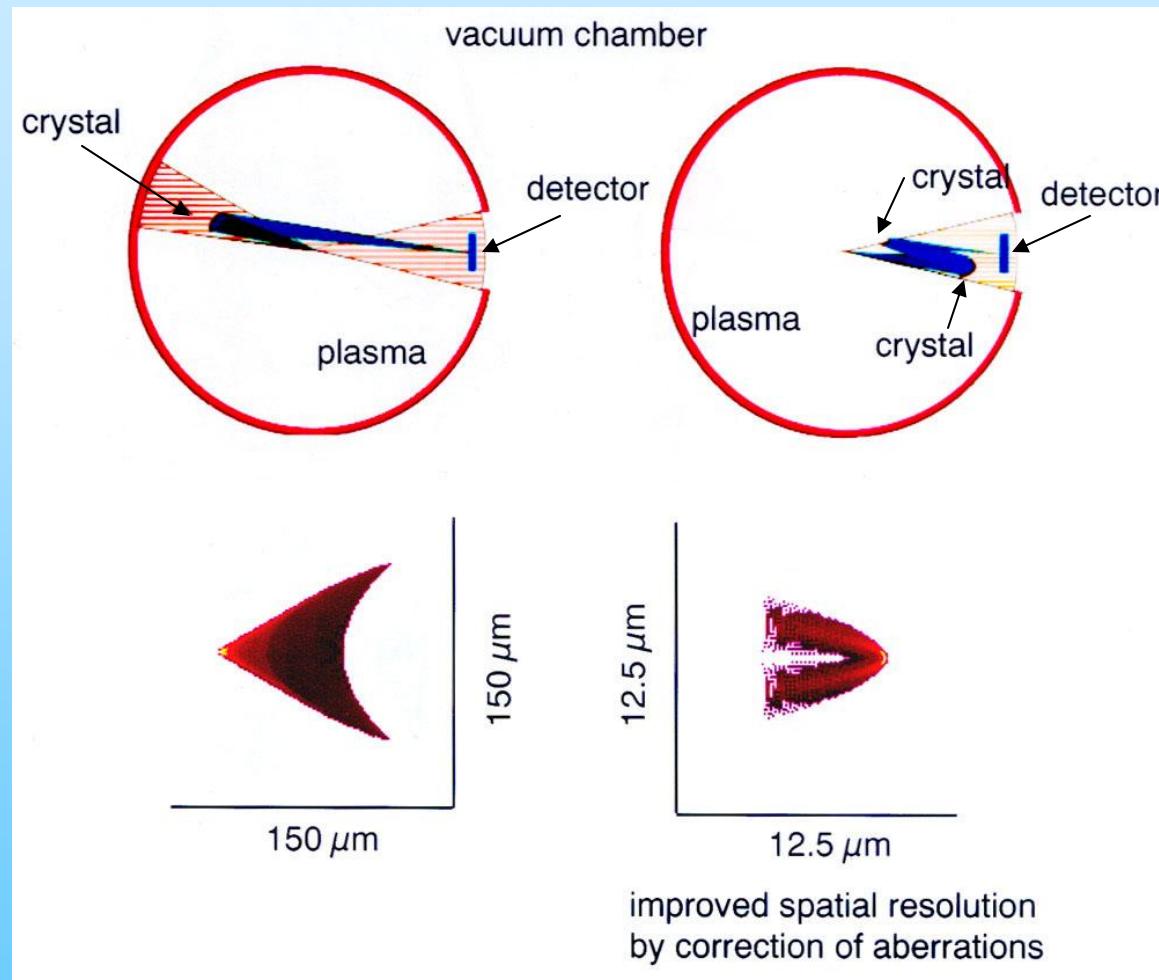


# Abbe Sine Condition



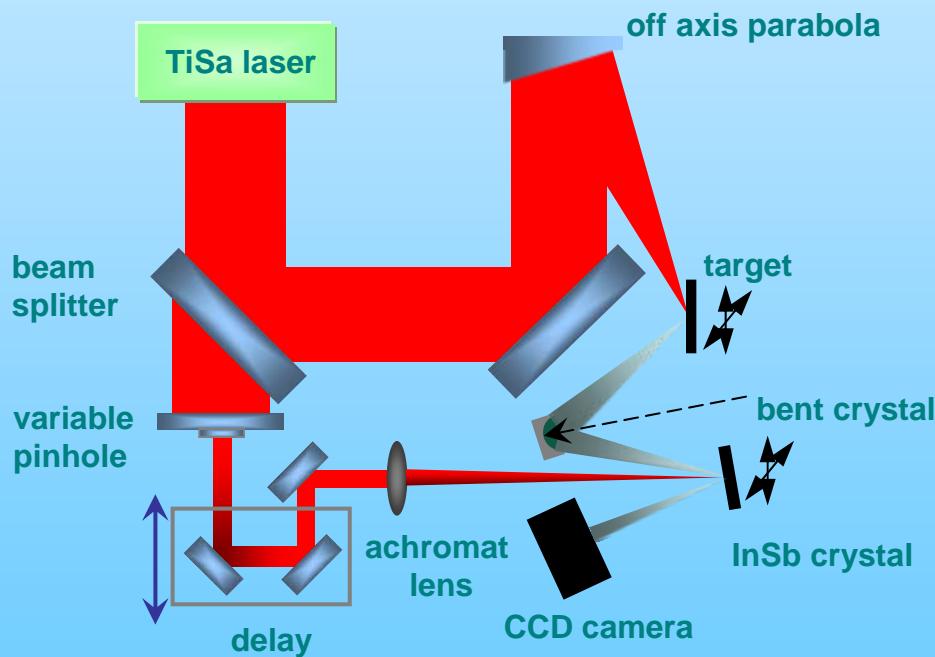
Coma can be corrected in X-ray optical systems with the use of two mirrors. A single X-ray mirror strongly violates the Abbe sine condition, since  $\beta$  increases as  $\alpha$  decreases, while the sine condition demands, that  $\sin\alpha / \sin\beta$  remain constant (upper diagr.). Approximate constancy of the sine ratio can be achieved through the use of two mirrors (lower diagr.), so that  $\beta$  increases as  $\alpha$  increases.

# Two Crystal Scheme for X-Ray Monochromatic Imaging of Ultradense Plasmas



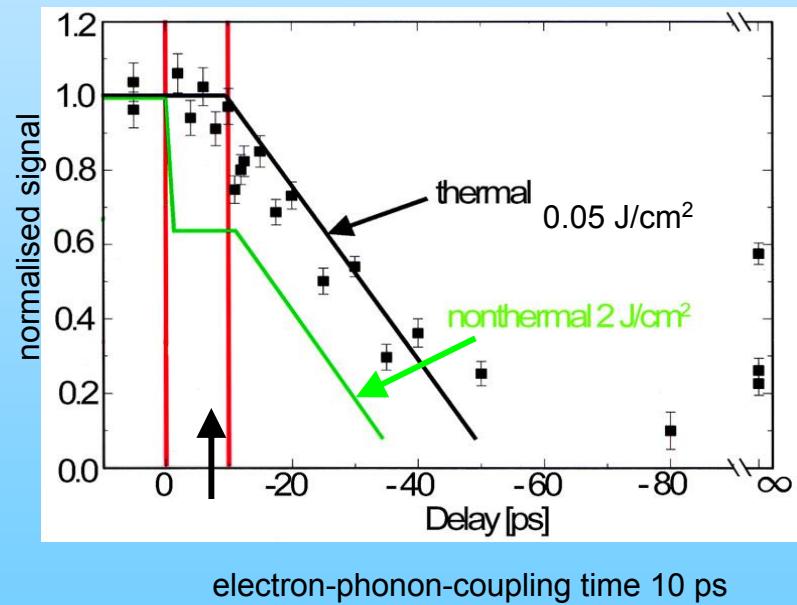
	one crystal	two crystals
spatial resolution	14 $\mu\text{m}$	1.6 $\mu\text{m}$
spectral window ( $\lambda/\Delta\lambda$ )	235	6069
relative luminosity	1	1/15

## Setup of an Optical Pump X-Ray Probe Experiment



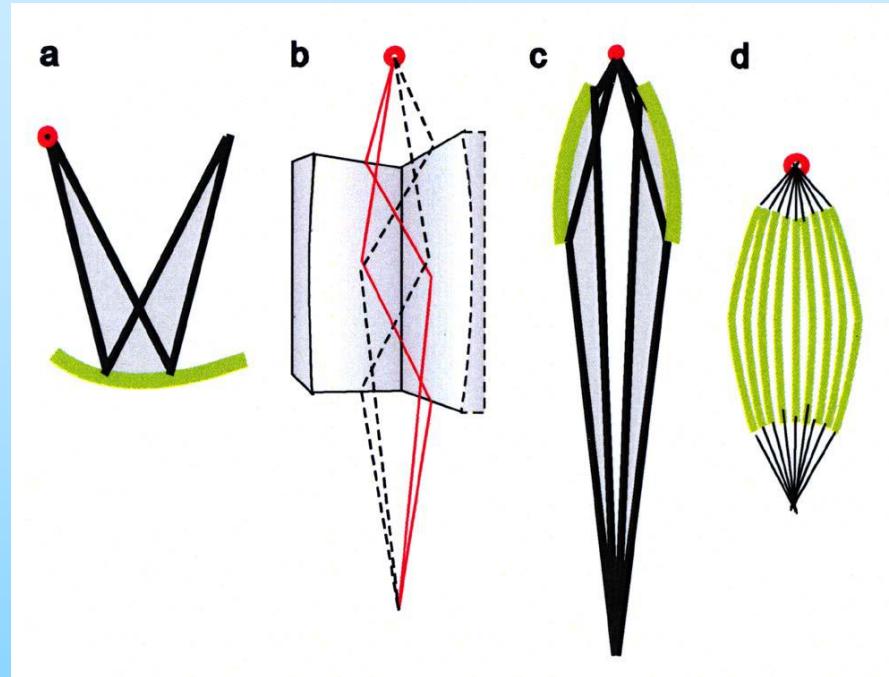
T. Feurer et al., Appl. Phys. B (2001) 72, 15

## Non-thermal Melting: InSb X-ray signal ( $7 \cdot 10^{16} \text{ W/cm}^2$ )



A. Rousse et al., Nature, 410, No. 6824 (2001) 65 - 68

# Schematic of Four Cu K $\alpha$ Optics



- a. toroidally bent Ge crystal, 444 reflex,  $\theta = 70^\circ$ ,
- b. two perpendicular elliptical Ni/C multilayer mirrors,  $\theta \approx 3^\circ$ ,
- c. ellipsoidal lead-glass capillary,
- d. borosilicate poly-capillaries (59,000).

# Characteristic Parameters of Cu K $\alpha$ Optics

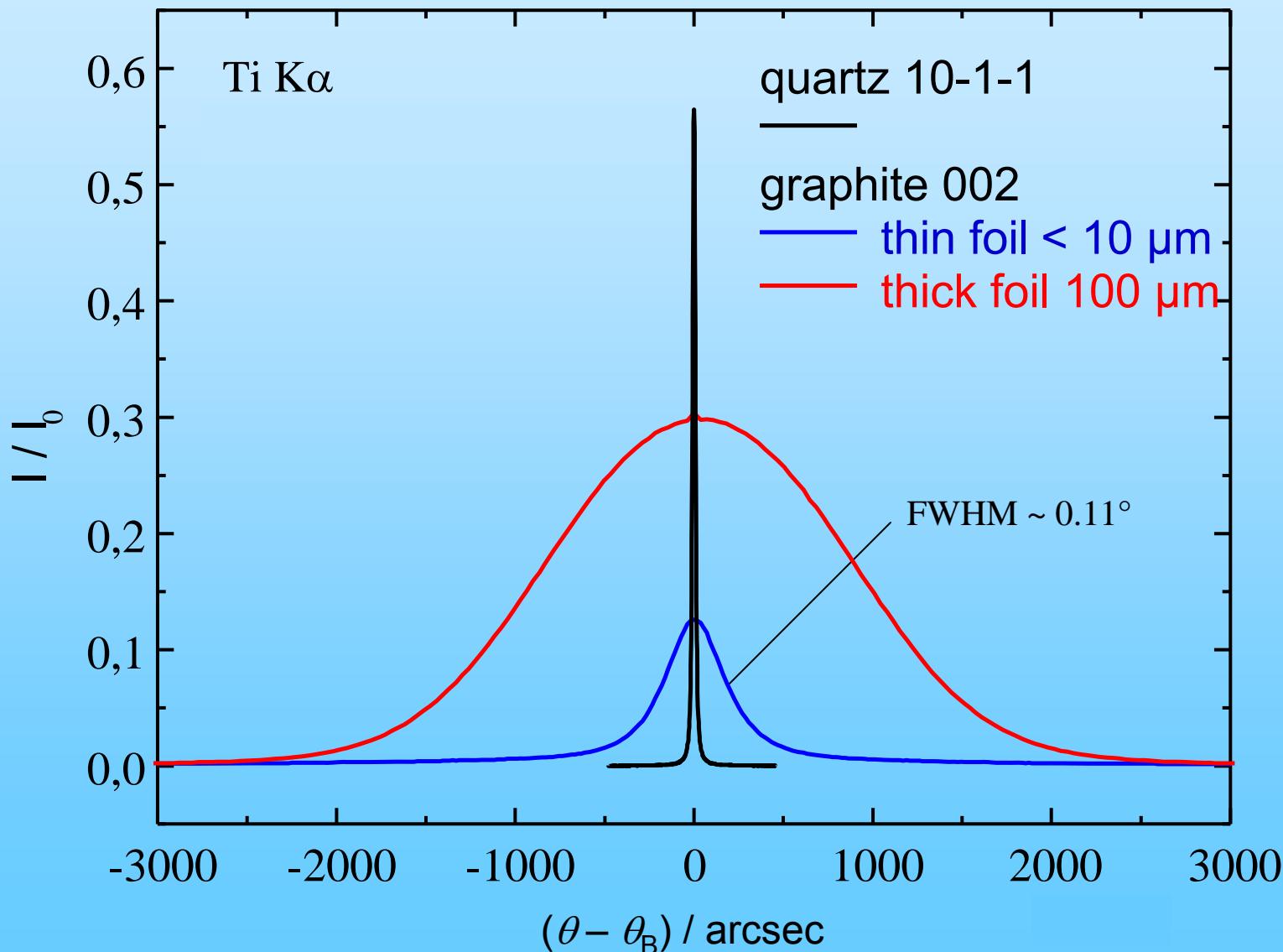
CuK $\alpha$ optics	toroidal Ge	multilayer mirror system	ellipsoidal capillary	Poly-capillaries
size of focus ( $\mu\text{m}$ )	23	32	155	105
1D-convergence angle (deg)	1.5	0.45	0.2	3.5
solid angle (sr)	$2.3 \cdot 10^{-3}$	$8.8 \cdot 10^{-4}$	$4.0 \cdot 10^{-4}$	$1.1 \cdot 10^{-2}$
reflectivity or transmission	0.03	0.2	0.8	0.09
suppression of K $_{\beta}$	0.017	$5 \cdot 10^{-4}$	1.4	1.7

red – best value

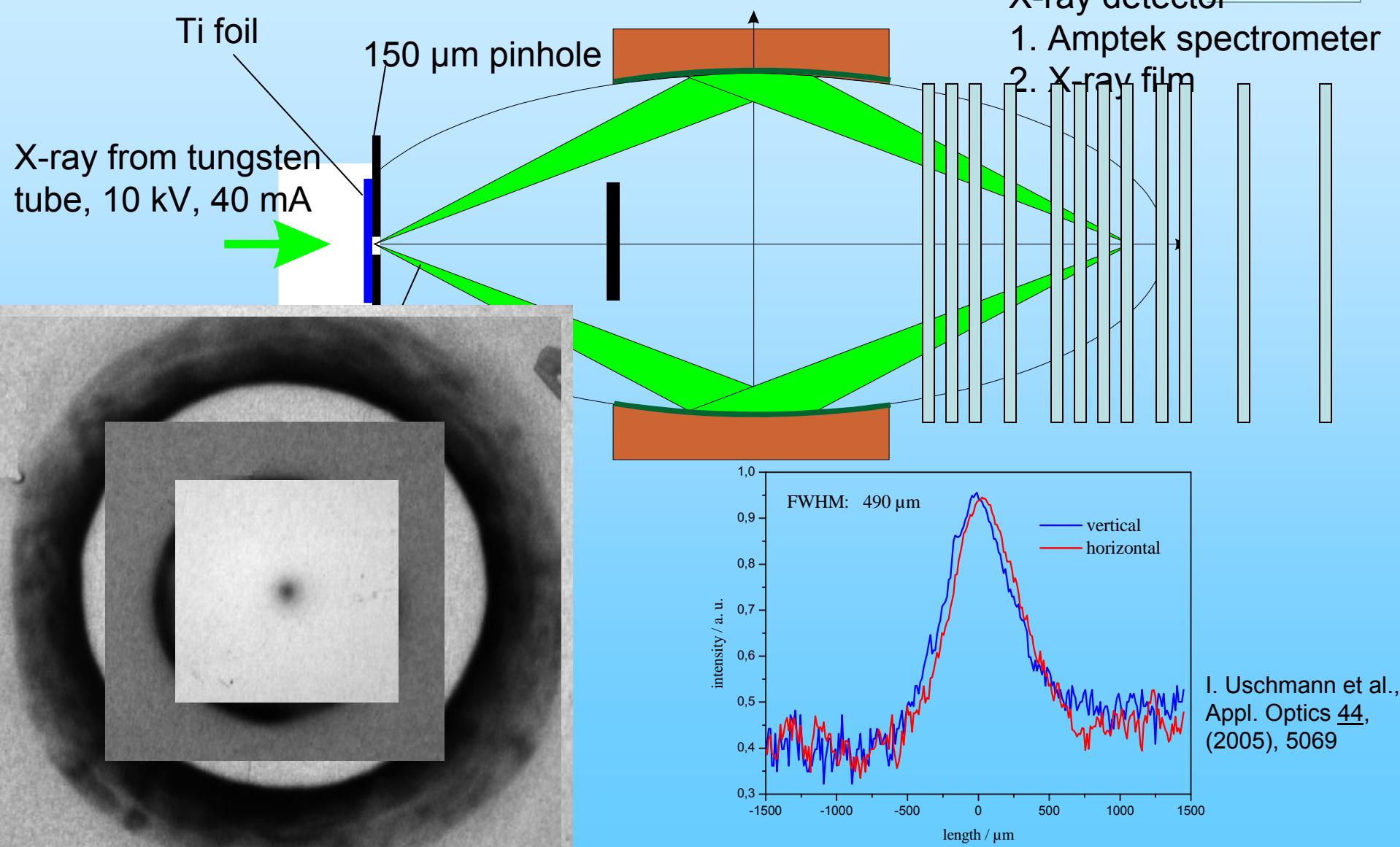
pink –second best value

M. Bargheer et al., Appl. Phys. B 80 (2005), 715

# Ellipsoidal HOP Graphite Crystal Reflection Curve



# Ellipsoidal HOP Graphite Crystal X-Ray Focus Test



# Summary of X-Ray Crystal Optics Parameters



- Energy range: 500 eV – 40 keV (reflection case)  
20 keV – 100 keV (transmission case)
- Spectral resolution:  $\Delta E / E = 1,000 – 10,000$
- Used solid angle:  $10^{-5}$  sr –  $10^{-3}$  sr
- Focal size: 1  $\mu\text{m}$  – 5  $\mu\text{m}$  @ large  $\theta$  angles,  
sub- $\mu\text{m}$  for a two-crystal device
- Focal distance: 5 cm – 5 m
- Cost: 10,000 \$ for one crystal
- Availability: firms of precision optics and crystal manufacturer,  
scientific institutes



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# Multilayer Laue Lens for Efficient Nanometer Focusing of Hard X-rays

G.B. Stephenson<sup>1,2</sup>, H.C. Kang<sup>2,4</sup>, H. Yan<sup>1,5</sup>,  
R.P. Winarski<sup>1</sup>, M.V. Holt<sup>1</sup>, J. Maser<sup>1,3</sup>, C. Liu<sup>3</sup>,  
R. Conley<sup>3,5</sup>, S. Vogt<sup>3</sup>, and A.T. Macrander<sup>3</sup>

<sup>1</sup>Center for Nanoscale Materials,

<sup>2</sup>Materials Science Division, and

<sup>3</sup>X-ray Science Division,

Argonne National Laboratory

<sup>4</sup>Advanced Photonics Research Institute,

Gwangju Institute of Science and Technology

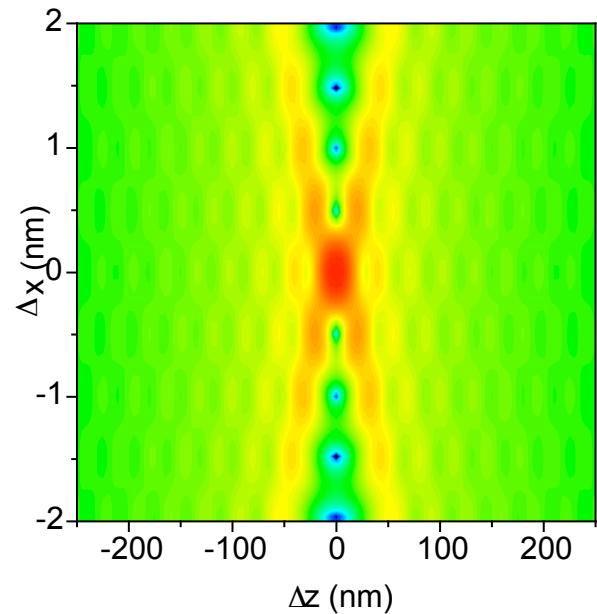
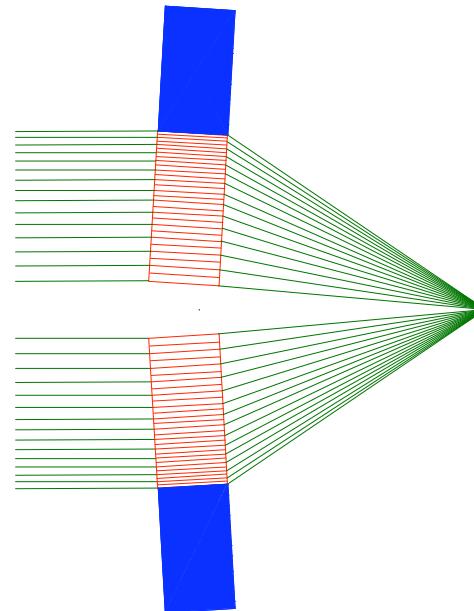
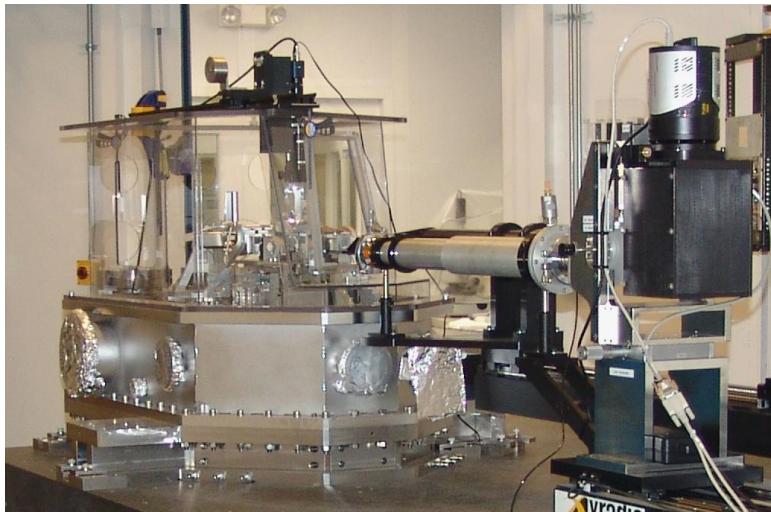
<sup>5</sup>National Synchrotron Light Source II,

Brookhaven National Laboratory

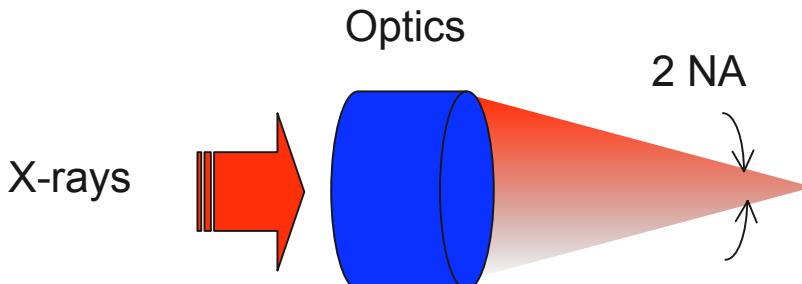
Workshop: Focus on X-ray Focusing, 2008 SPIE,  
San Diego, CA, August 13, 2008

# Outline

- Multilayer Laue Lens
  - Motivation and Approach
  - Status: 16 nm line focus, 31% efficiency, 19.5 keV
  - Future: Sub-nanometer focusing
- Overview of the Nanoprobe Beamline at Argonne



# **Ultimate Resolution of X-ray Focusing Optics**



$$\text{Rayleigh criterion : Best Possible Resolution} = \frac{\lambda}{2 \text{ NA}}$$

Can x-rays be efficiently focused to the atomic scale?

--> Need larger Numerical Aperture (NA)

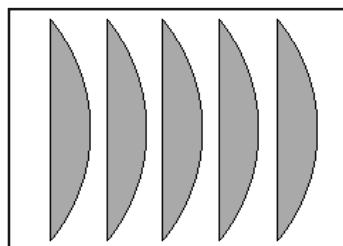
However, it is inherently difficult to produce large NA optics for hard x-rays

Currently,  $\text{NA} \sim 10^{-3}$ , resolution  $\sim 500 \lambda$

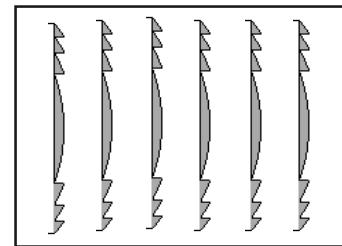
- What type of optics will work (e.g. reflective, refractive, diffractive)?
- What is the fundamental limit using real materials ?
- Can we fabricate optics that reach the fundamental limit ?

# High NA Hard X-ray Focusing Optics

## ■ Refractive: Lenses



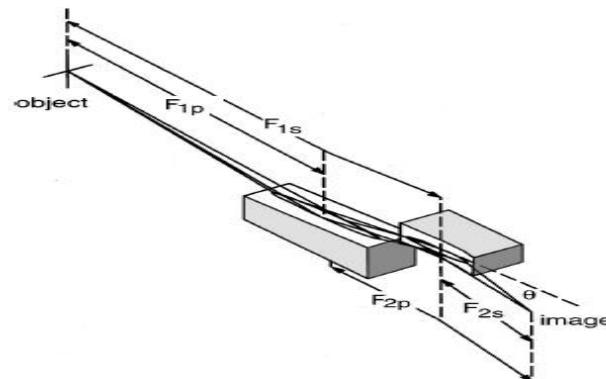
Compound refractive lens



Compound Fresnel lens for high NA

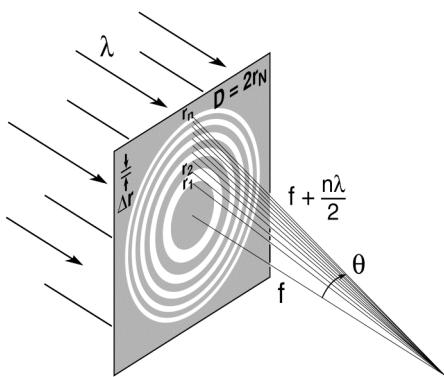
## ■ Reflective: Mirrors

Figure by differential deposition,  
multilayer coated for high NA

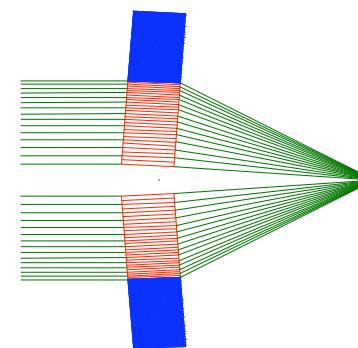


## ■ Diffractive: Zone Plates

High aspect ratio, tilted zones  
for high NA



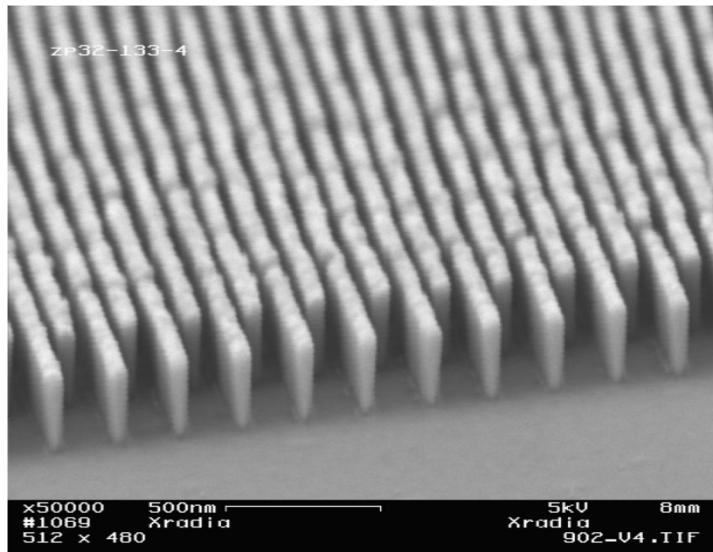
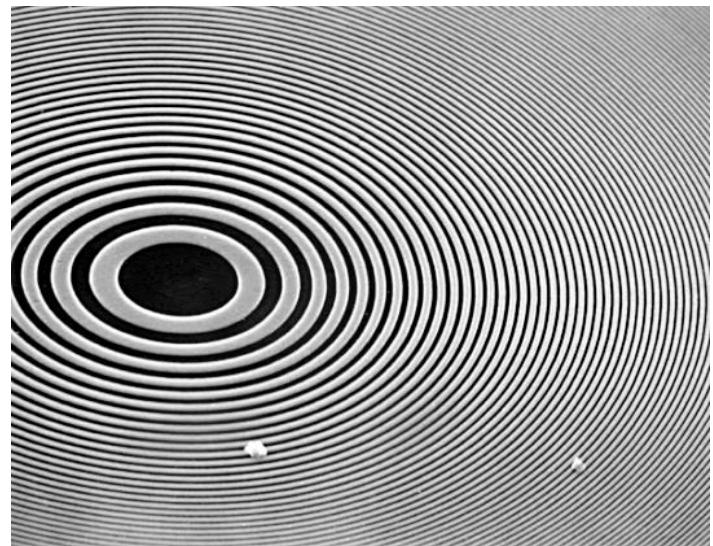
Lithographic zone plate



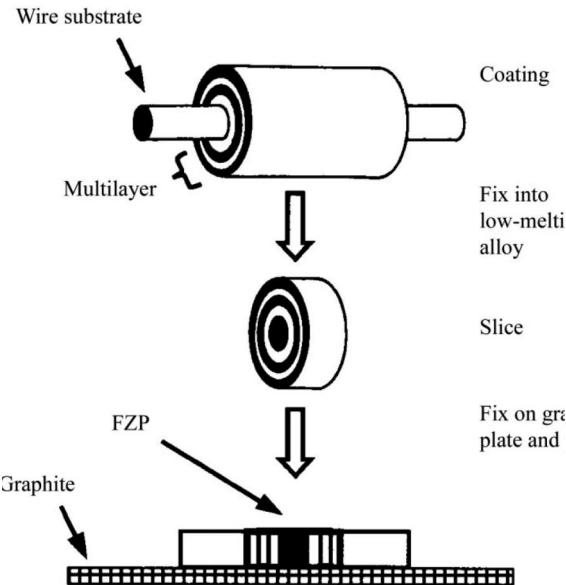
Transmission multilayer

# Diffractive X-ray Optics with High NA Require High Aspect Ratio Nano-structures

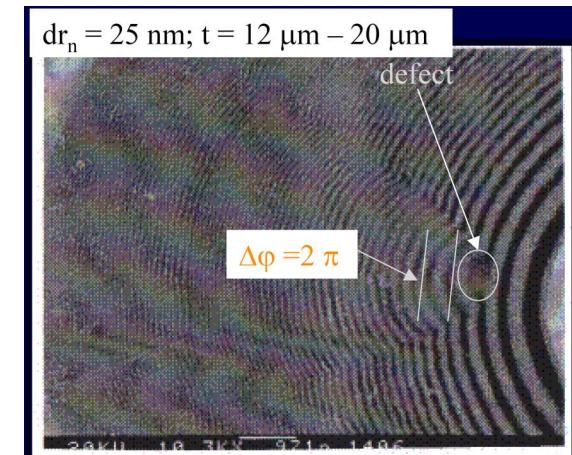
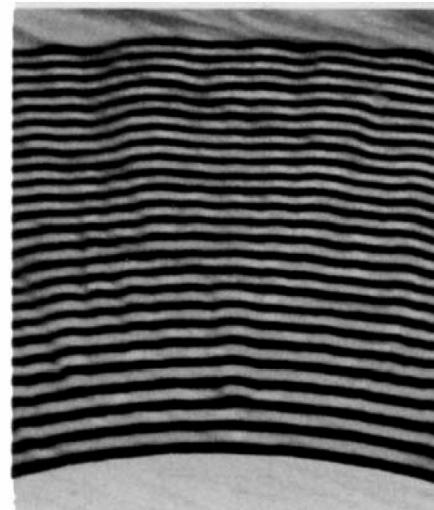
- Small focal spot sizes require small zone widths.
- Zone plate structures for hard x-rays must be several microns thick to achieve high efficiency, which implies **high aspect ratios (>>100)**.
- It is difficult to produce such high aspect ratio structures using lithography.
- **Sectioning of multilayers allows very high aspect ratios to be produced.**



# Sputtered-Sliced Fresnel Zone Plate



*S. Tamura et al. (2002) & B. Kaulich et al. (1996)*



- Deposition of zone plate structure on circular wire
- Imperfections of wire are amplified
- Later coating of the outermost zones gives worse layer position accuracy in most sensitive region
- Circular geometry gives 2-D focus in one optic, but can't tilt layers to get high efficiency

- Cu-Al materials are relatively difficult to section without damage
- Focal spot size  $\sim 200 \text{ nm}$

# Multilayer Laue Lens

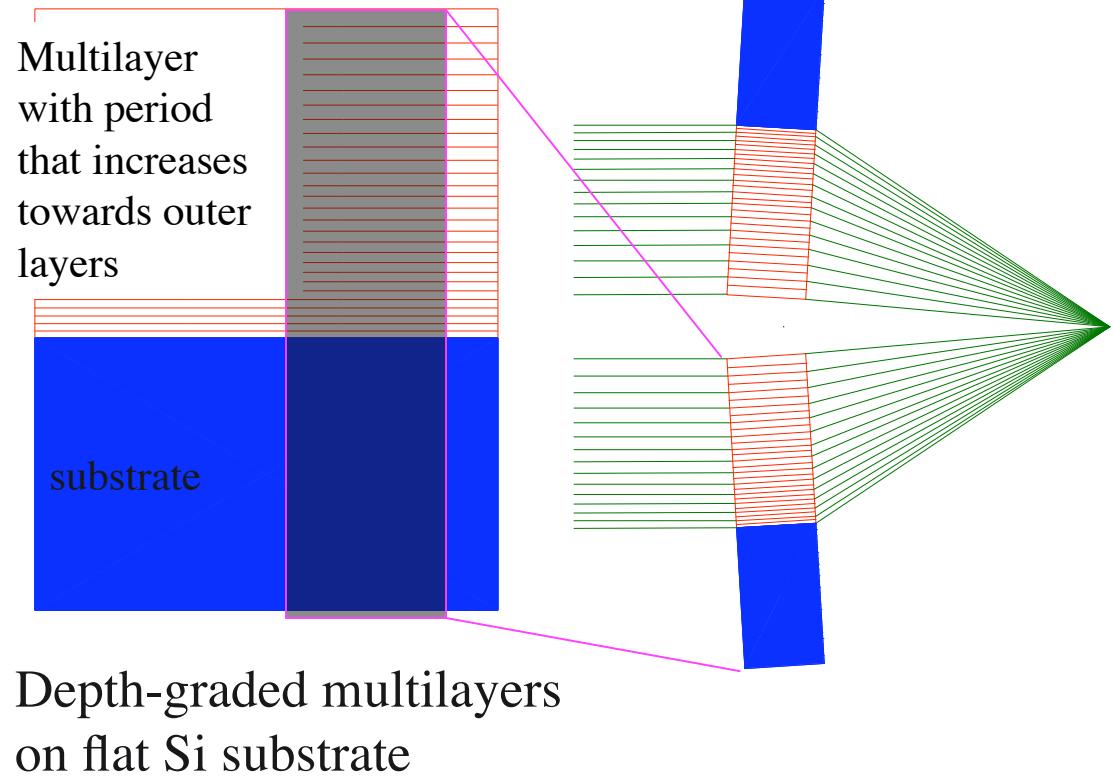
Deposit multilayer on flat substrate to produce one-dimensional focusing optic

(1) Deposit multilayer with depth-graded spacing to form zones of linear zone plate  
**(thinnest structures first)**

(2) Make cross-sections to allow use in Laue geometry  
**(high aspect ratio structure)**

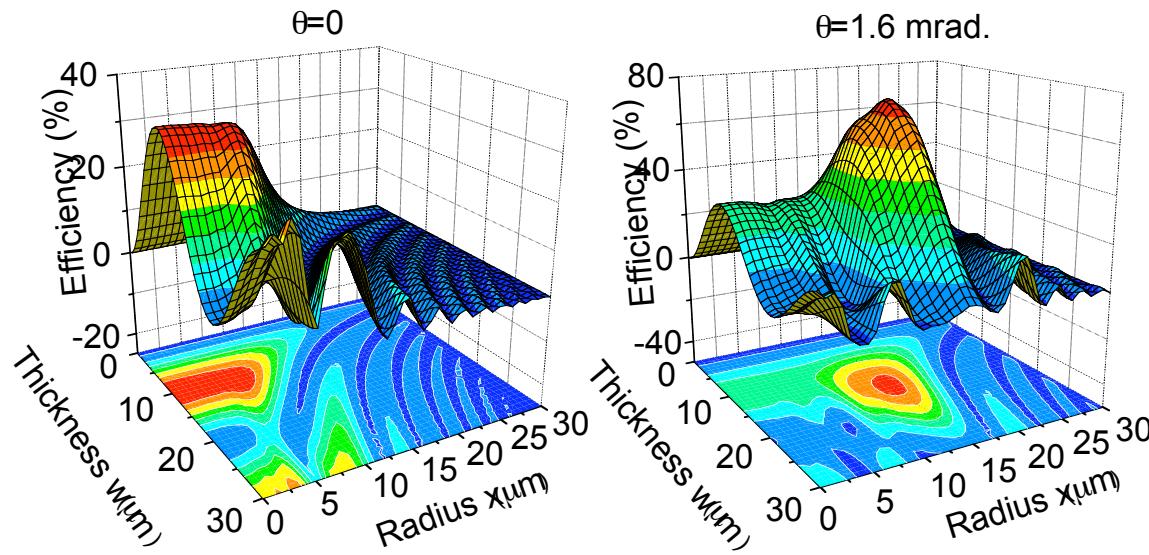
(3) Assemble sections: two opposite to collect full NA  
**(tilt to achieve high efficiency);**  
a second pair at right angles to form point focus  
**(high efficiency allows two optics in series)**

Multilayer Laue Lens

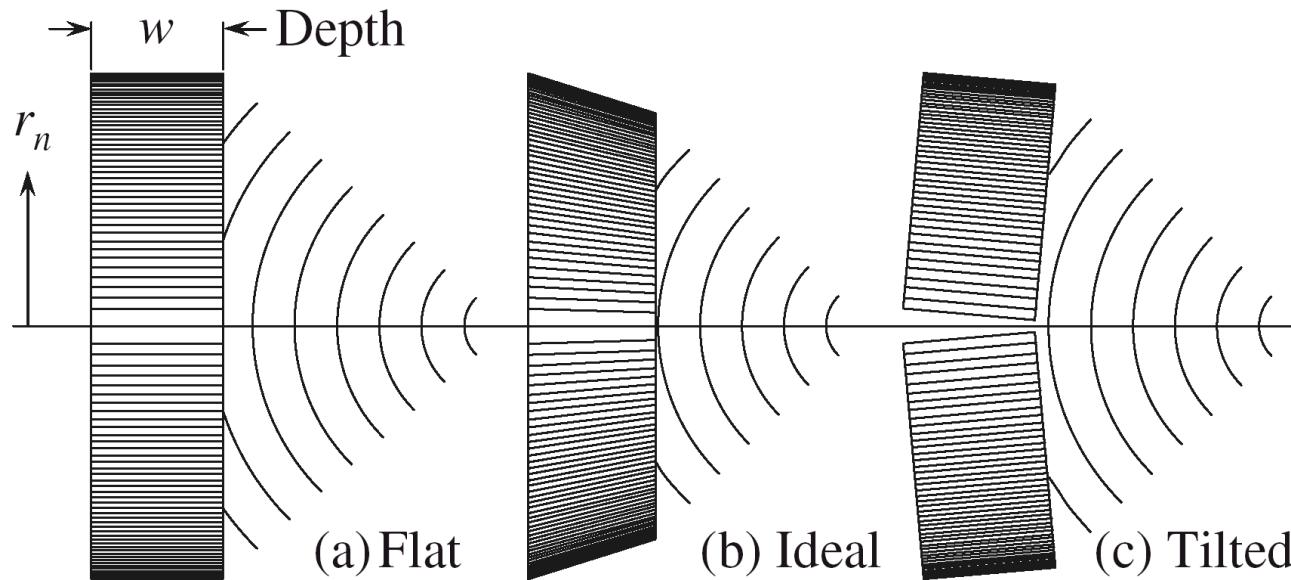


## Theory for MLL

- MLL's operate in a different optical regime than standard zone plates
- Dynamical diffraction effects inside the volume of the structure are dominant
- Theory for focusing performance:
  - J. Maser et al. - Coupled wave theory (*Optics Commun.* **89**, 355 (1992); *Phys. Rev. Lett.* **96**, 127401 (2006))
  - C. Shroer - Parabolic wave equation (*Phys. Rev. B* **74**, 033405 (2006))
  - H. Yan et al. - Takagi-Taupin (*Phys. Rev. B* **76**, 115438 (2007))

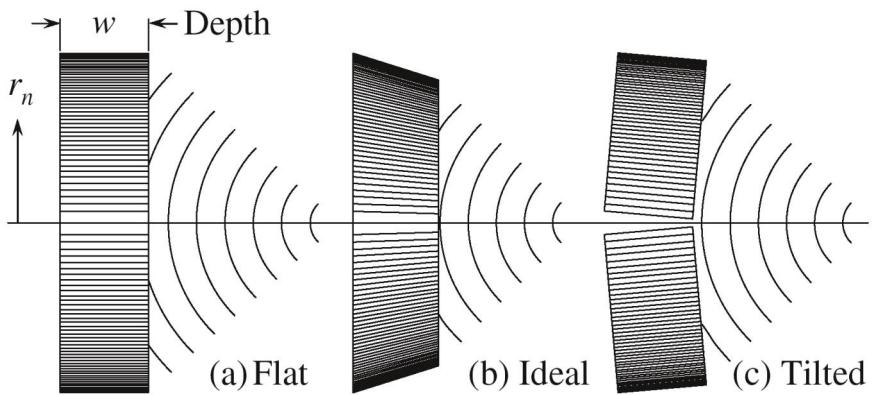


## Optimum Zone Geometry



- Flat geometry with all layers parallel is standard for lithographic zone plates
- Ideal “wedged” geometry where each layer makes the Bragg angle for its spacing becomes favorable for high NA focusing
- Ideal geometry can be approximated by tilting each half of MLL

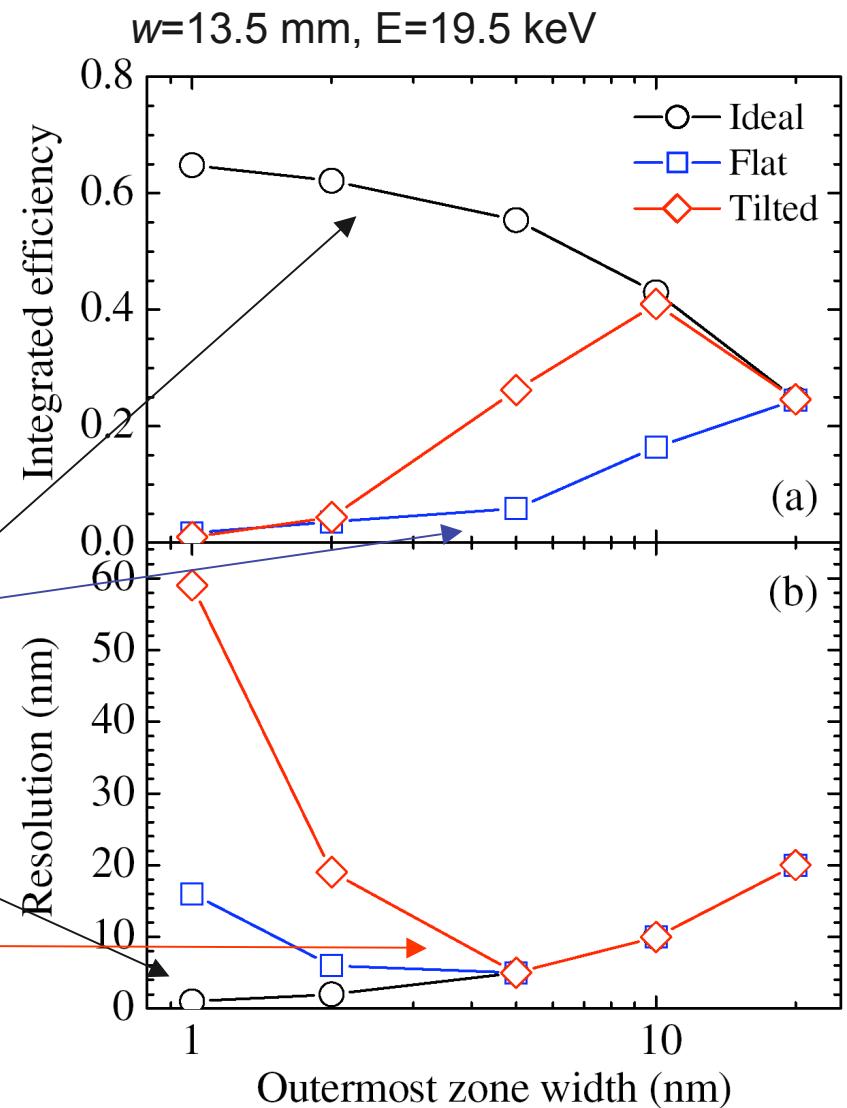
# Where is the Spatial Resolution Limit?



- Flat structure: loses efficiency below 10 nm
- Ideal “wedged” structure:
  - High diffraction efficiency
  - Resolution below 1 nm feasible
- Tilted MLL structure:
  - 6 nm resolution feasible

H. C. Kang et al.

Physical Review Letters **96**, 127401 (2006)



## Multilayer Structure for MLL

WSi<sub>2</sub>/Si, 1588 layers, t<sub>dep</sub> = 13.25 μm

Δr<sub>max</sub> = 25 nm

Δr<sub>min</sub> = 5 nm



H. C. Kang et al., *Applied Physics Letters* **92**, 221114 (2008)

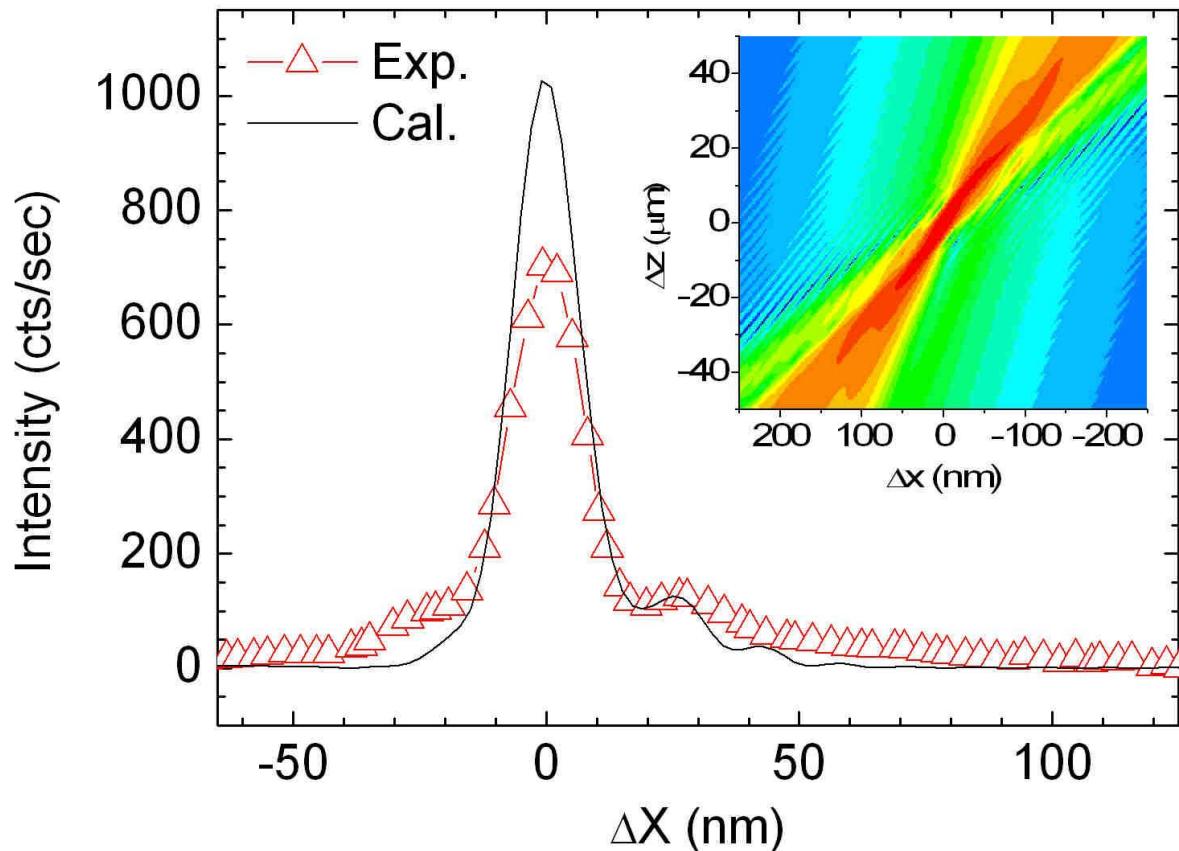
## Measured and Calculated Performance

FWHM = 16 nm

Efficiency = 31% at 19.5 keV

Measurement of half-MLL structure agrees well with calculation

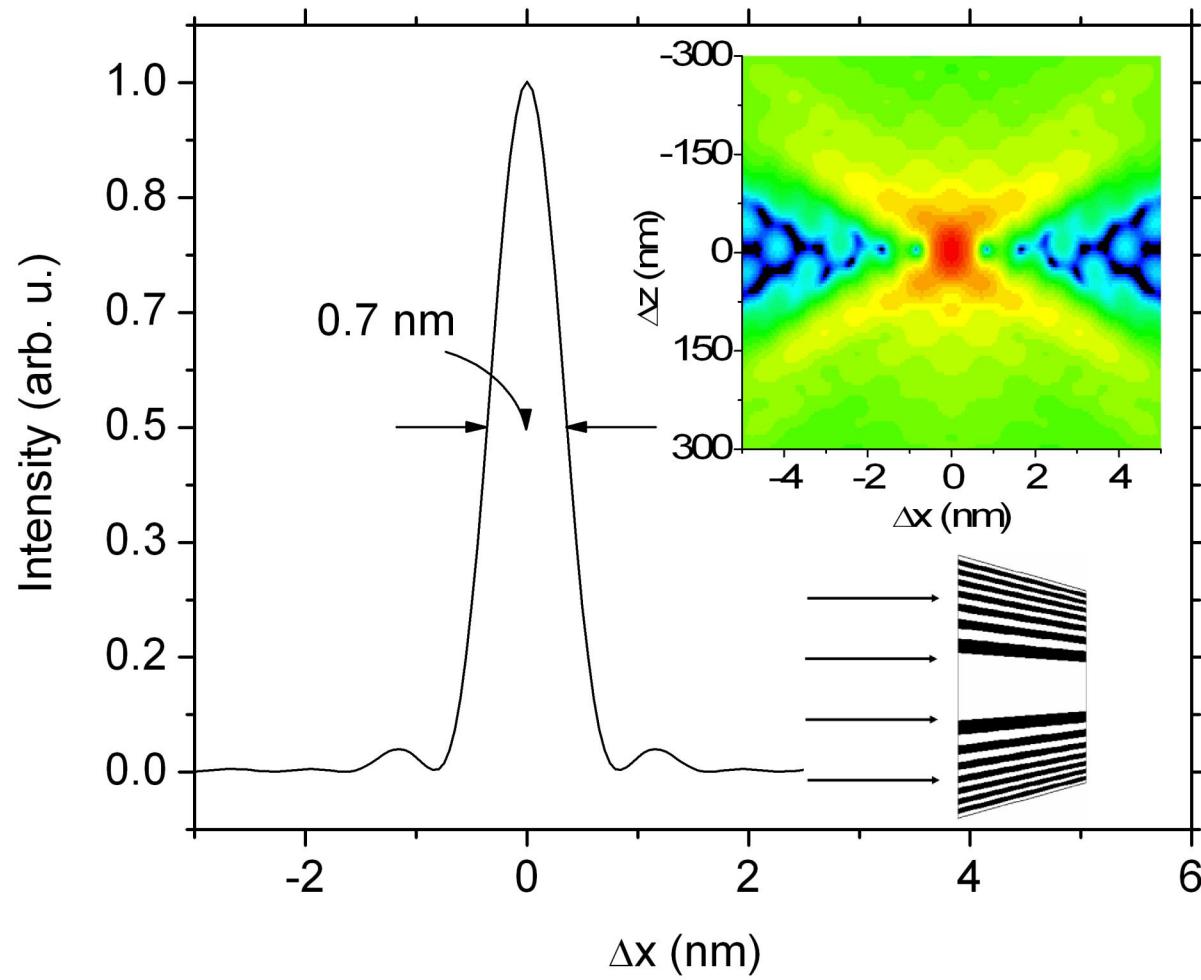
Assembly of complete MLL of this structure should give focus of 6 nm, which will be the smallest focus of photons yet achieved



H. C. Kang et al., *Applied Physics Letters* **92**, 221114 (2008)

## Near-Atomic-Scale Focusing Possible with “Wedged” MLL

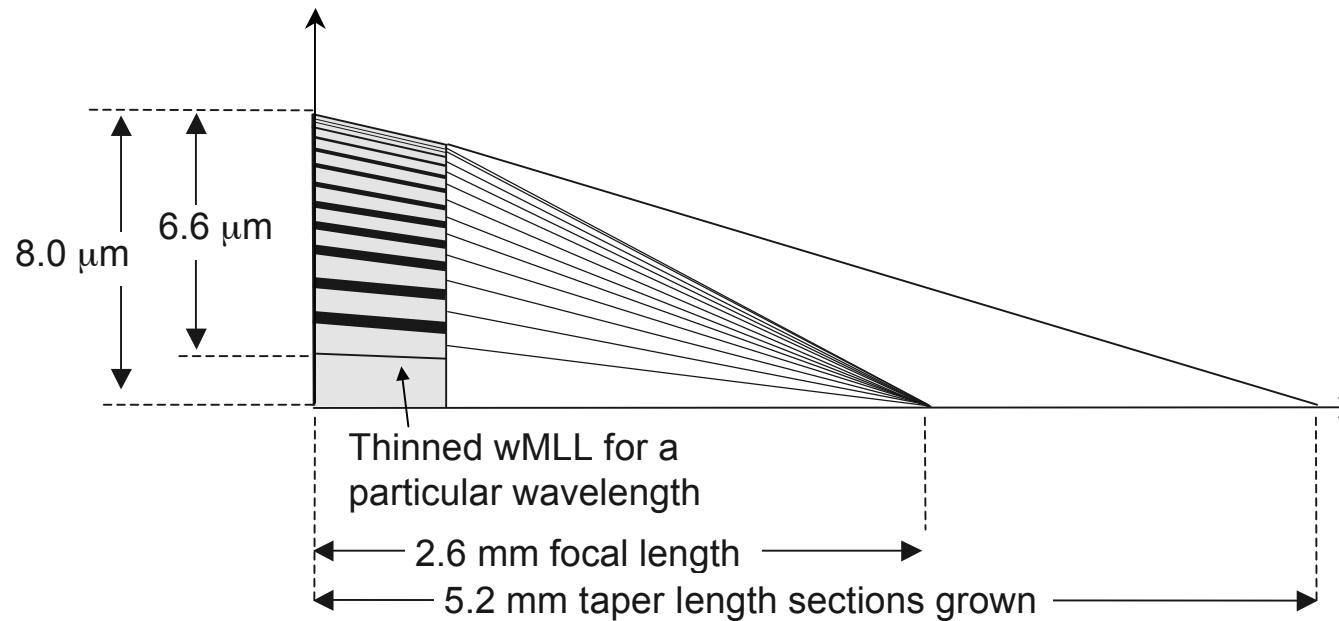
Calculations show that focusing to below 1 nm is possible using “wedged” layers



H. Yan et al., *Physical Review B* **76**, 115438 (2007)

## *Progress of Deposition of Wedged Multilayer Structures*

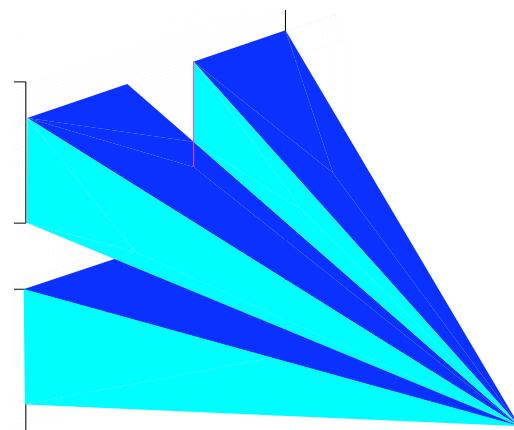
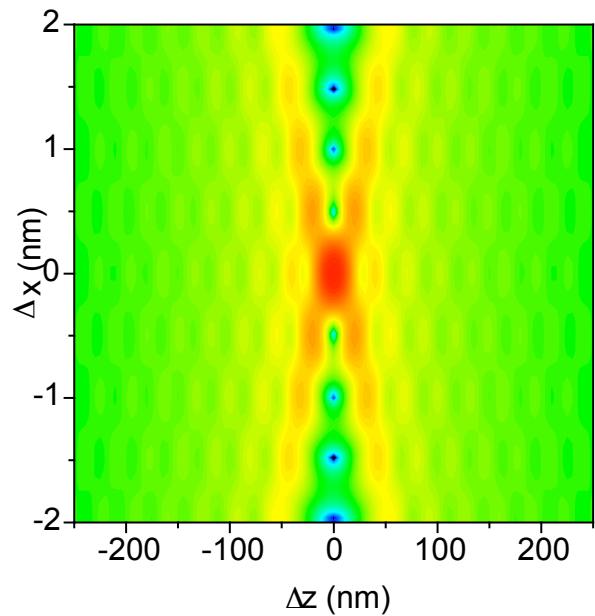
- We have succeeded in depositing initial multilayer structures for a “wedged” MLL
- Examples:
  - 40% structure, outermost zone width 2.5 nm, 1588 layers, 6.6  $\mu\text{m}$  tot.
  - Full structure, outermost zone width 3 nm, 6543 layers, 40  $\mu\text{m}$  total
- Characterization is underway



R. Conley et al., *Review of Scientific Instruments* 79, 053104 (2008)

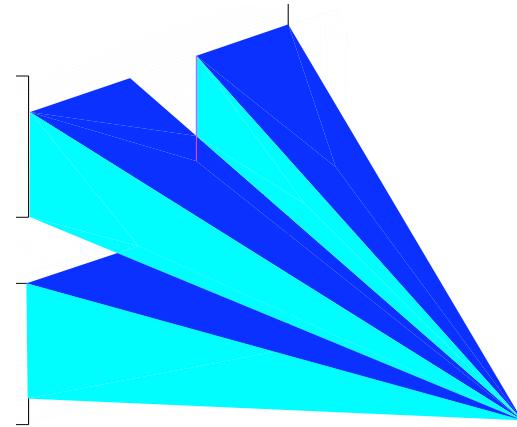
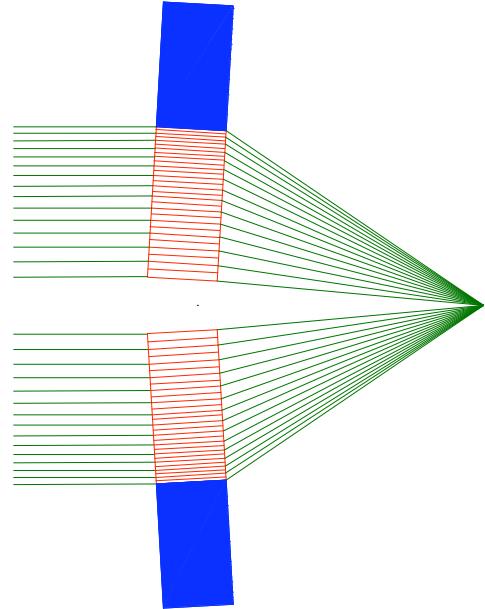
# Future Directions for MLL

- Theory
  - Determine optimum structure and performance as  $f(\lambda)$
  - Determine fabrication accuracy required
- Experiment
  - Cross two linear optics to make point focus
  - Assemble complete “tilted” structure to achieve 6 nm focus
  - Develop techniques to deposit “wedged” layers to achieve near-atomic-scale focusing



## *Summary of Multilayer Laue Lens Properties*

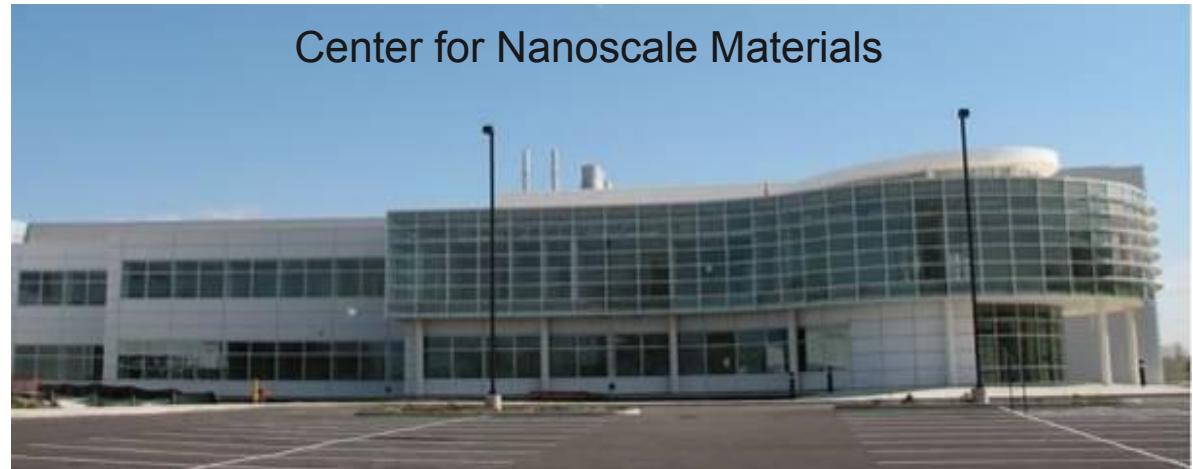
- Energy range: 5 - 100 keV
- Gain: ~1000X or more in each dimension
- Focal size: 20 nm or less
- Focal distance: 2 mm or less
- Cost, availability:
  - Currently a research effort at ANL, NSLS II, GIST
  - Potentially available in a few years
  - Potentially less than \$10K per optic



# Nanoprobe Beamline at the Center for Nanoscale Materials

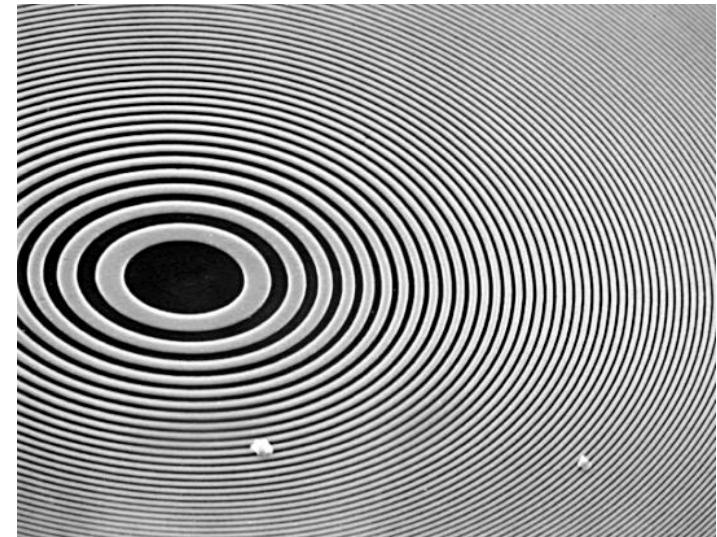
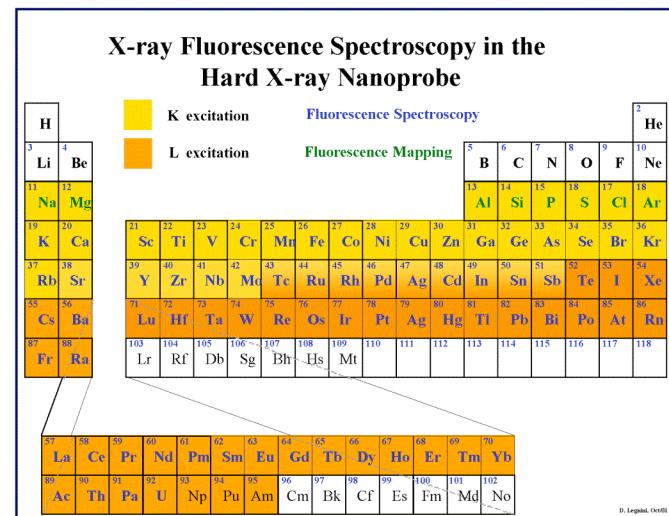
- Center for Nanoscale Materials
  - new nanoscience research center located adjacent to APS
- Nanoprobe Beamline
  - state-of-the-art hard x-ray microscopy beamline, built and operated in partnership between CNM and APS

Advanced Photon Source, ANL



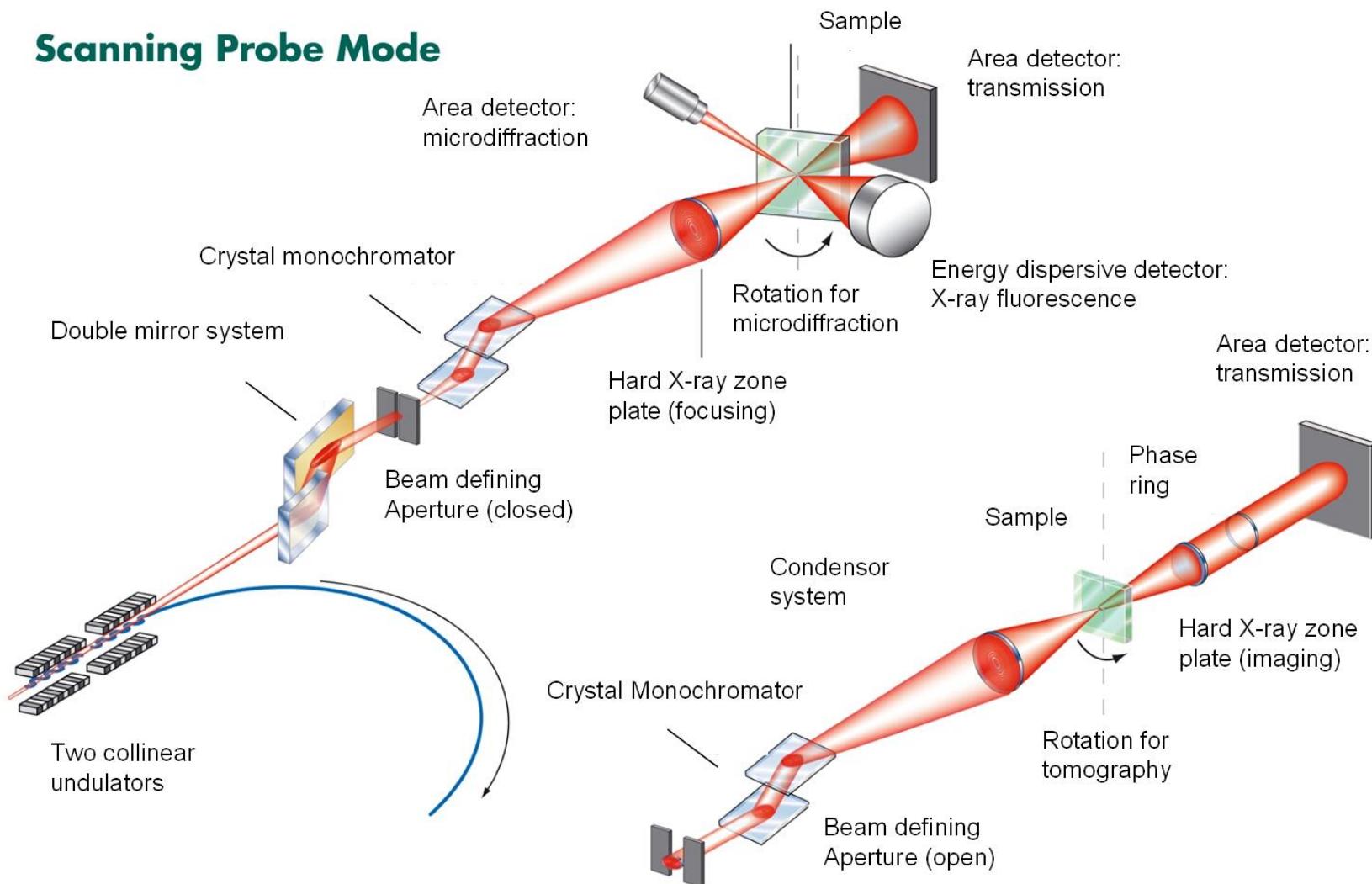
# Nanoprobe Beamline: Overall Specifications

- Hard X-ray microscopy at the highest achievable spatial resolution
  - Initial spatial resolution of 30 nm using lithographic zone plates
  - Energy range 3 - 30keV (nano-spectroscopy excitation of most elements)
  - Large penetration → sample environments/fields
  
- Planned capabilities
  - **Fluorescence:** atto-g elemental sensitivity, chemical state sensitivity
  - **Diffraction:** sensitivity to crystallographic phase, strain, orientation
  - **Tomography:** transmission absorption / phase contrast imaging
  - **Coherent x-rays:** disorder, imaging
  - **Magnetic contrast** using polarized x-rays
  - **Dynamic studies** at 100 ps time resolution



# Nanoprobe Beamline Schematic

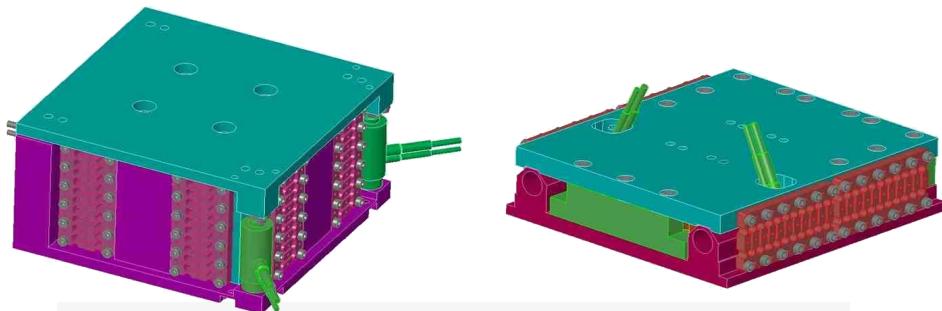
## Scanning Probe Mode



## Full-Field Transmission Mode

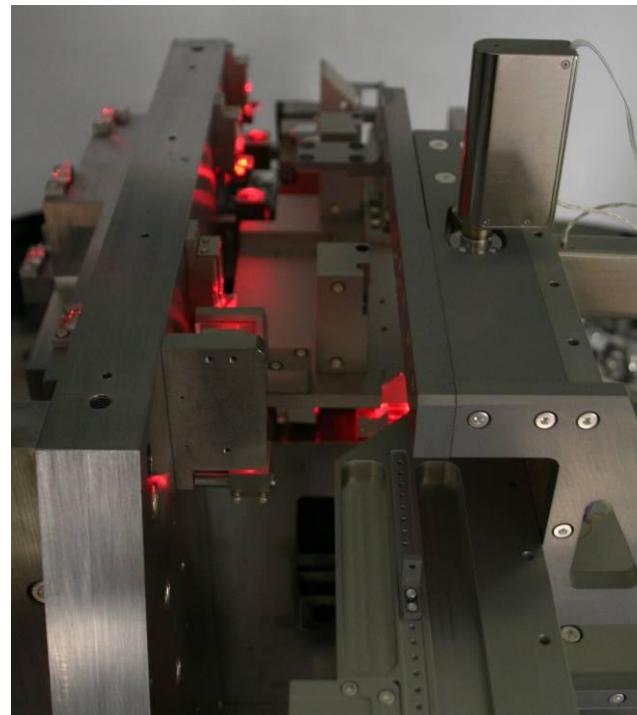
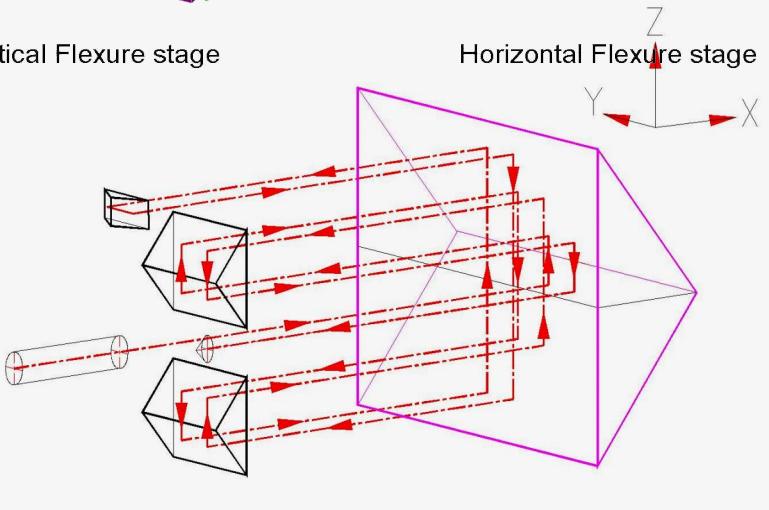
# Nanoprobe Scanning Design

- Laser interferometers monitor positions of optics and sample to Angstrom precision
- Nanoscale scanning of focusing optic using piezo stages
- Feedback used to lock beam to desired position on sample at each point in scan



Vertical Flexure stage

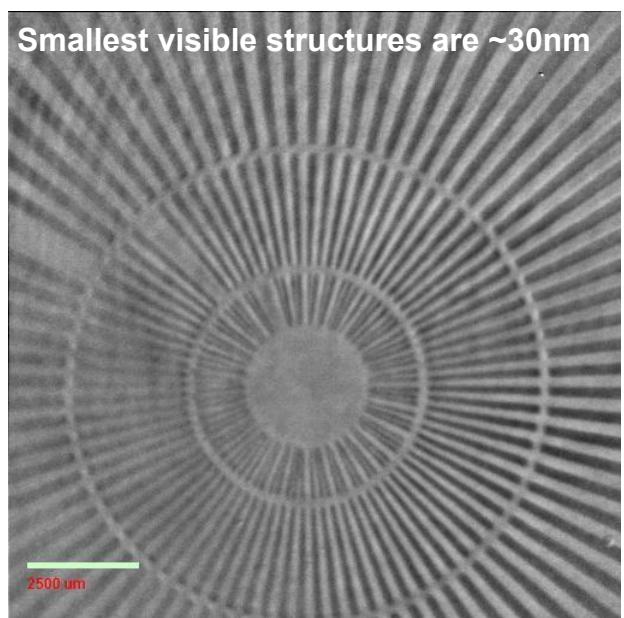
Horizontal Flexure stage



# Nanoprobe Beamline Construction Complete

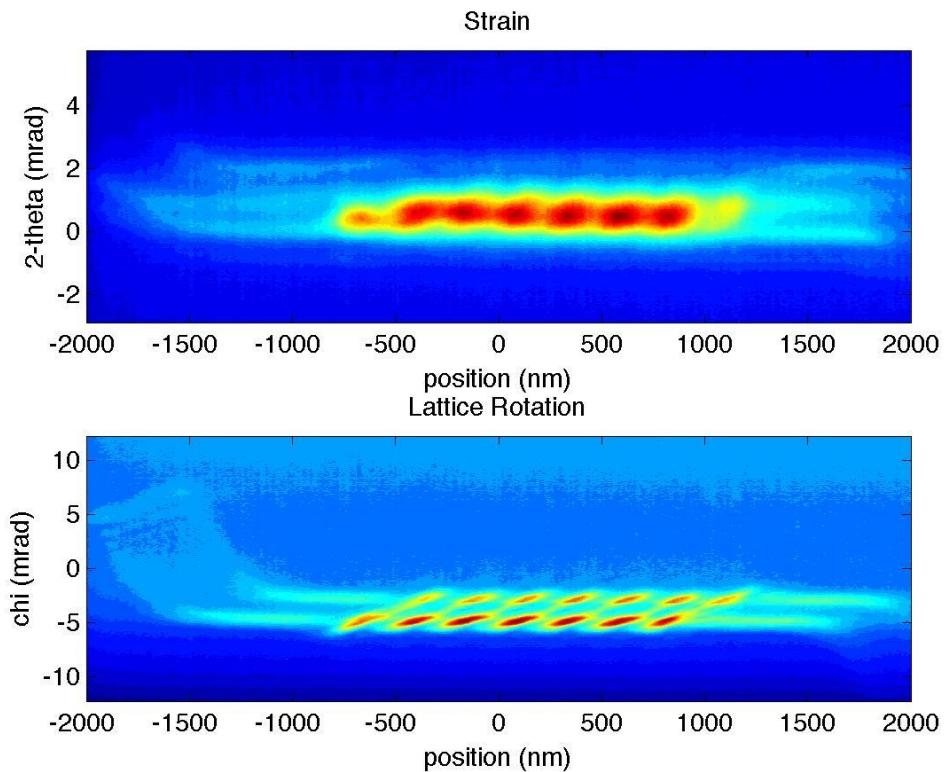


Smallest visible structures are ~30nm

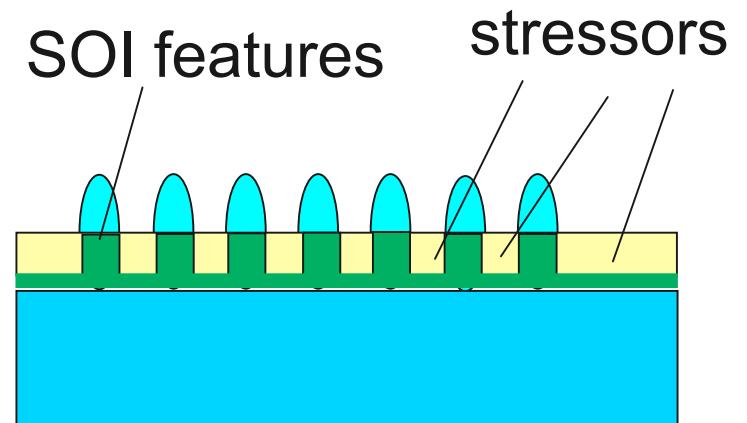


- Zone plate performance at 30 nm verified
- Beamline commissioning underway
- First user program experiments started this year

## *Recent Example: Nanodiffraction from Strained Silicon*



~50 nm resolution  
scanning diffraction  
maps of device features  
of strained silicon on  
insulator (SOI)



Courtesy: Conal Murray\*, Sean Polvino†, Andrew Ying†, Ozgur Kalenci†, I.C. Noyan†

\* IBM, †Columbia University

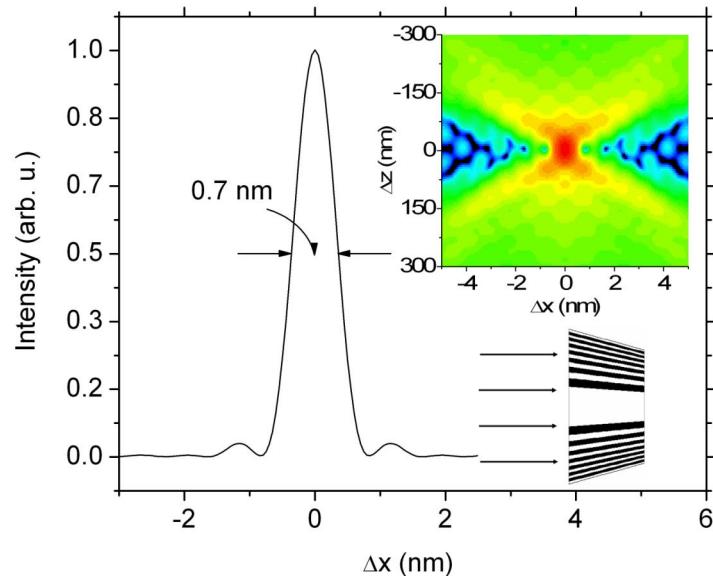
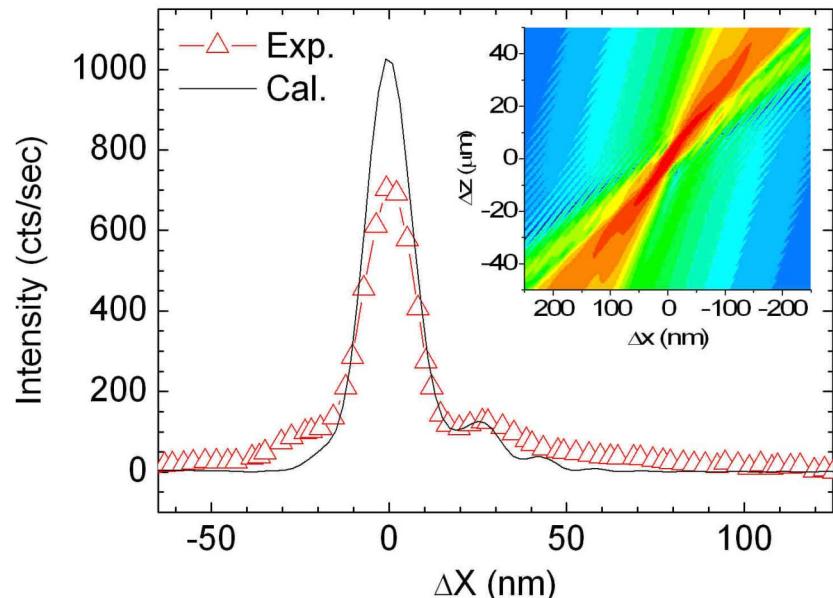
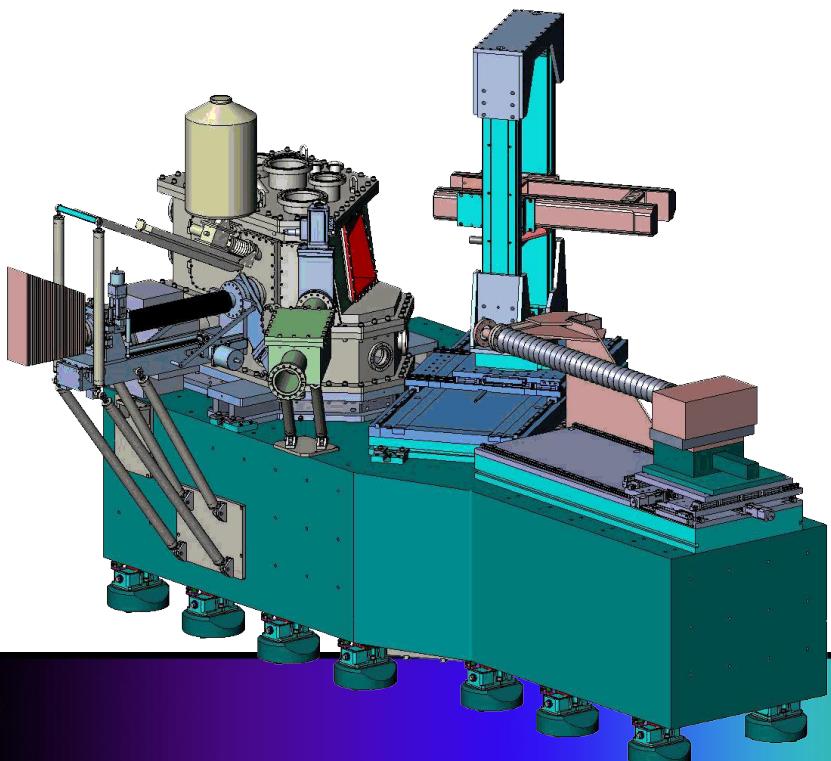
# Summary

## ■ MLL

- Achieved 16 nm FWHM line focus,  
31% efficiency at 19.5 keV
- Sub-nanometer focusing predicted

## ■ Nanoprobe

- Currently: 30 nm resolution zone plates
- Plan: 10 nm resolution MLL



# Diffractive Focusing By Zone Plates



*3D X-ray Imaging for Science and Industry*

Dr. Michael Feser  
Vice President / General Manager  
nano-Imaging  
Xradia Inc.

SPIE X-ray  
Focusing Workshop



# High-resolution Optics: Comparison

	KB Mirror	Refractive Lens	Zone Plates (+Laue optics)
Demonstrated Resolution (nm)	<30	<50	<15 for 0.5 keV 22 for 8 keV
Flux Density Gain	>500,000	10000	>500,000
Imaging Optic	No	Yes	Yes
Chromatic Aberration	No	$1/\lambda^2$	$1/\lambda$
Theoretical resolution limit (nm)	<10	~2 ? (Schroer et al.)	~1 <sup>(1)</sup> ?
Minimum focal length for 100 μm aperture (mm)	~30	100 for 10 keV	0.5 for 0.5 keV 20 for 10 keV

<sup>(1)</sup> Kang et al., PRL96(2006)

# Diffractive Focusing By Zone Plates

## Outline



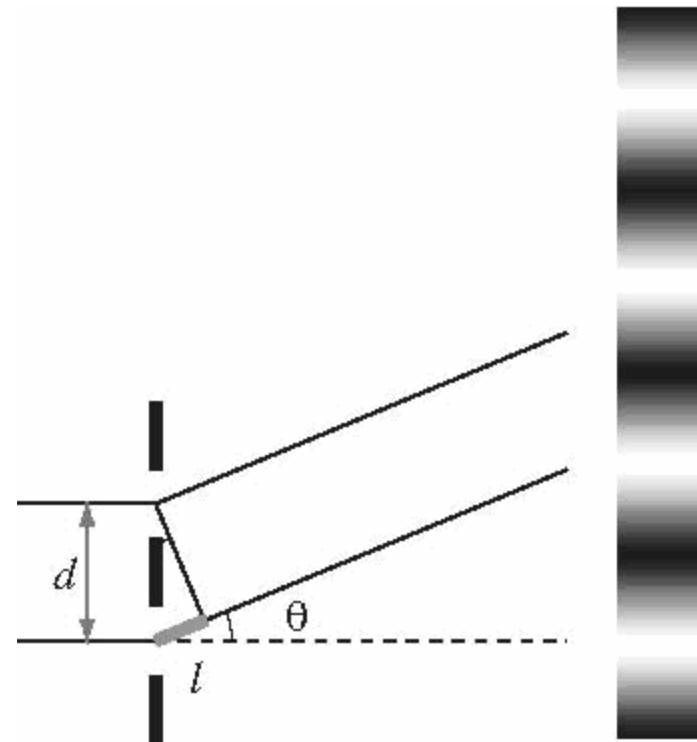
- History and working principle
- Fabrication, limitations and future developments
- Applications
  - X-ray imaging / microscopy
  - X-ray nano-probing: Diffraction, spectroscopy
- Summary and outlook

# Diffraction From a Grating

- Recall diffraction from slits separated by  $d$
- diffraction *maxima* for positive interference of light waves occurs when  

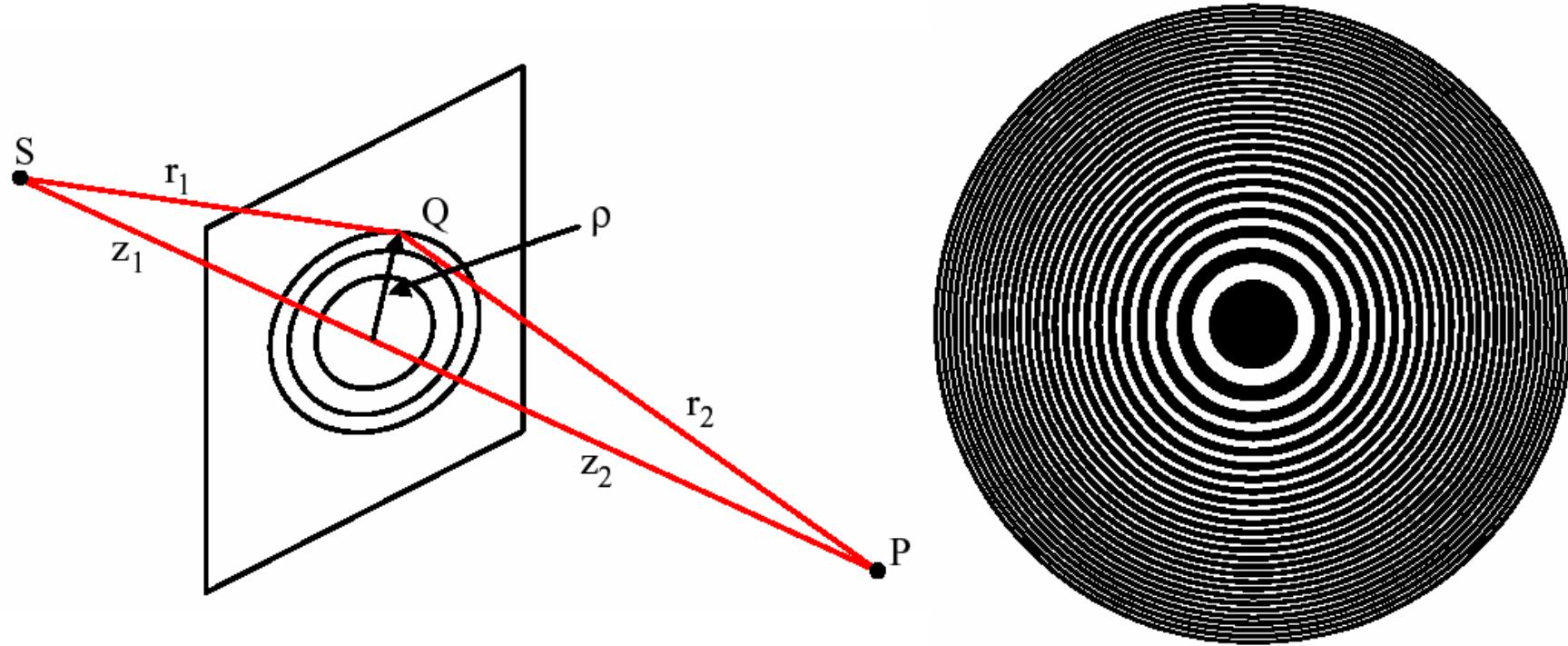
$$d \sin \theta = n\lambda$$

$n$  = diffraction order  
 $\theta$  = diffraction angle
- Constant grating pitch acts like a prism for one diffraction order (deflects light)
- Deflection is a linear function of wavelength  $\lambda$



# Diffraction from Circular Grating

- By varying the grating pitch radially in a circular grating, positive interference on-axis at a focal point is obtained



- Excellent Reference: M. Young, JOSA 62(8), pp. 972-976



# Diffractive Lenses: Fresnel Zone Plates

- ❑ Focal length has a strong wavelength dependence:

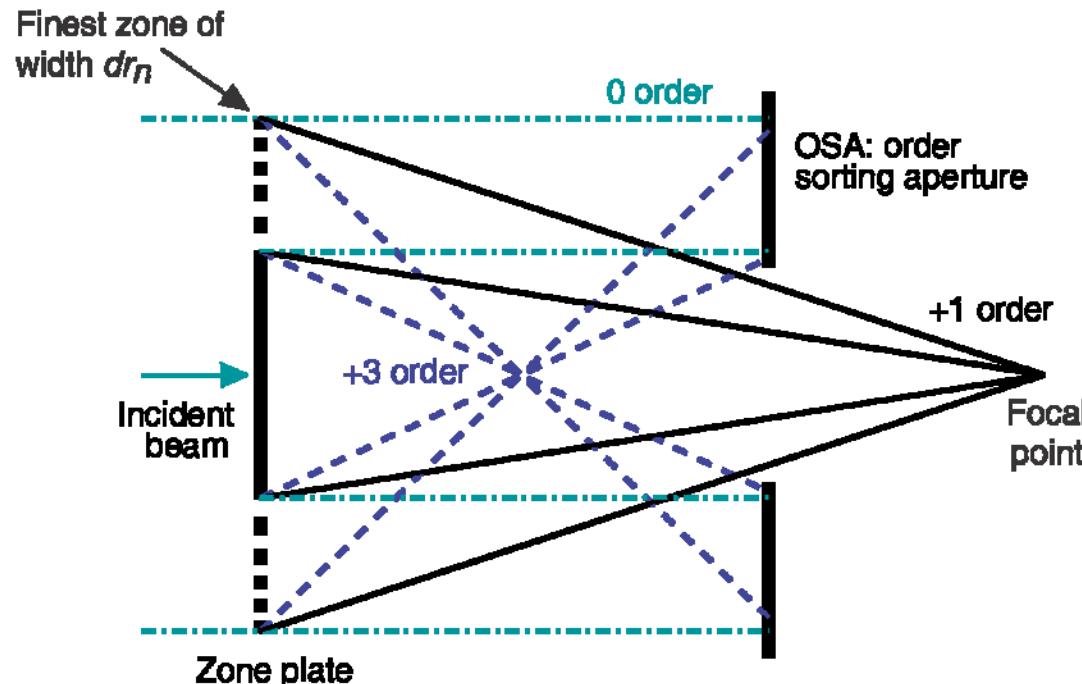
$$f = \frac{OD \Delta R_N}{\lambda}$$

- ❑ Necessitates use of monochromatic beam, with bandwidth  $E/\Delta E >$  number of zones
- ❑ Resolution limited by outermost zone width  $\Delta R$ :

$$\text{Res} = 1.22 \Delta R$$

# Diffraction Orders of Zone Plates

- Diffractive elements have more than one diffraction order
- Directly transmitted beam: 0<sup>th</sup> order  
Higher diffraction orders with decreasing intensity  
(even orders forbidden for 1:1 mark to space ratio)
- With use of apertures and stops one diffraction order can be isolated and ZP acts like a thin lens (disadvantage of zone plates)



Central stop and order sorting aperture (OSA) to isolate first order focus in a nano-probing application



# Zone Plates as Thin Lenses

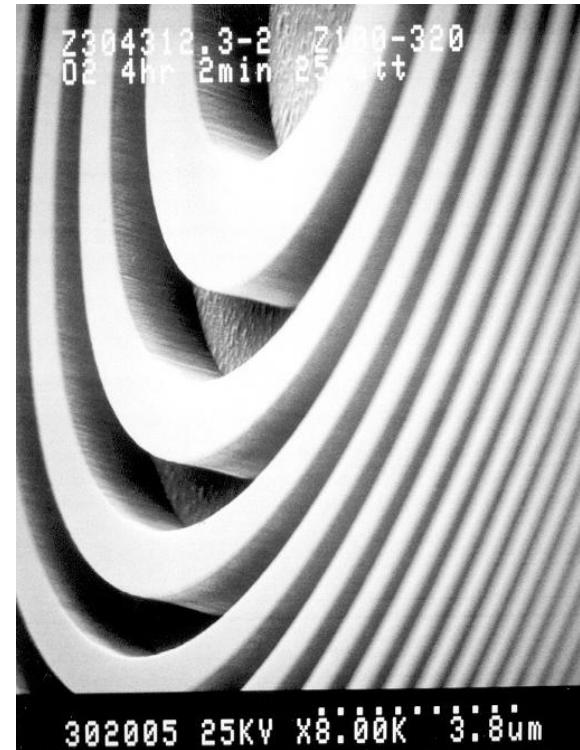
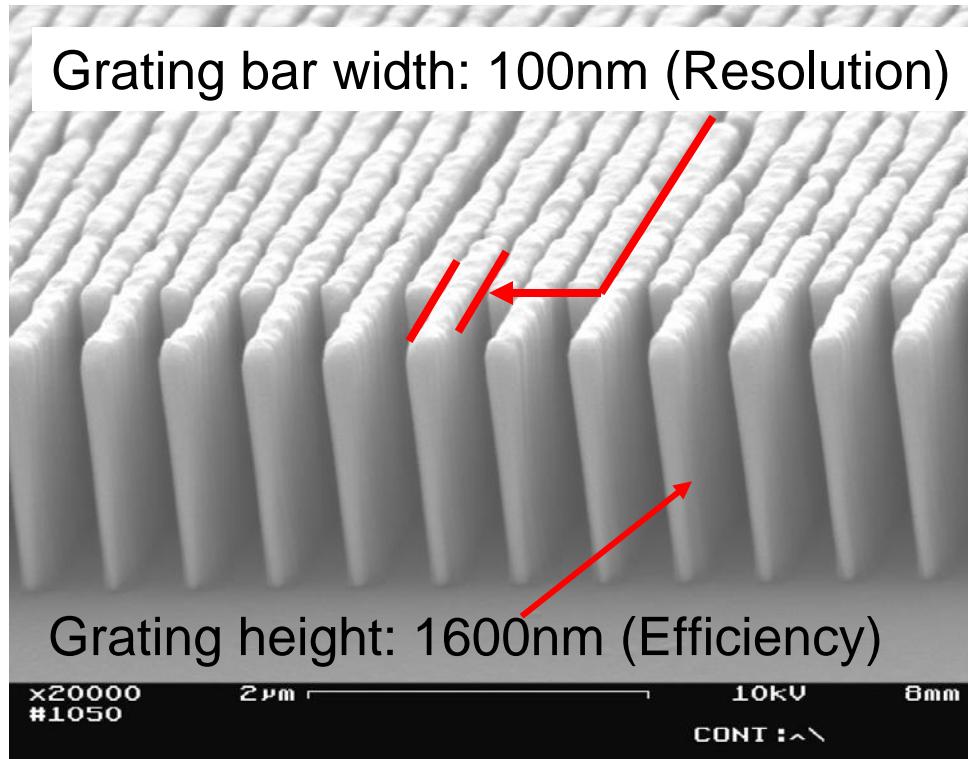
□ Works just like a thin lens, except:

- 1st order efficiency
  - Opaque zones ~10%
  - Phase reversing zones ~40%
  - Blazed zones 100%
  - (less for real materials)
- Need to deal with unwanted orders
- Highly chromatic :  $f \sim 1/\lambda$
- No spherical aberrations



# Zone Plate Efficiency for Real Materials

# Scanning Electron Micrographs of Zone Plates



- Resolution limited to approximately the zone width  $\Delta R$
- Focusing efficiencies up to 30% for high x-ray energies



# Zone Plates: Early History

- Rayleigh 1871 – unpublished
- Soret 1875 – first publication
- Rayleigh 1888 – phase zone plates
- Wood 1898 – experiments with zone plates using light
  
- Some simple cameras use zone plates instead of pinholes!

# First Images With a Fresnel Zone Plate

□ R. W. Wood (1898): zone plate figure drawn with a pen and a compass!  
Photographically reduced



PLATE 2. ZONE-PLATE, FROM A DRAWING.

# X-ray zone plate history

- Albert Baez (UNESCO, SAO/Cambridge)
  - “The possibility constructing a single Fresnel zone plate for x-rays should be explored” - J. Opt. Soc. Am. 42, 756 (1952) - paper on x-ray holography.
  - Demonstrated free-standing metal zone plate for X rays: “auguring well for resolution at 100 Å” - Nature 186, 958 (1960).
- Gunter Schmahl and Dietbert Rudolph (Göttingen)
  - Proposed holographic fabrication method - Optik 29, 577 (1969)
  - First TXM demonstration using synchrotron radiation - Niemann et al., Opt. Comm. 12, 160 (1974)
- Janos Kirz (Stony Brook)
  - Phase enhancement of efficiency - J. Opt. Soc. Am. 64, 301 (1974)
  - First STXM demonstration using synchrotron radiation - Rarback et al., 1983 XRM conference proceedings; Kenney et al., J. Microscopy 138, 321 (1985). Zone plates: D. Kern et al., IBM.
- E-beam zone plates:
  - Proposed by D. Sayre, IBM tech report RC 3974 (1972).
  - First demonstrated by Nat Ceglio, MIT, in E. Ash, Scanned Image Microscopy (Academic Press, 1980); J. Vac. Sci. Tech. B 1, 1285 (1983)



# Zone Plate Patterning Techniques

## □ E-beam writing

(Xradia, CXRO, Agere/SB, Göttingen, Trieste, Kings, etc)

- current method of choice for high resolution patterning
- Direct write into resist, very high resolution (<15nm demonstrated)

## □ Optical, Holographic Patterning (Göttingen)

- First high resolution zone plates for x-ray imaging at synchrotron
- Limited by diffraction of light used (wavelength)
- New efforts with EUV radiation at synchrotrons

## □ Sputtered, sliced (Göttingen, Japan)

- Engineering challenges have proven hard to overcome

## □ Imprint litho (U. Texas/SB)

- Master for imprint has to be fabricated using E-beam techniques
- Imprint mainly motivated by mass-production aspect



# Zone Plates By Electron Beam Lithography

- Produces the finest possible arbitrary 2-D structure (other than what nature can be persuaded to make by itself)
- Top end machines (such as JEOL JBX-9300FS, Vistec VB300) offer ~2 nm spot size at ~1 nA and 100 kV, 500 µm field, ~1 nm positioning with 5-10 nm absolute placement on a rectangular grid. DoE nanocenters have such systems

A. Stein at the NJNC JBX-9300FS



# Zone plate efficiency and thickness

- For binary zones, 1:1 mark:space ratio.
- See Kirz, *J. Opt. Soc. Am.* **64**, 301 (1974)

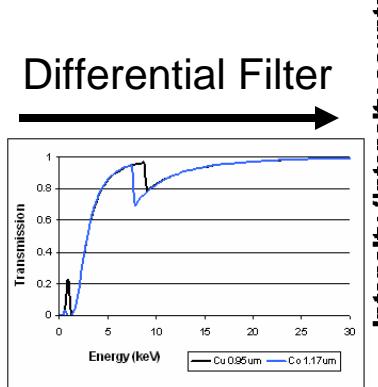
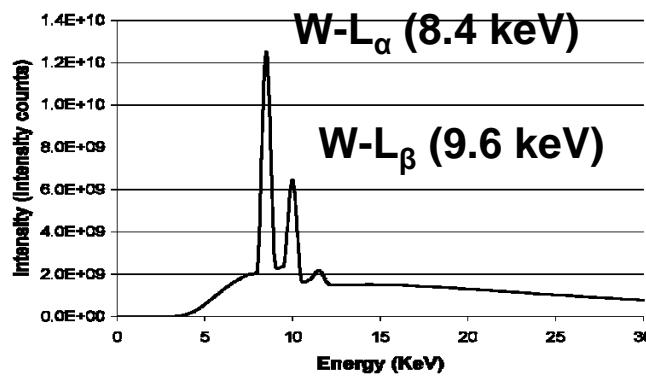
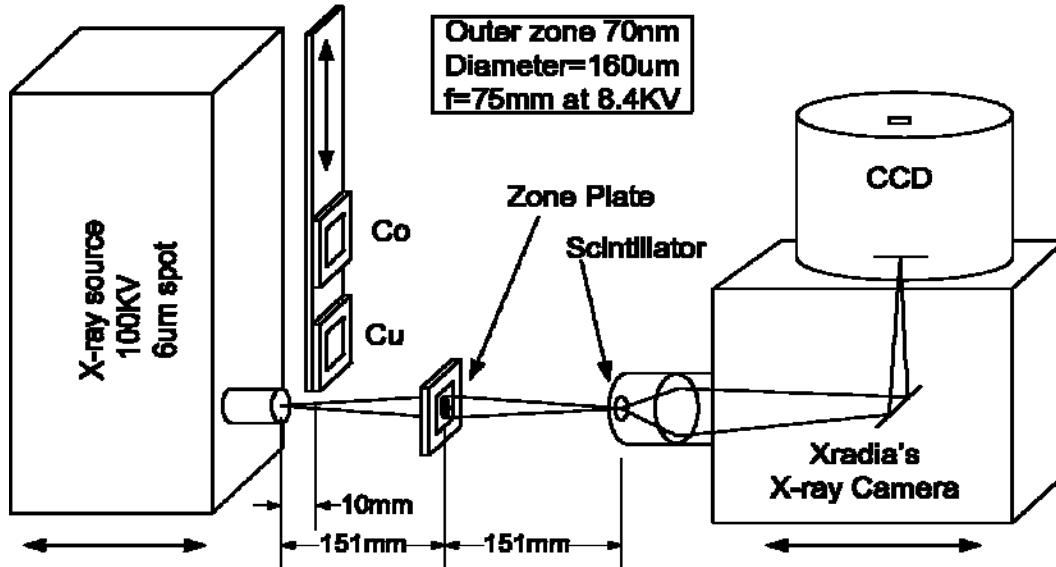


# Gold Zone Plate Efficiency

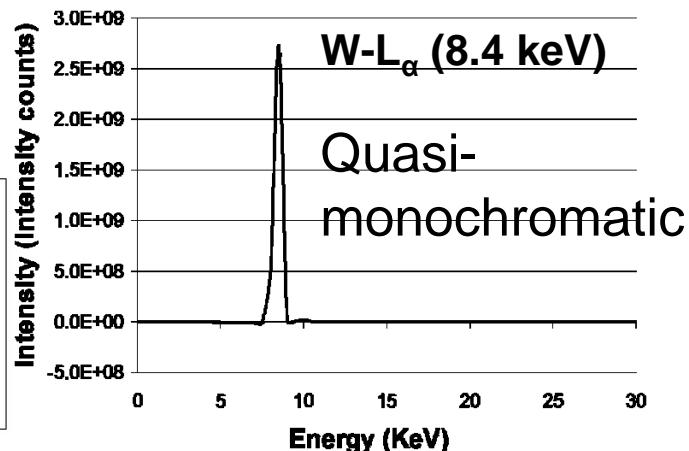
2 aligned ZPs



# Quantitative Efficiency Measurements of Zone Plates Using Laboratory Sources



- Quantitative measurements have been restricted to synchrotron
- Balanced filter method to obtain monochromaticity with laboratory sources
- Final test and process development tool

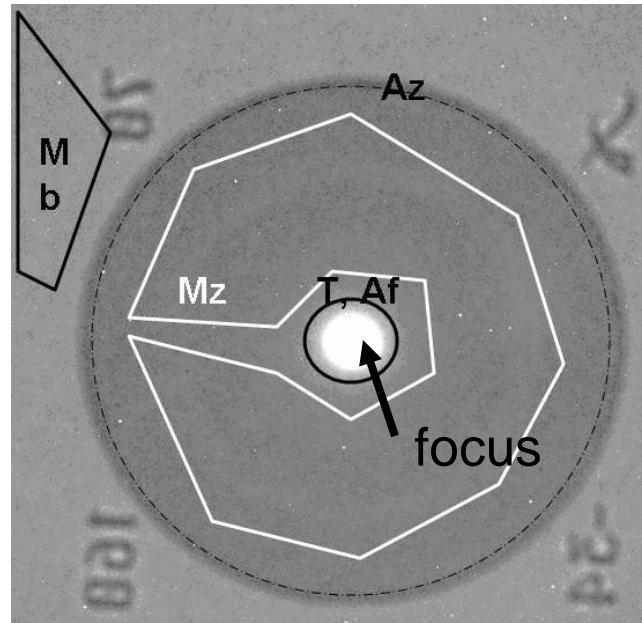


Poly-chromatic source output

# Quantitative Efficiency Measurements of Zone Plates Using Laboratory Sources



Monochromatic projection x-ray image of 70nm zone width, 160um diameter ZP



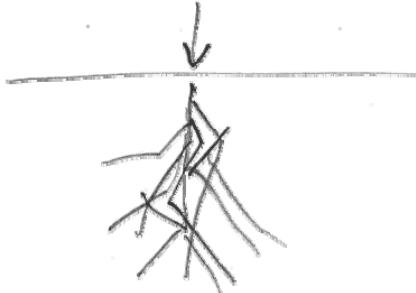
$$\text{Efficiency} = (T - M_Z A_F) / (M_B A_Z) = 8.7\%$$

- Quantitative measurements that agree with synchrotron measurements
- Objective measurement of zone plate efficiency
- Efficiency of 70nm zone plate 700nm zone height measured at 73% of theoretical
- Agreement with synchrotron measurements

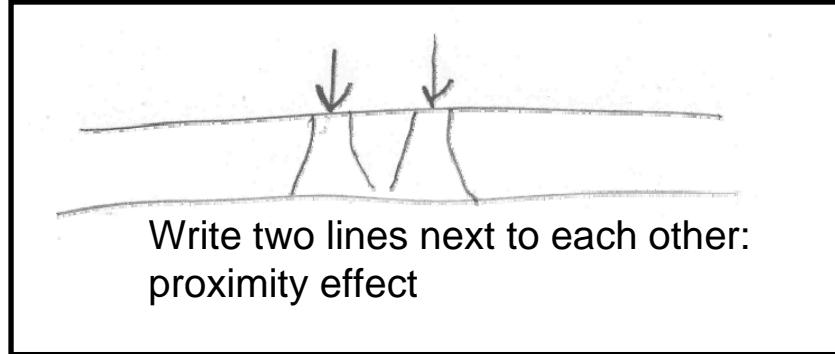
S. Chen, et al., *Journal of x-ray science and technology*, in press

$M_B$ Bkgd intensity (counts/pixel)	$M_Z$ Pedestal intensity (counts/pixel)	$A_Z$ ZP area (pixels)	T focused intensity (counts)	$A_F$ focus area (pixels)
$9.40 \pm 0.1$	$7.00 \pm 0.009$	$157000 \pm 7100$	$157000 \pm 400$	$4100 \pm 300$

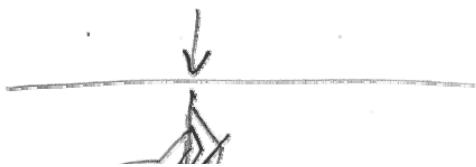
# The Proximity Effect in E-Beam Lithography



Electrons in thick resist:  
sidescatter



Write two lines next to each other:  
proximity effect



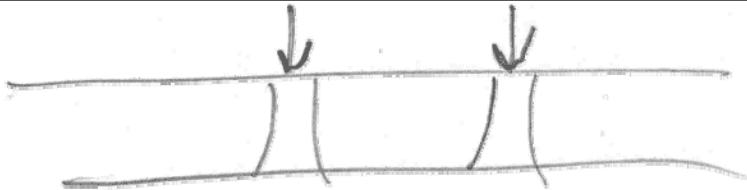
Thin resist, higher voltage:  
reduce sidescatter blurring

- Scattering limits the depth of structures that can be produced
- High (100keV) voltage e-beam writing preferred
- Dense gratings (such as zone plates) suffer proximity effect leading to collapse of tall structures
- Direct write to produce zone plate limited to small zone height

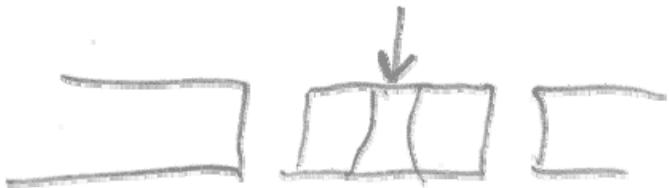
# Avoiding the Proximity Effect



- Proximity effect can be reduced by splitting the process of producing a zone plate into two steps



If lines are farther apart, proximity effect is reduced.



Process every other line, then go back and do the ones you missed (Chao *et al.*, CXRO)

# Heroic efforts at Lawrence Berkeley Lab

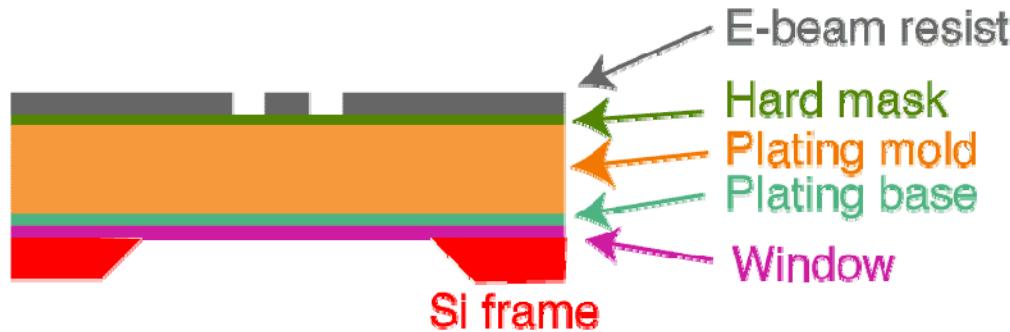


- Chao *et al.*, *Nature* **435**, 1210 (2005):  
15.1 nm half-pitch multilayer slice  
imaged with a 15 nm outermost zone  
width zone plate.
  - Efficiency ~3%.
  - Focal length if used at 290 eV  
edge: 100 µm.
- Other results: 9.2% at 20 nm: Peuker,  
*Appl. Phys. Lett.* **78**, 2208 (2001)

# Tri-Level Processing Scheme

- Write high resolution pattern in top layer.
- Use highly directional reactive ion etching to transfer to a hard mask, and then into a secondary mask. Tennant et al., JVST 19, 1304 (1981); Schneider et al., JVST B 13, 2809 (1995); Spector et al., JVST B 15, 2872 (1997).

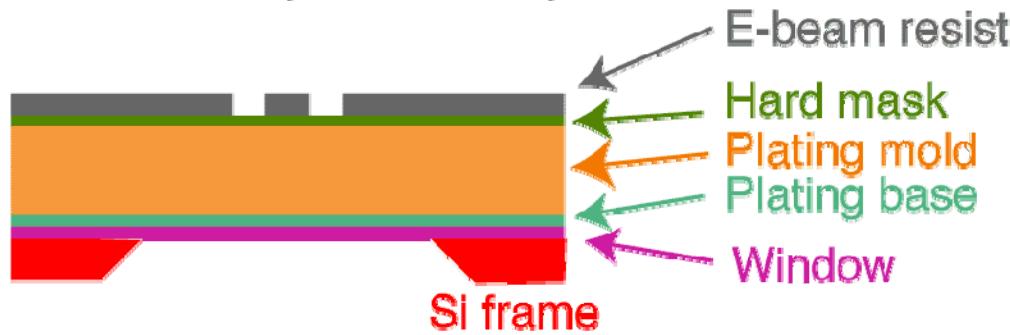
## 1. E-beam expose, develop



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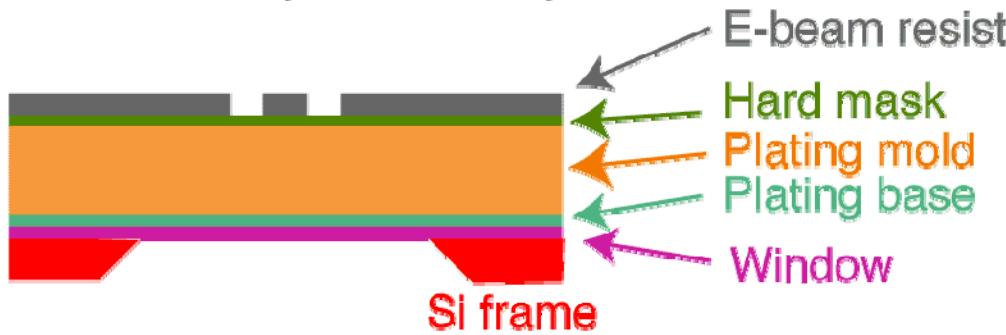
## 2. Etch hard mask



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## 2. Etch hard mask



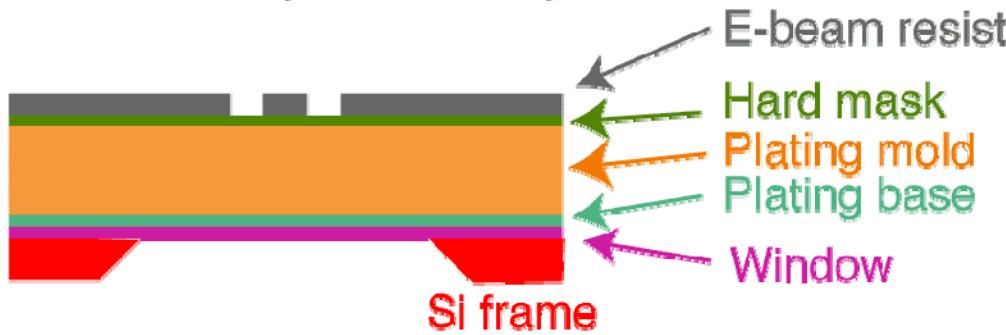
## 3. Etch plating mold; strip hard mask



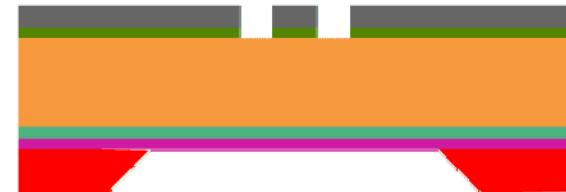
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## 1. E-beam expose, develop



## 2. Etch hard mask



## 3. Etch plating mold; strip hard mask

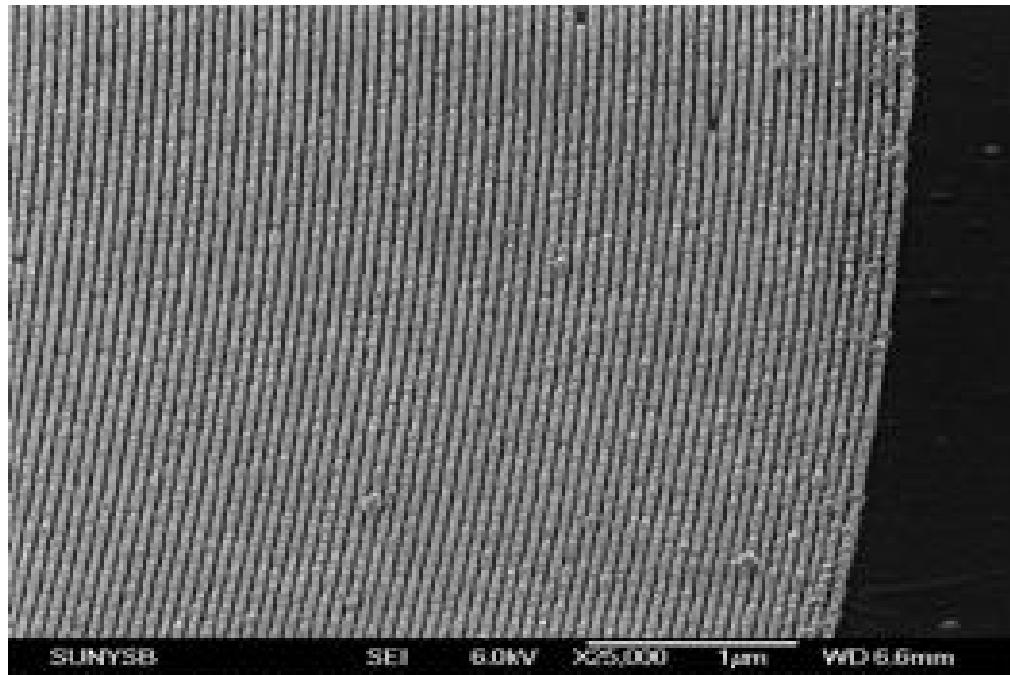


## 4. Metal plating

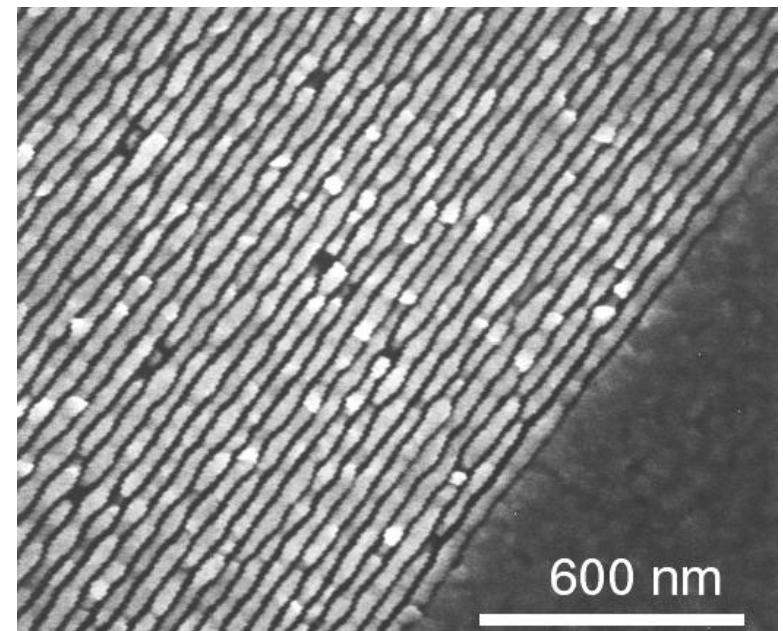


# Zone Plates: Stony Brook

- Spector *et al.* [J. Vac. Sci. Tech. B **15**, 2872 (1997)], Stein *et al.* [J. Vac. Sci. Tech. B **21**, 214 (2003)], Lu *et al.* [J. Vac. Sci. Tech. B **24**, 2881 (2006)].
- Support from NSF and from BNL, collaboration with Don Tennant (Lucent/NJNC; now Cornell)

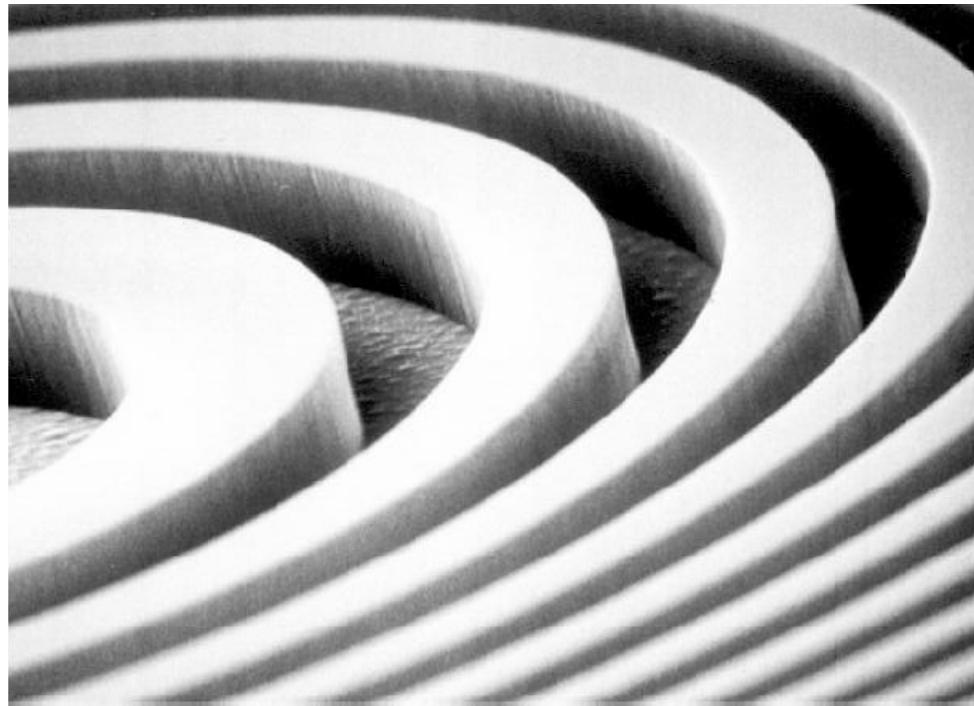


30 nm wide, 130 nm tall Ni, 160 μm diameter

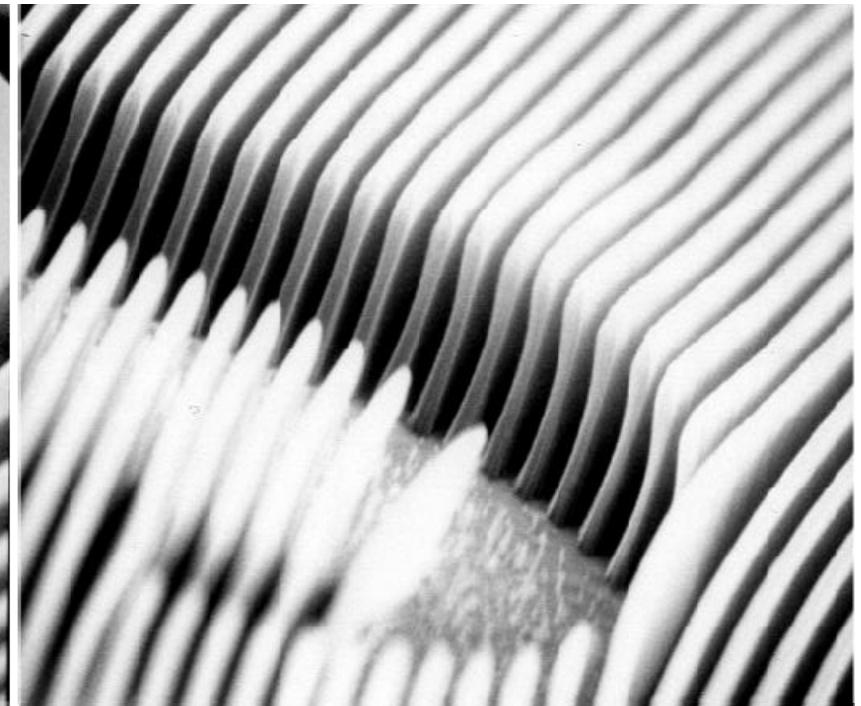


18 nm wide, 60 nm tall Ni, 80 μm diameter

# Hard x-ray zone plates from Xradia Inc.



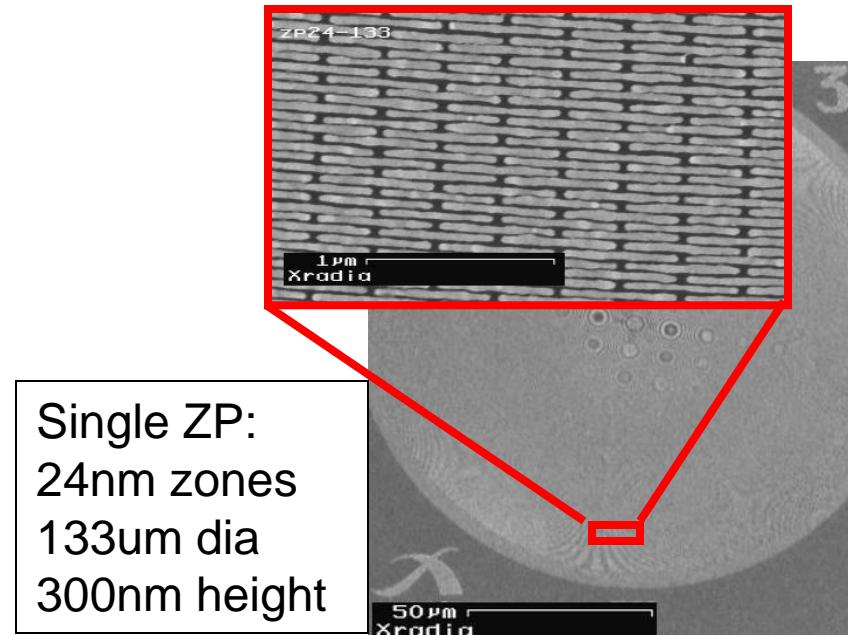
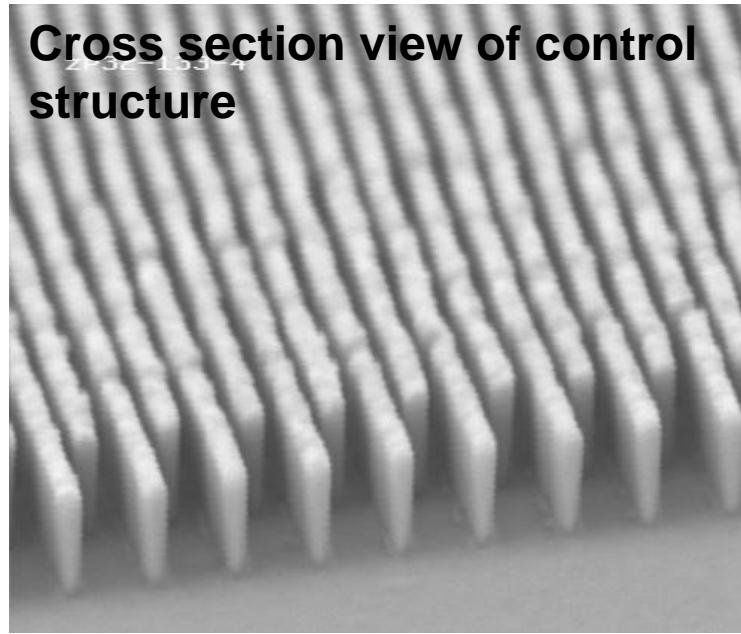
2  $\mu\text{m}$



1  $\mu\text{m}$

Gold zone plates, Xradia, Inc.: 70 nm outermost zones

# Recent Fabrication Highlights at Xradia

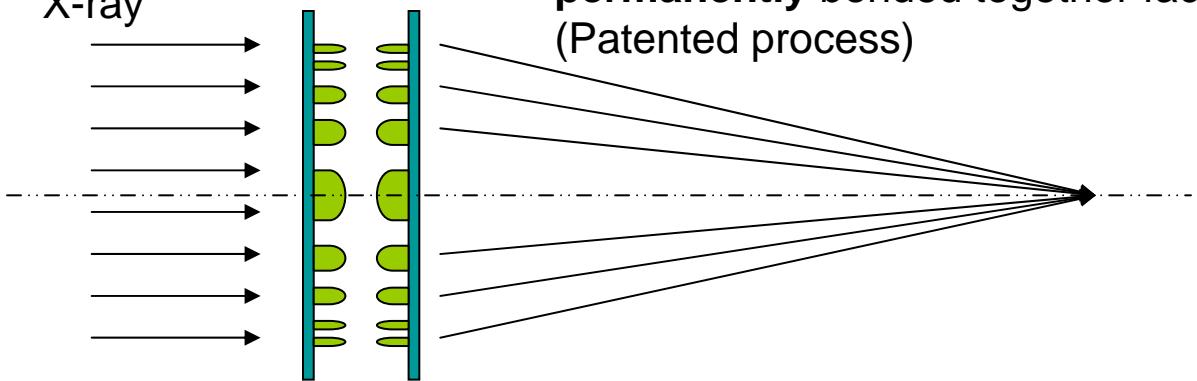


- 32nm gold zone plates, 450nm thick fabricated for CNM nanoprobe project (Xradia under contract), AR=14
- 24nm available now (330nm thick, AR=14), procedure developed to align and bond two ZPs to double AR and thickness (660nm thick, AR=28)

# High-resolution, High-efficiency Zone Plates ZP Alignment



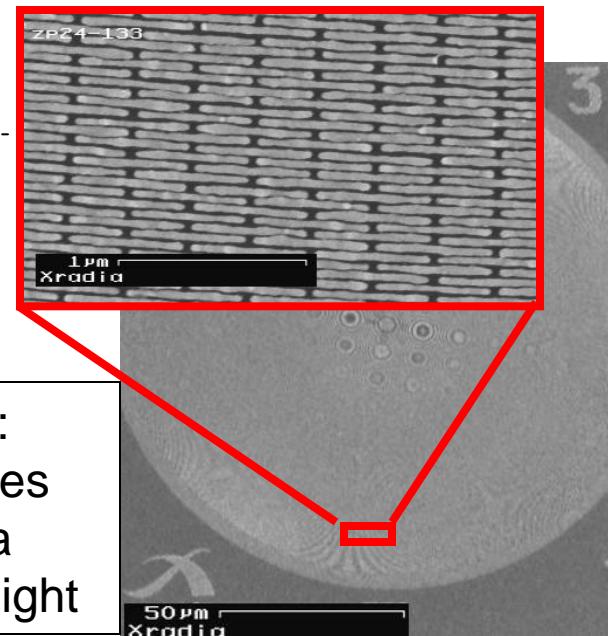
Monochromatic  
X-ray



Two zone plates are aligned and  
**permanently** bonded together face-to-face.  
(Patented process)

Two zone plates act effectively as one  
diffractive element if aligned precisely  
laterally and in very close proximity  
(within depth of focus of lens)

Single ZP:  
24nm zones  
133um dia  
300nm height

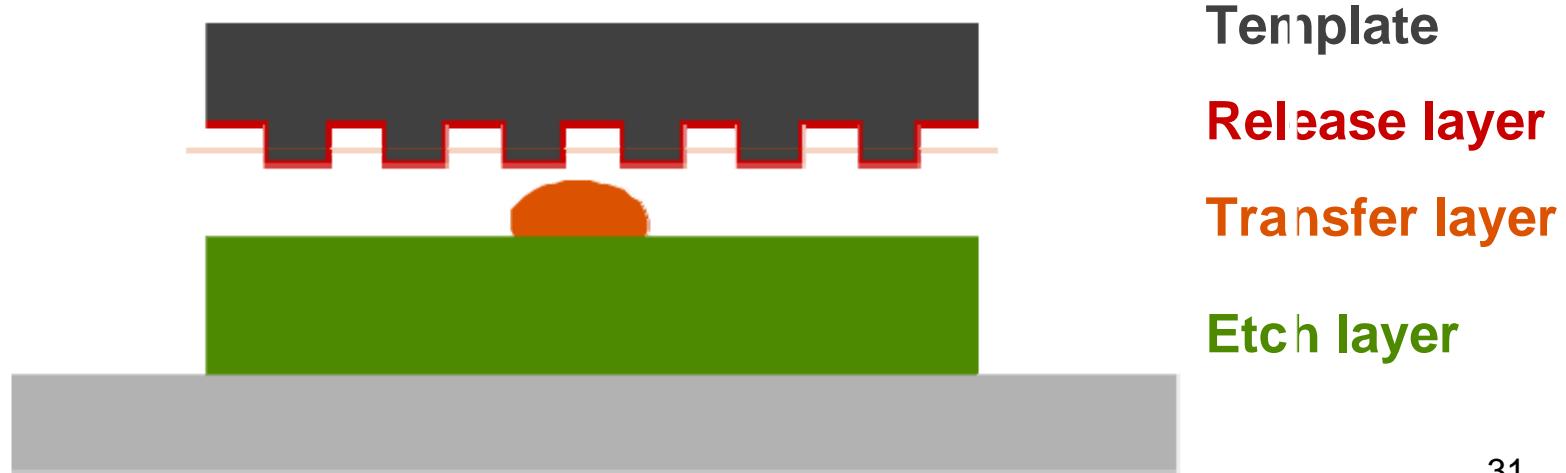


- High-resolution zone plates usually low efficiency
- Alignment to increase zone height increases efficiency
- 24nm zone width zone plates with combined 600nm height in use at ANL ID-26 nanoprobe.

# Disposable zone plates?

- ❑ Nanoimprint lithography: many cheap copies from one master.
- ❑ These slides: step-and-flash imprint lithography (SFIL) as pioneered by Wilson, Srinivasan *et al.*, UT Austin

Step 1: template approaches liquid transfer layer

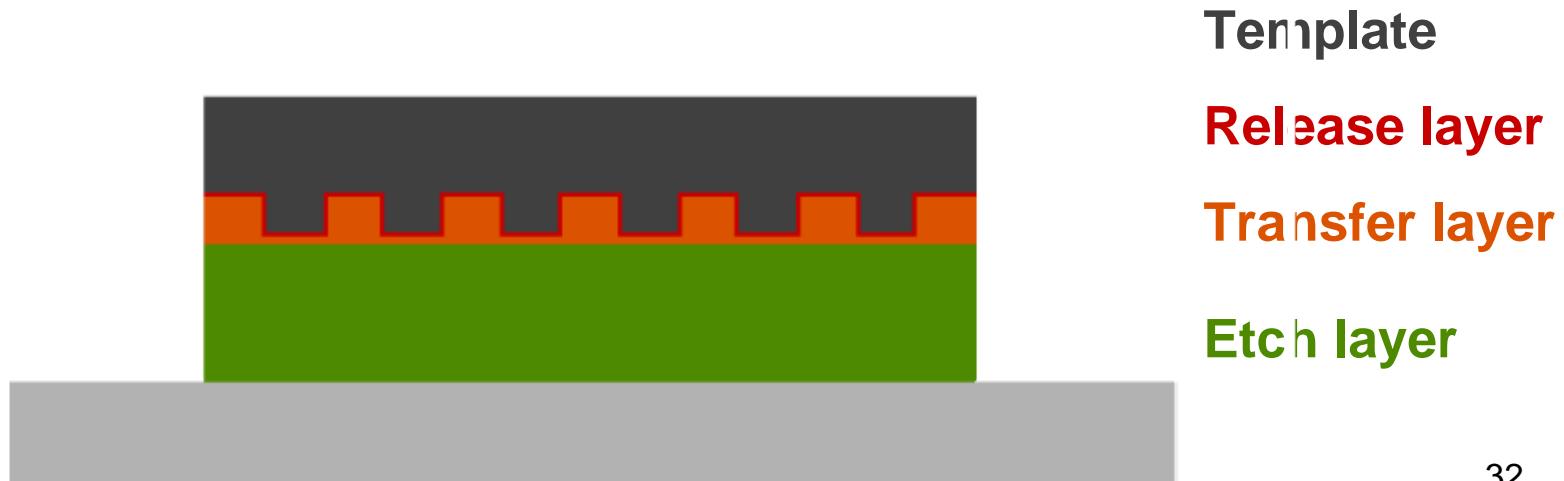


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# Disposable zone plates?

- ❑ Nanoimprint lithography: many cheap copies from one master.
- ❑ These slides: step-and-flash imprint lithography (SFIL) as pioneered by Wilson, Srinivasan *et al.*, UT Austin

Step 2: compress liquid transfer layer, and UV flash to harden

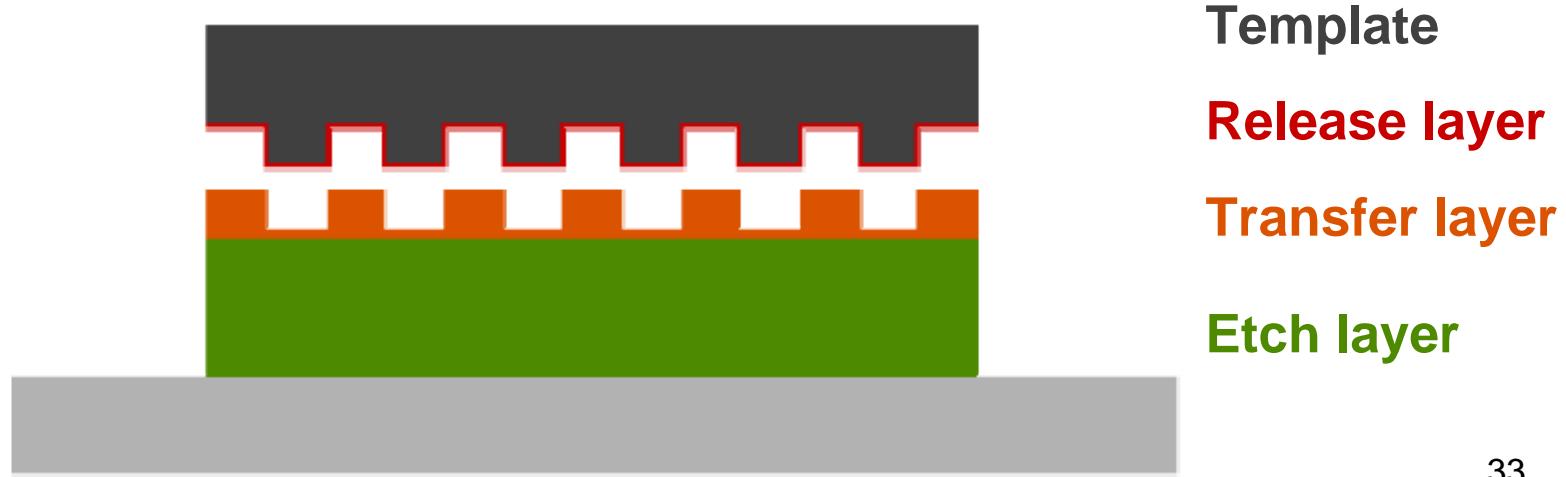


32

# Disposable zone plates?

- ❑ Nanoimprint lithography: many cheap copies from one master.
- ❑ These slides: step-and-flash imprint lithography (SFIL) as pioneered by Wilson, Srinivasan *et al.*, UT Austin

Step 3: remove template

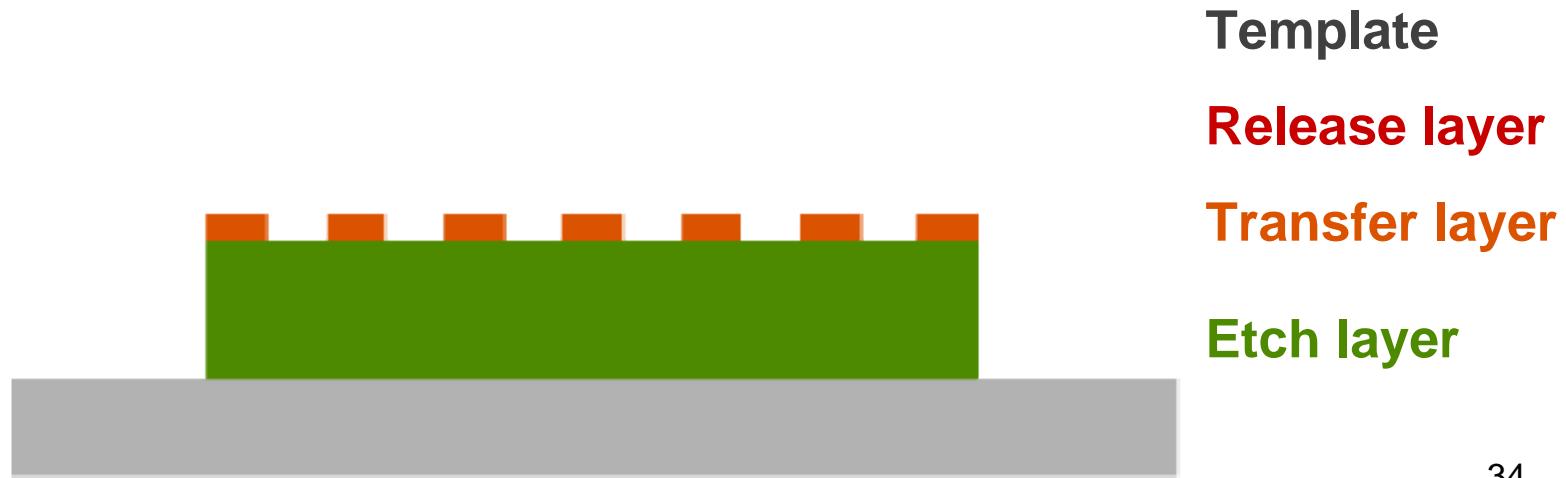


33

# Disposable zone plates?

- ❑ Nanoimprint lithography: many cheap copies from one master.
- ❑ These slides: step-and-flash imprint lithography (SFIL) as pioneered by Wilson, Srinivasan *et al.*, UT Austin

Step 4: etch transfer layer to break through to etch layer

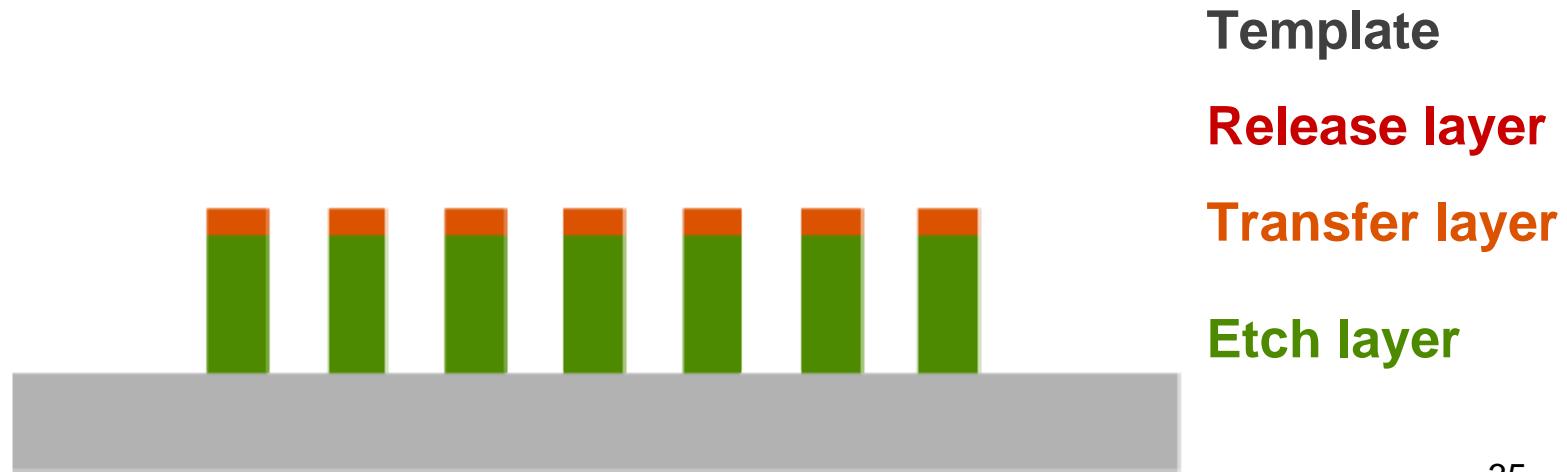


34

# Disposable zone plates?

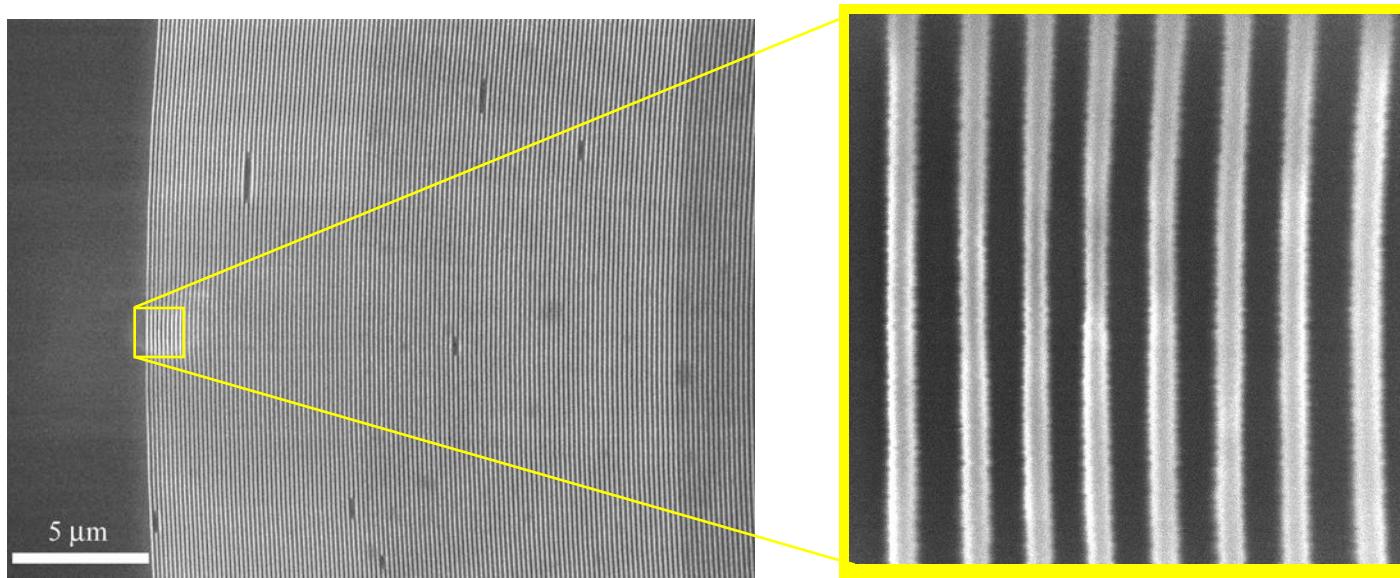
- ❑ Nanoimprint lithography: many cheap copies from one master.
- ❑ These slides: step-and-flash imprint lithography (SFIL) as pioneered by Wilson, Srinivasan *et al.*, UT Austin

Step 5: etch through the etch layer



35

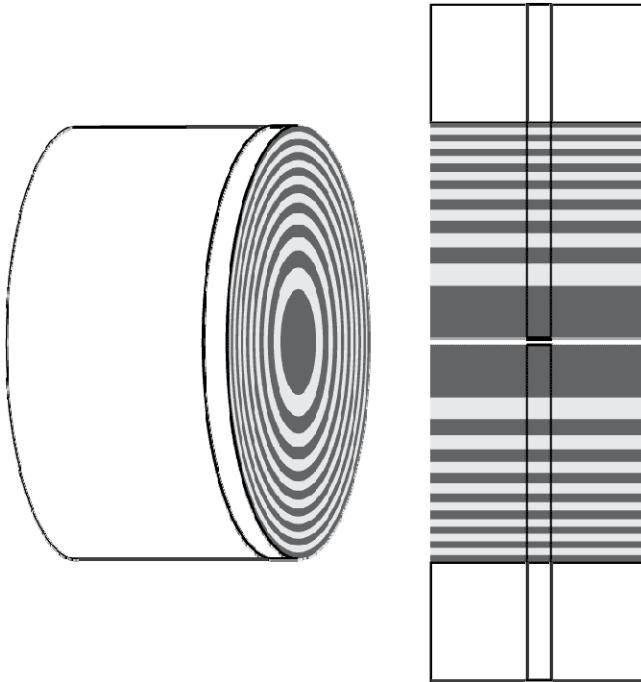
# SFIL zone plates: basic demonstration



50 nm zones replicated in transfer layer from quartz wafer. Stein *et al.*, JVST B **21**, 214 (2003)

# Sputter-sliced or “jelly roll” zone plates

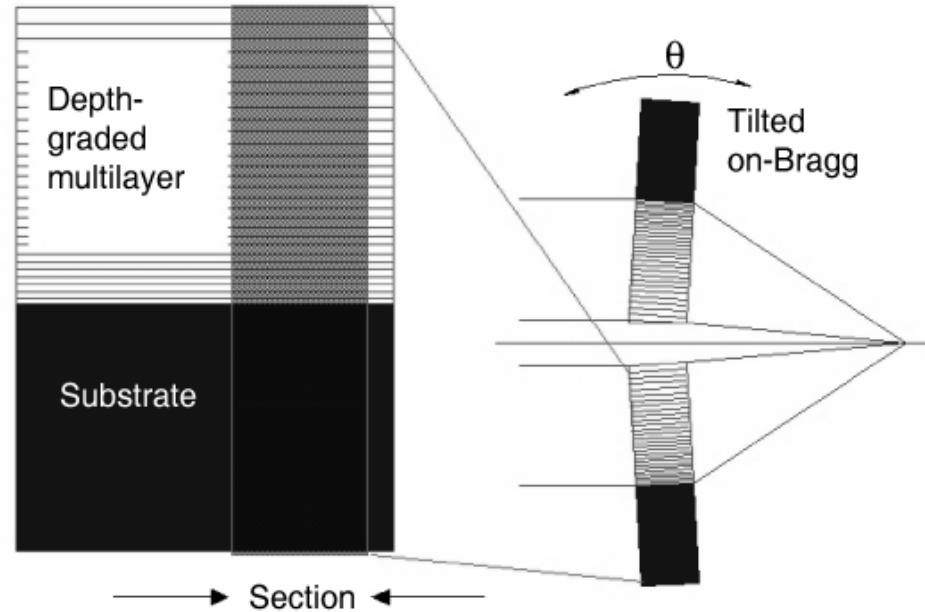
- It's easy to make thin layers! Successive layer deposition on a rotating wire. First proposed by Schmahl and Rudolph in 1980 (Ash, *Scanned Image Microscopy*).
- Many efforts, including Göttingen, Livermore, SPring-8, ESRF...
- Challenges: circularity, error accumulation....



# Multilayer Laue lenses

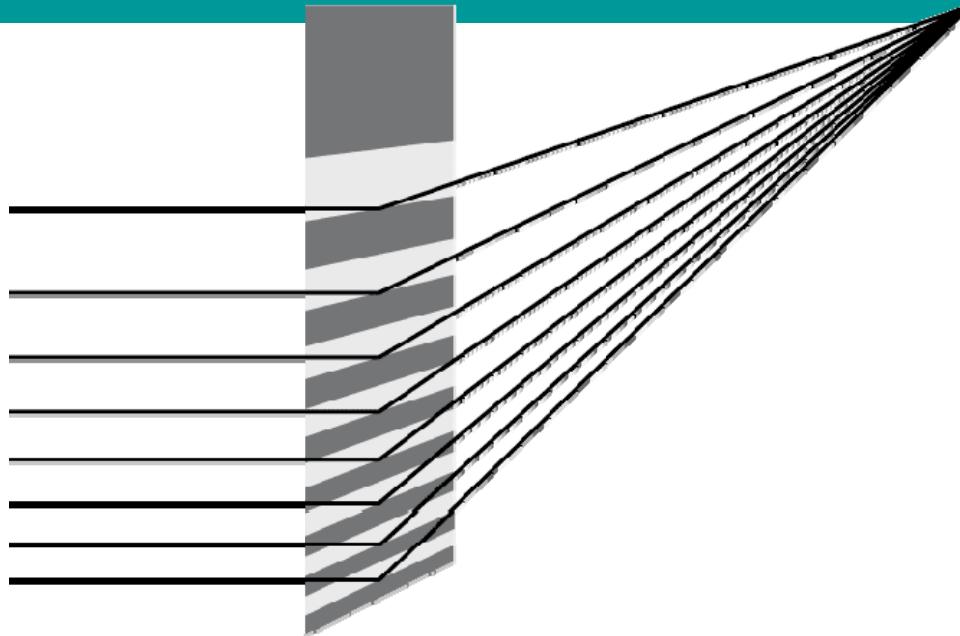
- Forget top-down circles, and go sideways! Start by depositing thinnest zones first on a flat substrate, and work your way up to thicker zones. Cross two 1D lenses for 2D focusing.
- For thick optics, you want to tilt to be on the Bragg condition anyway [Maser, PhD thesis; Maser and Schmahl, *Opt. Comm.* **89**, 355 (1992)]

NSLS II: stated goal is 1 nm resolution using MLLs (or kinoform refractive lenses)



J. Maser et al., *SPIE 5539*, 185 (2004); plus tests by Liu et al., *J. Appl. Phys.* **98**, 113519 (2005); Kang et al., *Appl. Phys. Lett.* **86**, 151109 (2005); Kang et al., *Phys. Rev. Lett.* **96**, 127401 (2006).

# MLLs are not without challenges



Must stay on-Bragg for  
good efficiency



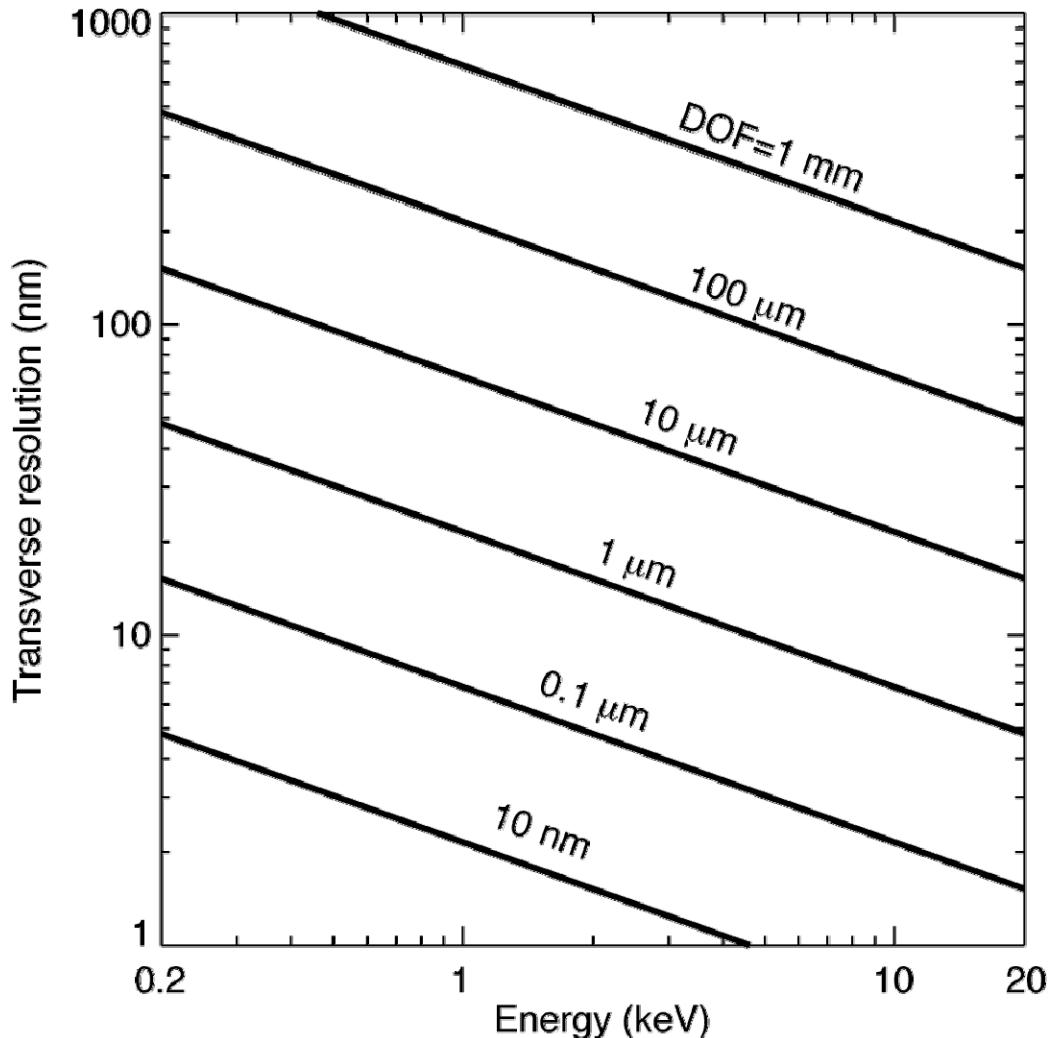
# High resolution: lots of layers!

- Transverse resolution  $\Delta_t = 1.22\Delta_{rN}$ , where  $\Delta_{rN}$ =outermost zone width
- Diameter  $d = 1.22 \lambda f / \Delta_t$ , # zones  $N = 1.22^2 \lambda f / \Delta_t^2$

# Challenge at high resolution: depth of focus

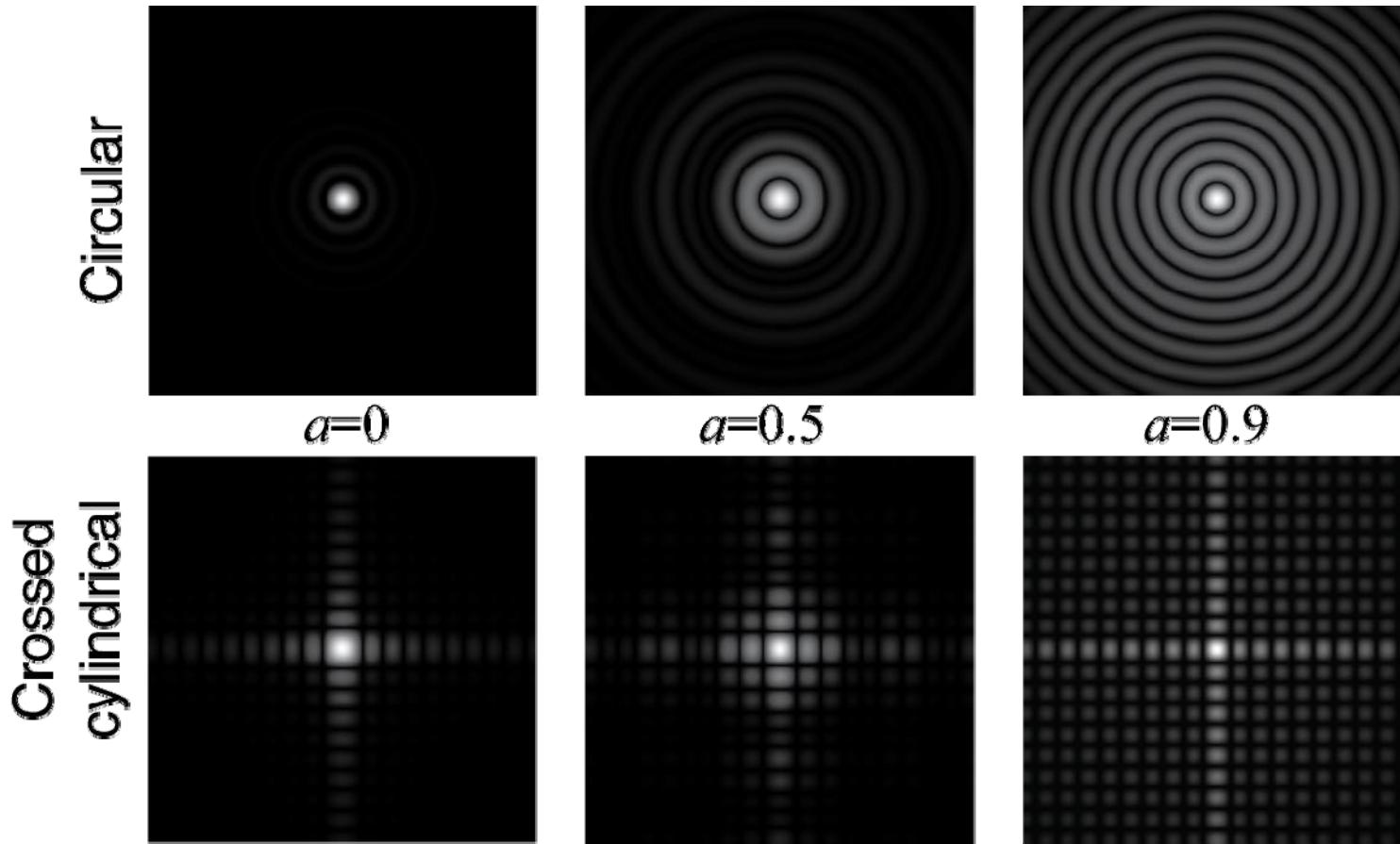


- Depth of focus is  $1.22\lambda/\text{N.A.}$ , or  $4.88(dr_N)^2/\lambda$  where  $dr_N$  is the outermost zone width



# How clean is the focus?

- $a = (\text{central stop diameter}) / (\text{zone plate diameter})$



You really want all zones!

# X-ray optics: best resolution



# X-ray optics: best resolution

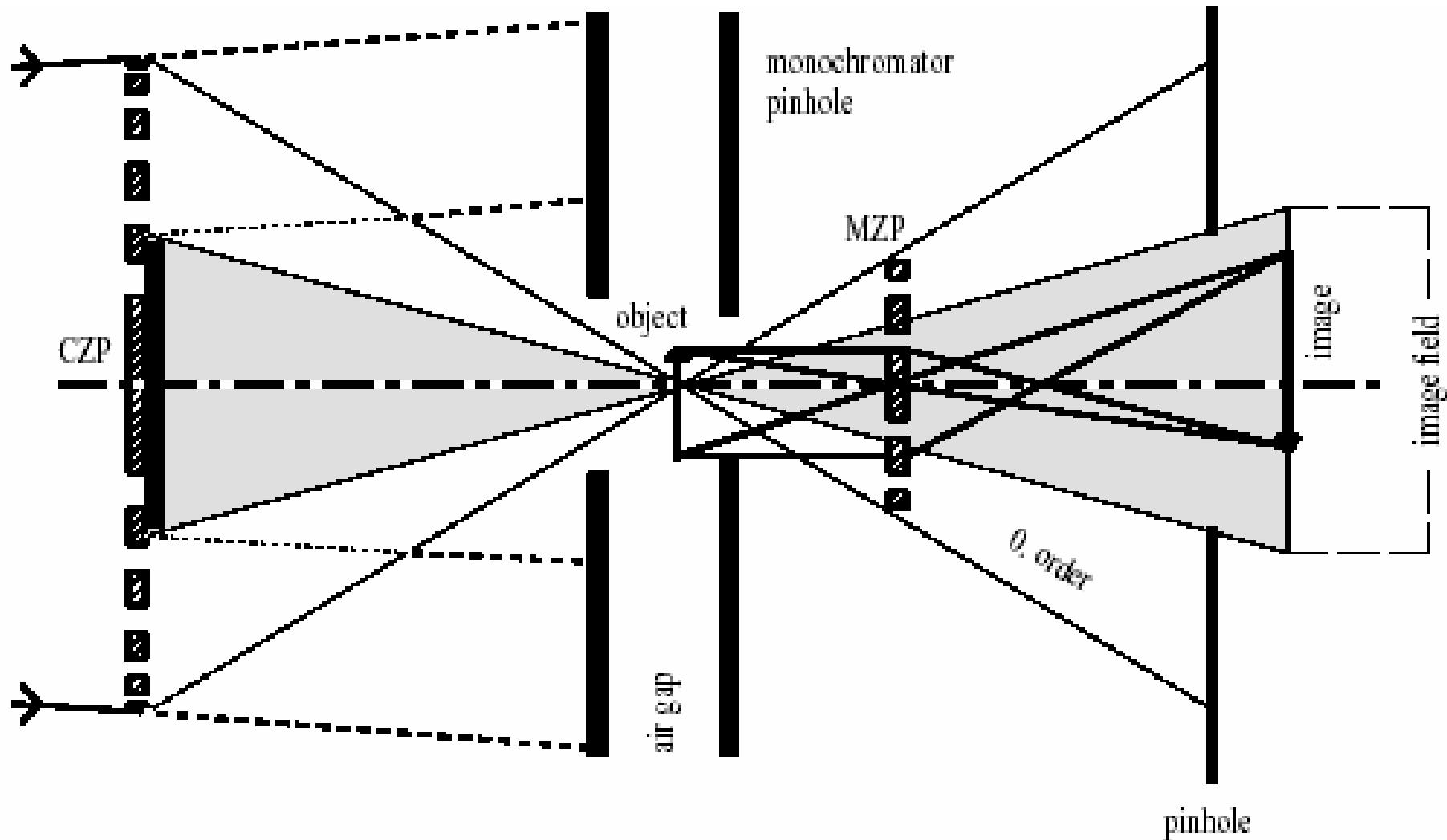


# ZP Uses



- ❑ Microscope objective
- ❑ Condenser/monochromator
- ❑ Microprobe forming lens
- ❑ Beam splitter
- ❑ Works for any wave (including neutrons and atoms)

# ZP based x-ray microscope

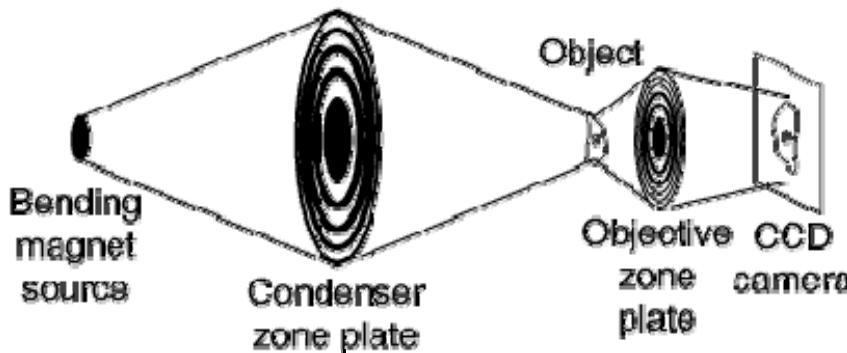


# Full-field and scanning

## □ TXM

- Incoherent illumination; works well with a bending magnet, with fast imaging
- More pixels (e.g.,  $2048^2$ )
- Optic efficiency specimen dose
- Moderate spectral resolution if zone plate condenser used - but most new TXMs use grating/crystal and reflective condenser!

## TXM: transmission x-ray microscope



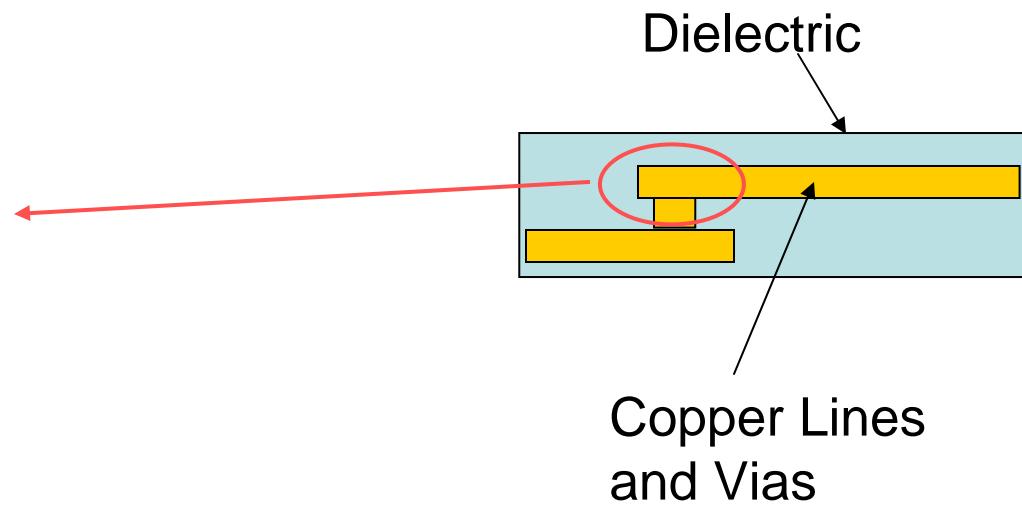
## STXM

- Coherent illumination; works best with an undulator
- Less dose to sample (~10% efficient ZP)
- Better suited to conventional grating monochromator [high  $E/(\Delta E)$ ]
- Microprobes: fluorescence etc.

## STXM: scanning transmission x-ray microscope



# X-Ray Advantage: High-resolution imaging of buried Structures



# Computed Tomography



(1) Sample imaged at various angles to acquire tomographic projections.

Sinogram



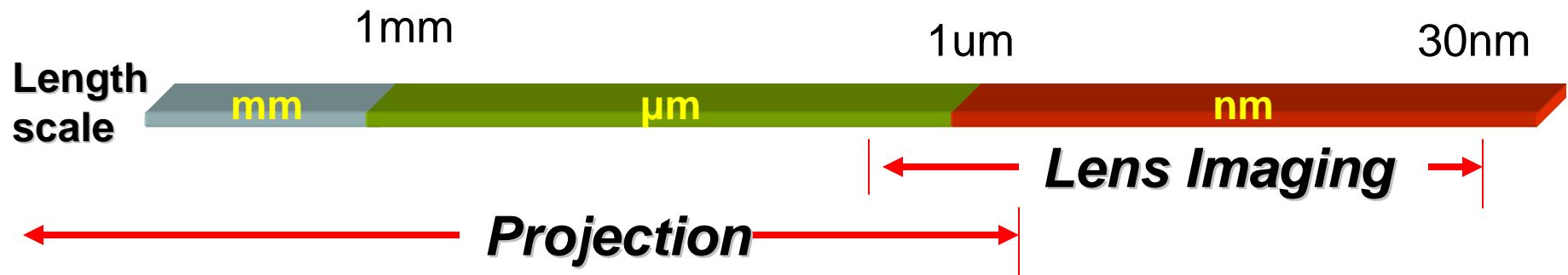
Sample rotation angle

(2) 3D reconstruction by backprojection results in 3D image of the sample.

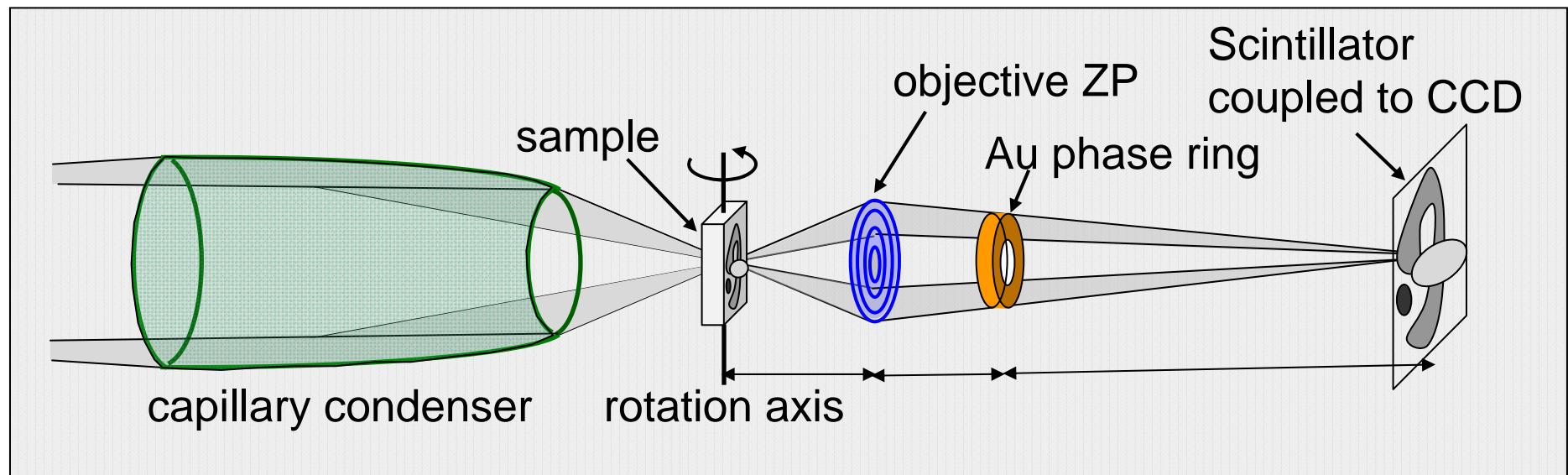
Line Image

# Imaging Length Scale Coverage

**Loss of contrast and throughput leads to a crossover at ~1um resolution**



# X-ray Imaging with High-resolution (nanoXCT) Optics and High Contrast



## □ Key components:

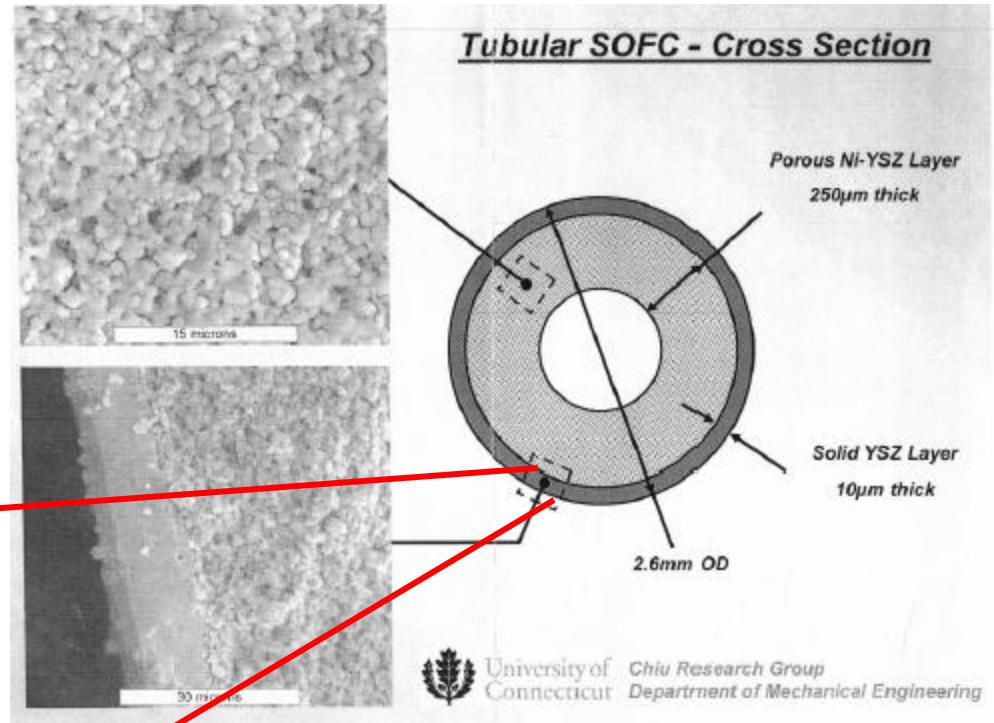
- High efficiency, reflective ellipsoidal capillary condenser
- High-resolution objective zone plate
- Zernike phase contrast phase plate
- High-efficiency, high resolution x-ray detector
- Precision tomography stages



# nm-scale: Tubular Fuel Cell (SOFC)

Courtesy of Dr. W. Chiu (U. Connecticut), Adaptive Materials Inc.

2D transmission x-ray images

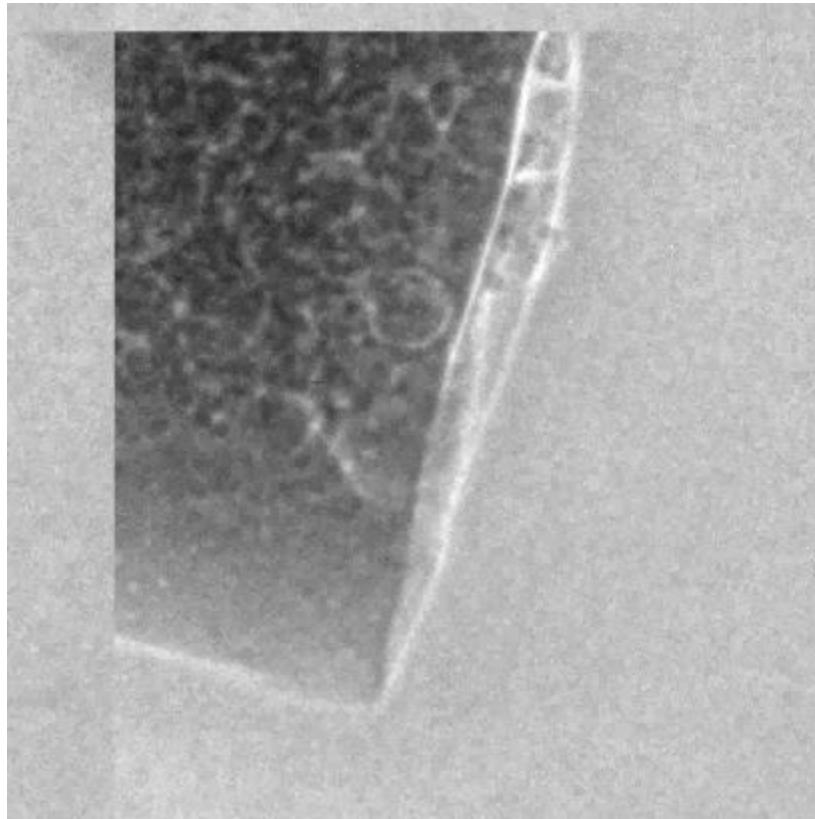


Xradia nanoXCT-8-50-Z  
8keV x-ray energy (stand alone)  
sub-50nm resolution  
Zernike phase contrast

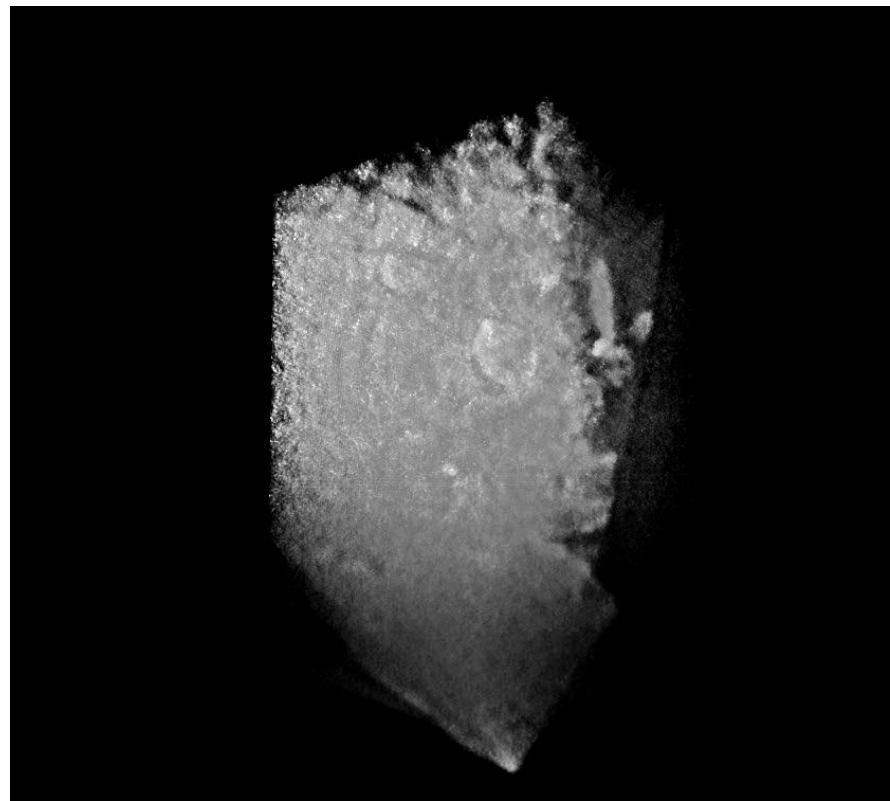
# Tubular Fuel Cell (SOFC)



2D transmission x-ray projection  
images (0-90 degree rotation)



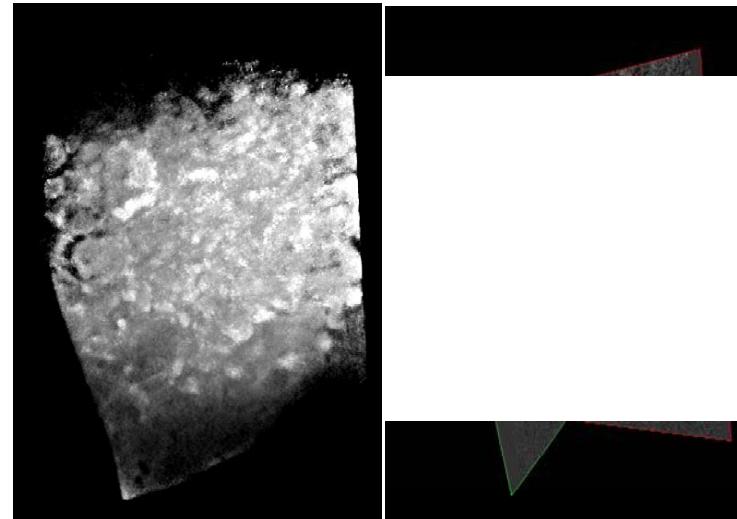
Reconstructed 3D volume



# SOFC Pore Structure Imaging – cont'd

## □ nanaoXCT Experiment details

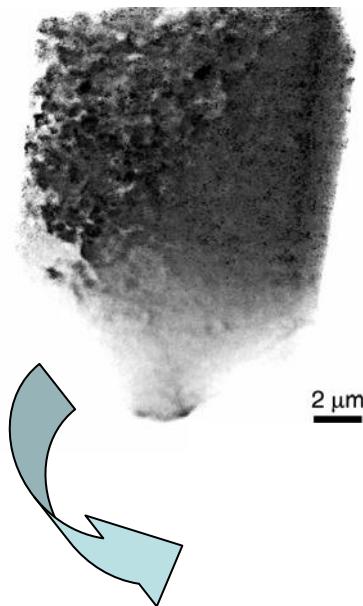
- Xradia (Concord, CA)
- 8 keV copper source
- 181 projections at 300 sec per projection
- 22.6  $\mu\text{m}$  field of view
- 50 nm resolution
- 3-D tomographic reconstruction



# Putting It All Together

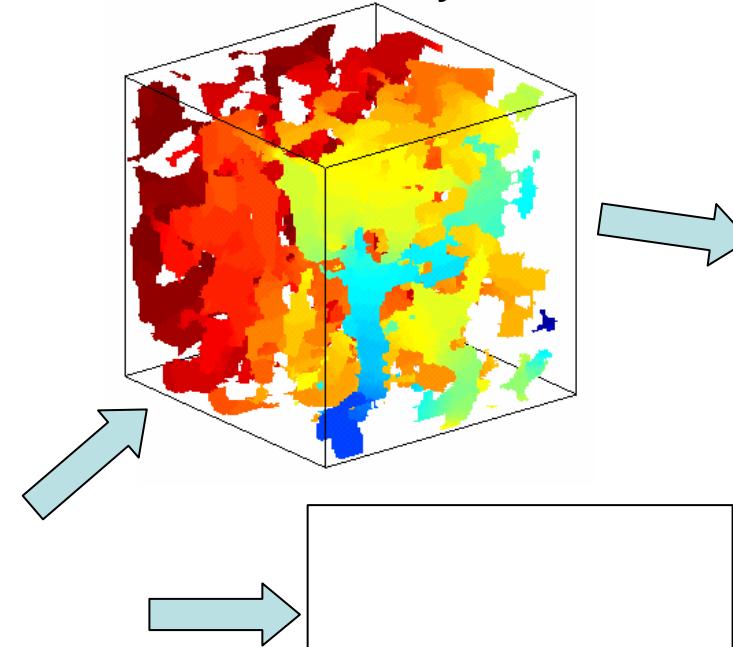


nXCT-Imaged  
SOFC Anode



3D  
Reconstruction

Gas Transport, Reformation &  
Electrochemistry



User Models



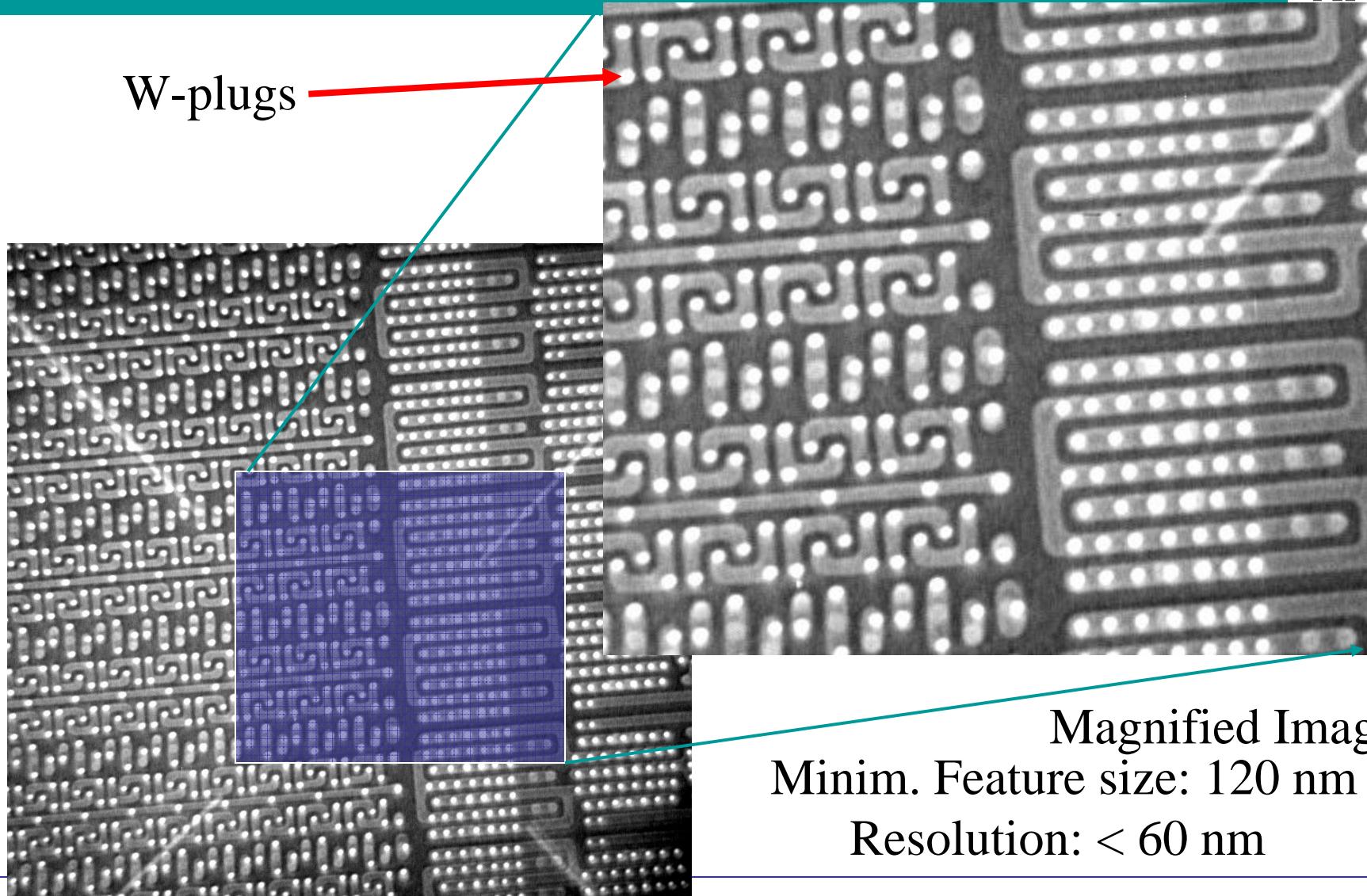
Optimum  
Structure

Parameters

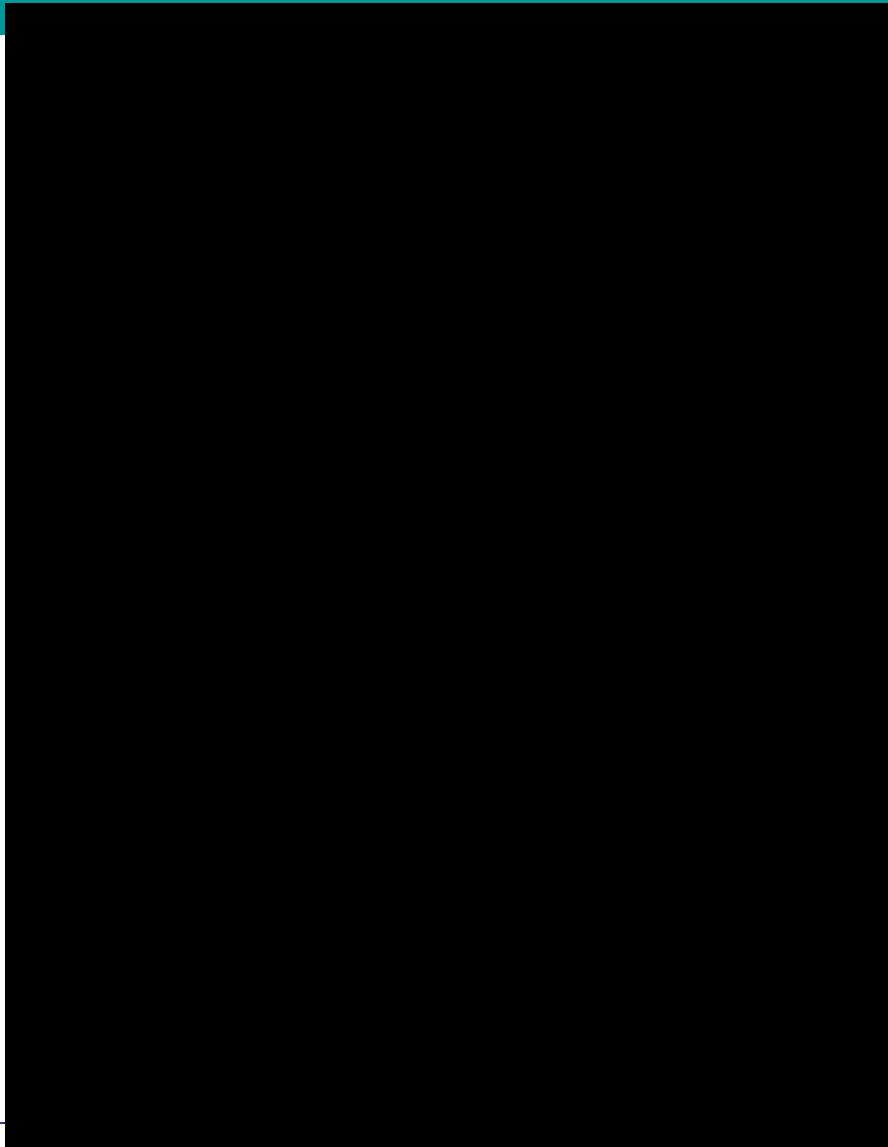
$\varepsilon \tau \langle r \rangle \langle r^2 \rangle$   
 $D_{ij} D_{ij}^k \mu k$   
 $\eta_{ohm} \eta_{conc} \rho$   
 $[i_o \beta \eta_{act} L_{TPB}]$

Ionic & Electronic  
Charge Transfer

# M1 Metal Layer IC Sample



# Raw Image Data of Cu-Interconnect

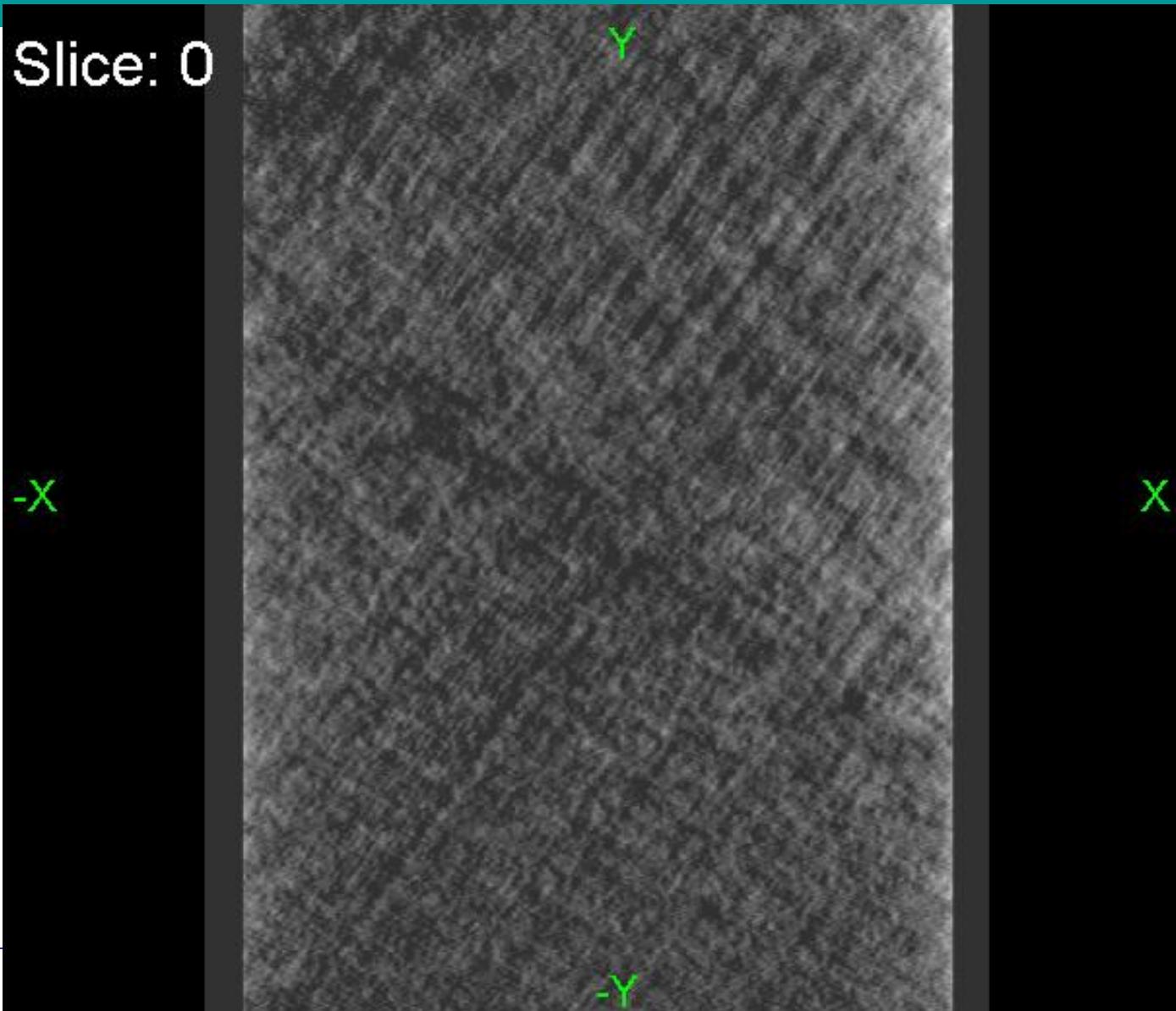


- Cr 5.4keV x-ray energy
- Cu interconnect sample with 5 layers of trenches and interconnecting vias
- 6 hr data collection time
  
- Bright structures are Cu

— 1 $\mu$ m

# CT Reconstruction – Planar Slices

Slice: 0

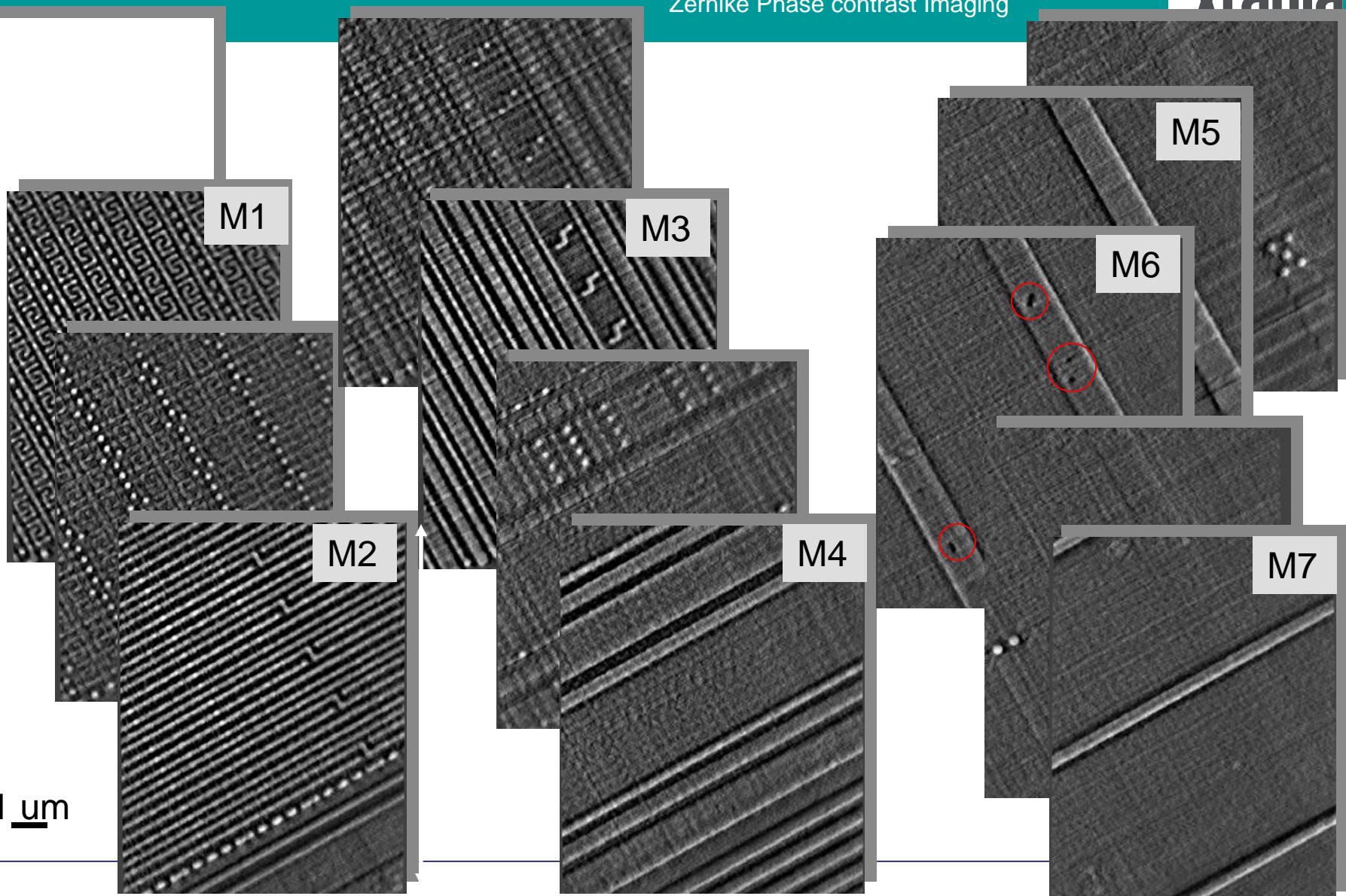


- Cu Layers, and W Layer clearly resolved

# Extracted Layers of Pentium 4 chip (120nm node)



Cu (8 keV) Laboratory x-ray source  
Zernike Phase contrast Imaging



1  $\mu\text{m}$

8/13/2008

SPIE X-ray Focusing Workshop

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# Technologically Relevant Application: TSV - Through-Silicon Vias (10um Diameter)

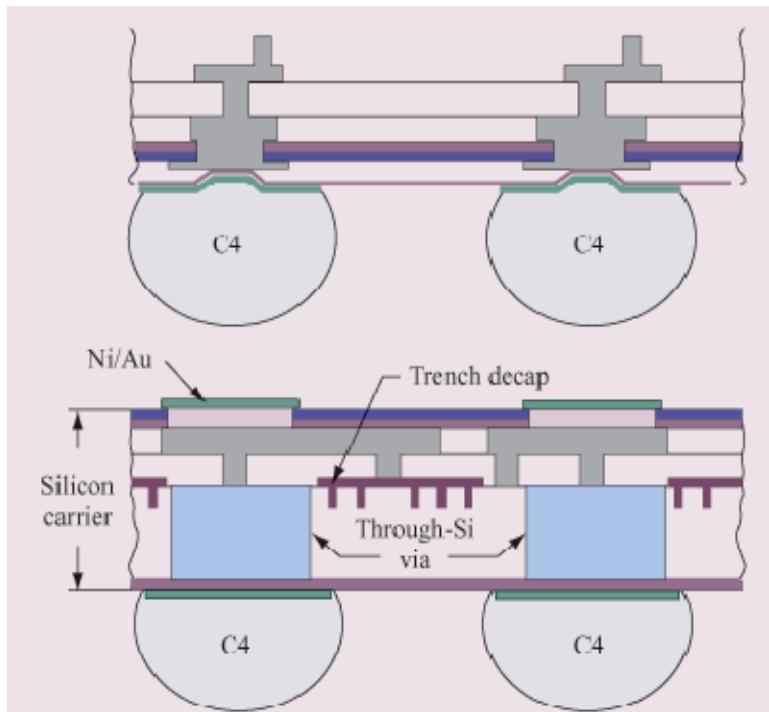


10  $\mu\text{m}$  vias tilted at 45 degree.  
Tile of 3x3 images 66x66  $\mu\text{m}$  each

All vias have missing electroplating  
(key hole) in center

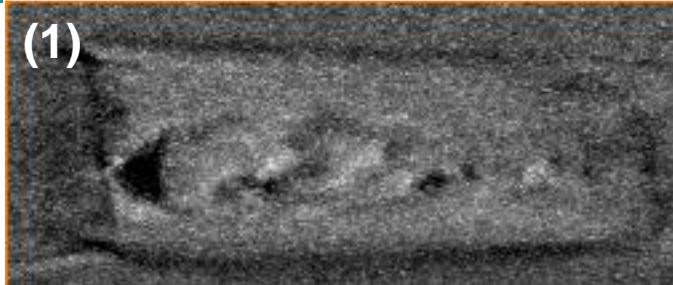
50  $\mu\text{m}$

Large field of view mode  
2 minute exposure per tile

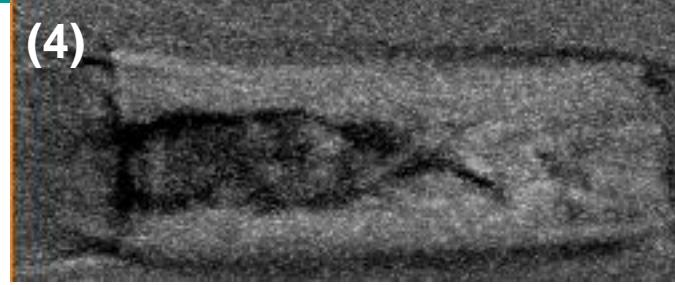


# Detailed X-ray Tomography of Single Via

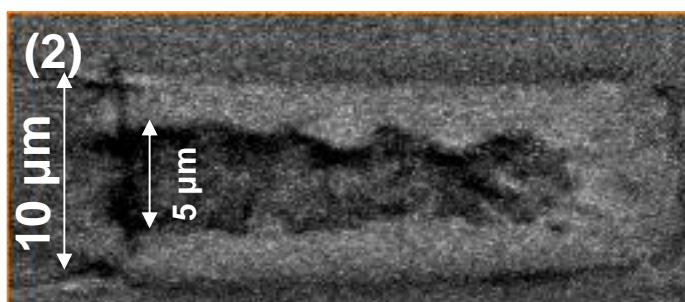
(1)



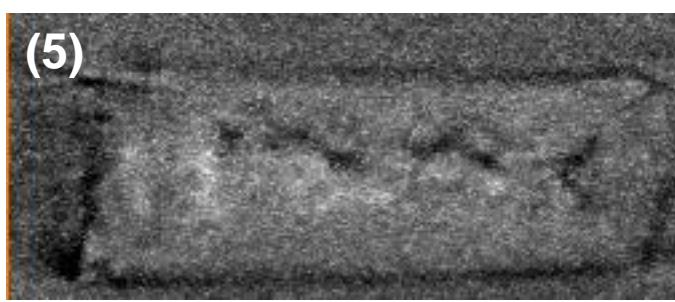
(4)



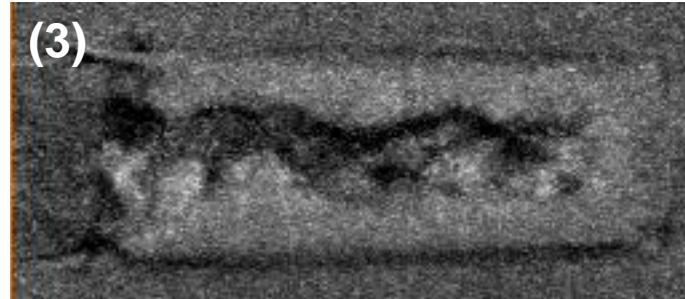
(2)



(5)



(3)



nanoXCT allows direct visualization of the key hole without physical cross-sectioning



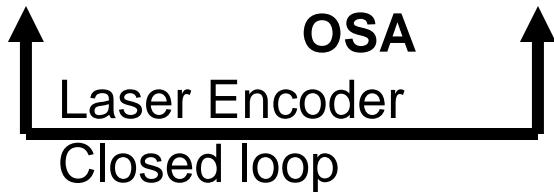
# Scanning Microscope Geometry and Detectors

## Coherent X-ray Beam

## Sample

Transmission  
Detector  
“Structure”

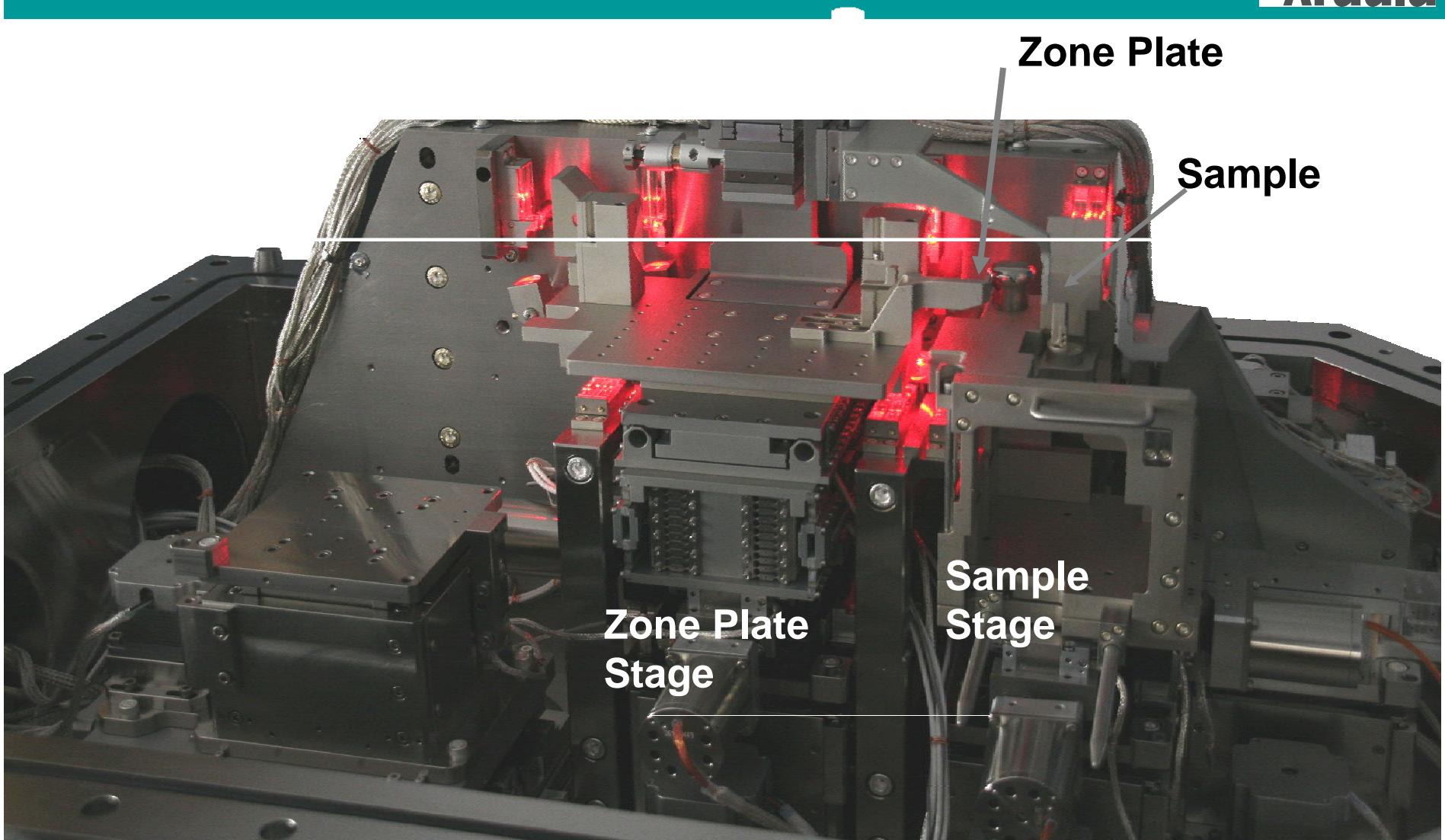
## Zone Plate



Fluorescence / Diffraction  
Detector  
“Phase / Chemistry”

- 30nm x-ray probe probes local elemental composition (fluorescence) and crystallinity (diffraction)
- Vibration and drift stability between zone plate and sample are critical for performance
  - laser encoding and stiff stages needed!
- Platform also suited for other coherence based experiments such as diffraction imaging, zone plate holographic methods

# Sub-nm Resolution Laser Doppler Encoder



# **Application Example Fluorescence: Marine Biology Trace Metals in Plankton and Global Carbon Balance**

- Standard approach: bulk analysis
- X-ray microscopy: separate and study individual organism

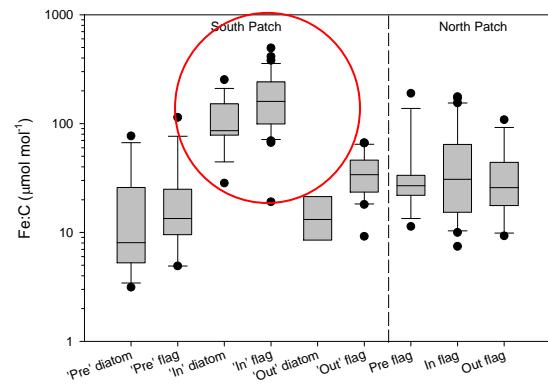
Visible light



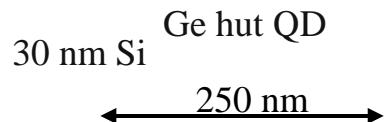
- B. Twining, S. Baines *et al.*, Marine Sciences Research Center, SUNY Stony Brook
- A. Osanna, C. Vaa, B. Winn, S. Wirick, C. Jacobsen, Dept. of Physics & Astronomy, SUNY Stony Brook

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Composite:  
Cl, Fe, Cu

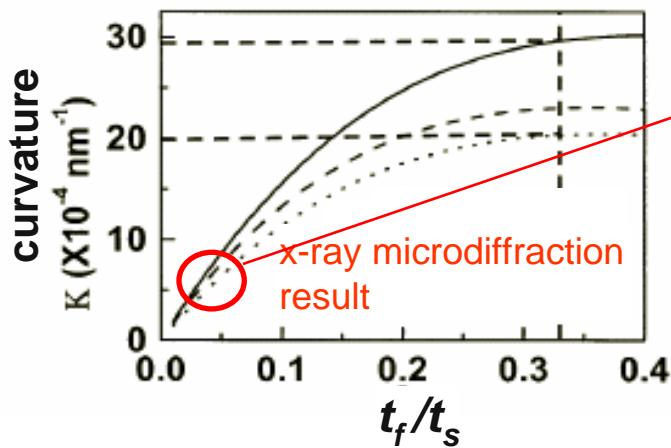


# Application Example Diffraction: - Quantum dot stressors on Si Nanomembranes

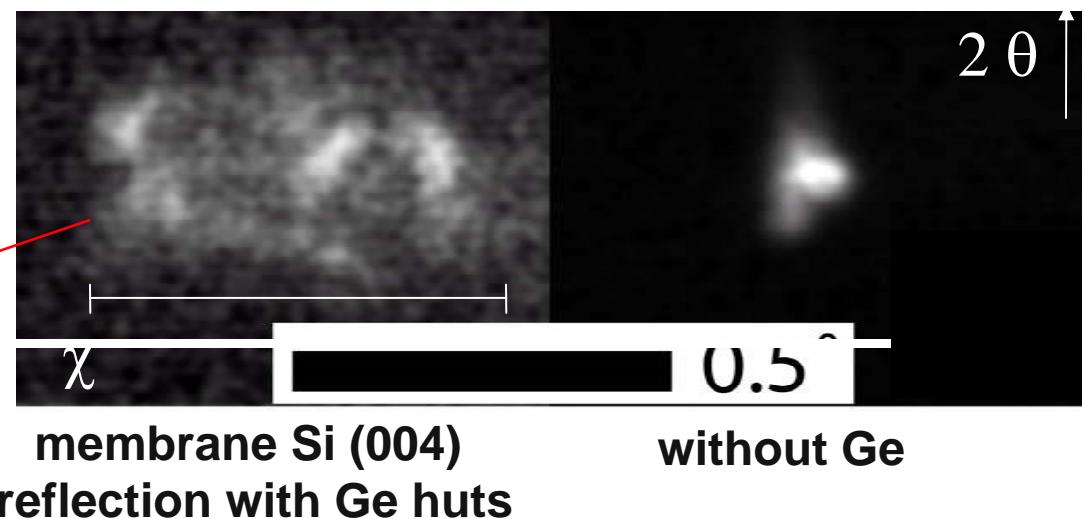


**Ge-Si Lattice Lattice Mismatch  
Distorts Si Membrane**

*Prediction: F. Liu, M. Huang, P. Rugheimer, D. E. Savage, and M. G. Lagally, Phys. Rev. Lett. (2002)*



Microdiffraction at  
APS Sector 2  
 $h\nu=11.2 \text{ keV}$   
200 nm spot



University of Wisconsin MRSEC IRG1

P. G. Evans, D. S. Tinberg, M. M. Roberts, M. G. Lagally,  
Y. Xiao, B. Lai, and Z. Cai, *APL* **87**, 073112 (2005).

# Summary / Outlook





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